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A COMBINED ADAPTIVE TABU SEARCH AND SET
PARTITIONING APPROACH FOR THE CREW SCHEDULING
PROBLEM WITH AN AIR TANKER CREW APPLICATION

DISSERTATION

Todd E. Combs, Captain, USAF

AFIT/DS/ENS/02-04

DEPARTMENT OF THE AIR FORCE
AIR UNIVERSITY

AIR FORCE INSTITUTE OF TECHNOLOGY

Wright-Patterson Air Force Base, Ohio

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Abstract This research develops the first metaheuristic approach to the complete air crew scheduling problem. It develops the first dynamic, integrated, set-partitioning based vocabulary scheme for metaheuristic search. Since no benchmark flight schedules exist for the tanker crew scheduling problem, this research defines and develops a Java (TM) based flight schedule generator. The robustness of the tabu search algorithms is judged by testing them using designed experiments. An integer program is developed to calculate lower bounds for the tanker crew scheduling problem objectives and to measure the overall quality of solutions produced by the developed algorithms.		
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TANKER CREW APPLICATION

DISSERTATION

Presented to the Faculty

Graduate School of Engineering and Management

Air Force Institute of Technology

Air University

Air Education and Training Command

in Partial Fulfillment of the Requirements for the

Degree of Doctor of Philosophy

Todd E. Combs, B.S., M.S.

Captain, USAF

August 2002

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APPROACH FOR THE CREW SCHEDULING PROBLEM WITH AN AIR
TANKER CREW APPLICATION

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Todd E. Combs

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Abstract

Aerial refueling is a crucial component of modern day military operations. A vital part of this refueling process is the individual tanker crews. Constrained by the number of tanker crews available, the United States Air Force must find ways to efficiently schedule them.

This research develops two effective tabu search approaches to Air Mobility Command's tanker crew scheduling problem. The first is an adaptive tabu search with intensification. The second is a hybrid adaptive tabu search/set partitioning scheme that combines the metaheuristic tabu search with a classical optimization approach. The research shows that group theory can be used to effectively direct the search process of each algorithm.

Since no benchmark flight schedules exist for the tanker crew scheduling problem, this research developed a JavaTM based flight schedule generator. The robustness of the developed tabu search algorithms is judged by testing them using designed experiments. An integer program (IP) is developed to calculate lower bounds for the tanker crew scheduling problem objectives and to measure the overall quality of solutions produced by the developed algorithms. The results show that either algorithm significantly improves the solutions found by the currently used heuristic methodology.

A COMBINED ADAPTIVE TABU SEARCH AND SET PARTITIONING
APPROACH FOR THE CREW SCHEDULING PROBLEM WITH AN AIR
TANKER CREW APPLICATION

I. Introduction

1.1 General Discussion

This research significantly contributes to the efficient scheduling of Air Mobility Command's (AMC) tanker crews. The general airline scheduling problem has been studied for over 30 years, with markedly increased interest in the last decade. Previous research has developed extensive optimization and heuristic algorithms for the airline crew scheduling problem, but it has focused little effort on the use of metaheuristics such as tabu search. In addition, the United States Air Force (USAF) has focused its analytic efforts on the scheduling of aircraft for aerial refueling and paid less attention to the crew assignment component of the problem. This research uses the tabu search metaheuristic to solve the USAF tanker crew scheduling problem (TCSP).

1.2 Motivation

One of the most important aspects of running an operational Air Force flying unit or major airline is scheduling flight crews. Once the Air Tasking Order (ATO) or airline schedule is published to specify the flights to be flown daily, crews must be intelligently assigned to each flight. For today's airlines, crew costs are the second highest component

of direct operating costs, with the fuel cost being the highest (Gershkoff, 1989:30). Crew costs such as temporary duty (TDY) per diem are also a significant portion of the direct operating costs of any flying unit within the U.S. Air Force, but the mission of the Air Force contains many more important concerns. Since many flying units operate with an insufficient number of crews, improper crew scheduling will further limit combat operations. A recent Air Force Times article addresses this issue (Simon, 2000:10). When lives and national interests are on the line, any increase in the probability of mission failure is unacceptable.

In addition to cost, many other factors must be considered in tanker crew scheduling. The USAF dictates the handling of its crews through various regulations. For example, a crew's flight duty period starts when an aircrew reports for a mission, briefing, or other official duty and ends with an outbriefing following engine shut down at the completion of a mission, mission leg, or a series of missions (AFI11-202V3, 1998:43). Air Force Instruction 11-202 Volume 3 (AFI 11-202V3) states that the maximum flight duty period for a tanker aircrew is 16 hours (1998:44). Many other such constraints apply to the TCSP, and they are defined in Section 4.1. For commercial airlines, the Federal Aviation Administration (FAA) has also established complex rules to ensure that crewmembers fulfill their duties at an appropriate performance level.

These regulations, combined with the nature of the underlying combinatorial problem, make the crew scheduling problem (CSP) very difficult to solve. The airlines are constantly searching for new ways to obtain "good" crew schedules, i.e., schedules that cover all the flights on the schedule, meet the FAA rules, meet union requirements, and are of relatively low cost. Because civilian airline crew costs often exceed \$1.3 billion

every year, even very small incremental savings can save the airlines a significant amount of money each year (Hoffman and Padberg, 1993:658). The success of tabu search on similar combinatorial problems motivates its use in this research (Barnes, *et al.*, 1995; Dowsland, 1998; Lourenco, *et al.*, 1998; Shen and Kwan, 2000).

1.3 Problem Statement

A major problem facing AMC is how to efficiently schedule its tanker crews. They have a severe shortage of tanker crews with no apparent relief projected in terms of either more crews or reduced mission requirements. Today, AMC analysts use a simulation program, “Crew Dog,” to determine the number of crews needed to fly a given aerial refueling schedule (Ryer, 2000). Crew Dog embodies a simple greedy heuristic. Greedy heuristics tend to converge to local optimal solutions, thus ignoring large portions of the solution space. This is true of the heuristic described in Section 4.2.2, which provides a starting solution for the tabu search approach developed in this work. Although the greedy heuristic provides very good initial solutions, the results from Chapter VI show that the solutions can clearly be improved.

The thrust of this research is to develop an efficient tabu search approach to AMC’s TCSP. Tabu search allows the search to overcome the trap of local optimality and provide more efficient crew schedules. For the two adaptive tabu search algorithms developed, group theory provides the mechanisms to efficiently direct the metaheuristic search process.

The robustness of the developed tabu search algorithms is judged by extensively testing them using designed experiments and benchmark test problems. Since no

benchmark problem sets for the TCSP exist, construction of these experiments required the development of a Java™ based flight schedule generator. Finally, an integer program (IP) to calculate lower bounds for the TCSP objectives is developed in order to measure the overall quality of the metaheuristics.

1.4 Organization of Dissertation

The remainder of this dissertation is organized as follows. Chapter II provides an introduction to tabu search and group theory, laying the foundation for Chapters III and IV. Chapter III provides a review of both the USAF's concern with crew scheduling and the airline CSP, to include previously developed solution methodologies.

Chapter IV discusses the adaptive tabu search methodology developed to solve the TCSP, including a hybrid methodology that uses set partitioning optimization as a vocabulary building mechanism within the metaheuristic. Chapter V details the general flight schedule generator developed during this research. Chapter VI provides a designed, statistical analysis of the tabu search approaches--to include the development of new IP-based lower bounds. Finally, Chapter VII concludes by discussing the contributions of the research and avenues for future research.

II Introduction to Tabu Search and Group Theory

This chapter explains the basics of tabu search and group theory. It provides the minimum background necessary to understand the adaptive tabu search methodology developed in Chapter IV.

2.1 Tabu Search

Tabu search is a metaheuristic, a master strategy that forces a local heuristic search procedure to explore the solution space beyond local optimal (Glover and Laguna, 1997:2). The fundamental philosophies of tabu search are the following:

- 1) Adaptive memory should be used to create a robust search methodology, unlike simulated annealing and genetic algorithms that use randomness to guide the search process.
- 2) The solution space should be explored intelligently, i.e., the search must respond appropriately to what is occurring or has occurred during the search process.

Section 2.1.1 describes the basic components present in any tabu search metaheuristic.

This basic tabu search mechanism is often so effective that it suffices for the problem under investigation. Unfortunately, the basic tabu search approach fails for some problems and the implementation of more advanced, readily available concepts is required. Section 2.1.2 discusses the advanced tabu search concepts exploited by this research.

2.1.1 The Basic Tabu Search.

Solution Structure.

The foundation of any optimization routine is the problem's solution structure. This structure mathematically describes the various decision variables inherent in the optimization model and precisely defines the elements of the solution space. Section 2.2.1 describes the solution structure the symmetric group on n letters provides for this research. Once a solution structure is chosen, the basic tabu search begins by creating an initial solution. Section 4.2.2 describes the constructive heuristic used to create initial solutions in this research.

The Neighborhood of Solution x .

Once the initial solution, x , is created, the metaheuristic needs a way to travel to other solutions within the solution space. This is done by creating and examining a neighborhood of the initial solution, x , and all subsequent solutions.

Reeves (1995:5) states, "A neighborhood $N(x, \sigma)$ of a solution x is a set of solutions that can be reached from x by a simple operation σ ." The operation σ is generally called a "move" in tabu search applications. Implicit in the definition of $N(x, \sigma)$ is M , the set of all moves of type σ that map x to $N(x, \sigma)$.

A simple example clarifies this neighborhood definition. Suppose for a 3-crew/3-flight problem the initial solution, x , has crew 1 assigned flight 1, crew 2 assigned flight 2, and crew 3 assigned flight 3. A swap move could be used to search beyond this incumbent solution. Define the swap move, σ , as exchanging flight i with flight j . M is

therefore all exchanges of flight i with flight j , for $i = 1, 2$ and $i < j \leq 3$. Therefore, $N(x, \sigma)$ is as follows:

- 1) Reassign flight 2 to crew 1 and flight 1 to crew 2. Crew 3 assigned flight 3.
- 2) Reassign flight 3 to crew 1 and flight 1 to crew 3. Crew 2 assigned flight 2.
- 3) Reassign flight 3 to crew 2 and flight 2 to crew 3. Crew 1 assigned flight 1.

Choosing the Next Incumbent Solution from $N(x, \sigma)$.

Once $N(x, \sigma)$ has been constructed, solutions in $N(x, \sigma)$ must be evaluated and one member chosen as the next incumbent solution. The function used to evaluate solutions within $N(x, \sigma)$ generally considers the particular problem's objectives and constraints, as shown in Section 4.2.4. Given this method to evaluate solutions, different rules may be used to choose the next incumbent solution from $N(x, \sigma)$. For example, one tabu search implementation may choose the first improving solution in the neighborhood while another selects the "best" neighbor solution. The tabu search routines developed in this research strategically exploit both of these rules.

Tabu List.

In choosing the new incumbent solution from $N(x, \sigma)$, the tabu list must also be considered. A tabu list provides the short-term memory needed to escape from a local optimum and progress into other regions of the solution space.

Glover and Laguna (1997:31) state, "The most commonly used short-term memory keeps track of solution attributes that have changed during the recent past." Suppose the first neighborhood move from the swap neighborhood previously described satisfies the "best" criteria and is selected as the new incumbent solution. One attribute of the

solution is the assignment changes of crews 1 and 2. A tabu list based on this attribute may make swaps involving crews 1 and 2 tabu for a period of time, called the tabu tenure. Another attribute of the solution is the reassignment of flights 1 and 2. One tabu list using this attribute may make any swaps involving flights 1 and 2 tabu for a period of time. This is a restrictive implementation when compared to another tabu list implementation that may only make the specific swapping of flights 1 and 2 tabu for a period of time. The tabu list to implement is generally problem specific and an area of research when developing a complete tabu search methodology.

Aspiration criteria provide a flexible tool to overcome the restrictive implementations described above, and may be important to avoid not visiting good solutions. The analyst defines the aspiration criteria conditions that must be satisfied before the tabu search accepts a currently forbidden move. A commonly used aspiration is to allow a forbidden move if the resulting solution quality is superior to the best found so far. Glover and Laguna note that aspiration criteria are very important in allowing tabu search to achieve its expected superior performance (1997:50).

Many different ways exist to represent recent solutions or moves on a tabu list and how you define the list can significantly affect the search. A solution tabu list may be used as an alternative to the attribute-based lists discussed above. In this case, an entire solution is placed on the tabu list. Since storing and comparing whole solutions can take an enormous amount of memory and time, hash values are generally used as solution surrogates (Glover and Laguna, 1997:246-248). Chapter IV describes the solution tabu list used within the adaptive tabu search (ATS) developed in this dissertation.

An Iteration of the Basic Tabu Search.

This section concludes by demonstrating an iteration of the basic tabu search, as implemented in OpenTS, the JavaTM-based software used in this research. Figure 1 below displays an iteration of the OpenTS tabu search framework (Harder: 2002).

OpenTS starts from an initial solution defined by the user. Instead of explicitly building the solutions defined by $N(x, \sigma)$, OpenTS builds the neighborhood of moves, M . This neighborhood of moves has a one-to-one correspondence to $N(x, \sigma)$, and is generally quicker and more memory-efficient to build.

Once the moves are created, OpenTS forwards M to the objective function evaluator. The objective function evaluator takes each move of M and examines $N(x, \sigma)$, one element at a time, using user-defined evaluation methods. Clearly, if the next incumbent solution is chosen as the first improving solution in $N(x, \sigma)$, it is unlikely the entire neighborhood will be evaluated and the time to evaluate $N(x, \sigma)$ should decrease. Further time efficiencies occur when elements of $N(x, \sigma)$ can be evaluated incrementally, i.e., without completely building the neighbor solutions. Section 4.2.4 describes the incremental evaluations used in this research.

Finally, the move chosen from $N(x, \sigma)$ is used to operate on the current solution, create the new incumbent solution, and complete an iteration of the basic tabu search.

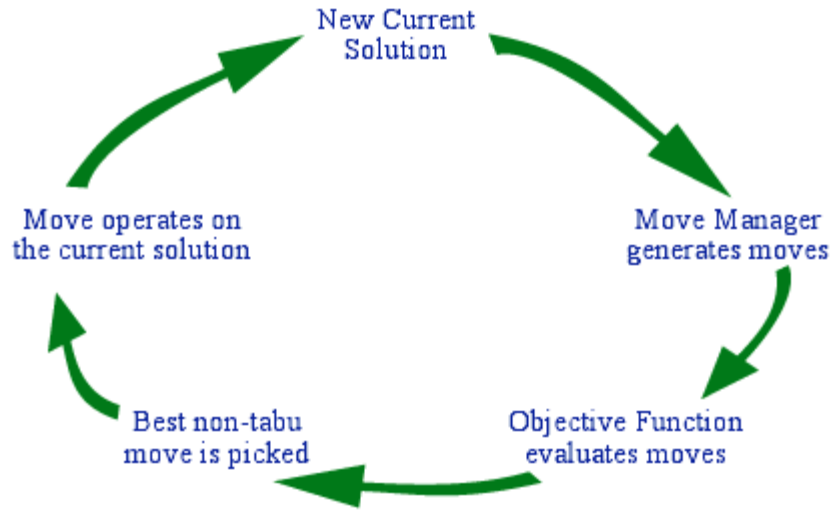


Figure 1: One Iteration of OpenTS (Harder, 2002)

2.1.2 Advanced Concepts.

The basic approach described above does not always produce the best solutions. The simple search often fails because of the combinatorial explosion in the number of variables and constraints present in many of the problems approached by tabu search. Such an explosion overwhelms simpler methods and does not allow the effective search of the problem's solution space.

For example, it would be impractical to examine the entire solution space of a scenario with 50 flights to schedule. The solution space consists of $50! = 3.04 \times 10^{64}$ solutions and a computer evaluating 1 trillion solutions per second would take 10^{44} years to examine all of them. Therefore, during the tabu search process, only the applicable portion of the entire solution space need be examined explicitly.

This does not imply defeat in the face of the basic tabu search's failure. It simply means other strategies must be invoked. Glover and Laguna (1997) emphasized the need

to understand advanced strategies early in their book. They stated that, “Incorporating only a couple of TS-related concepts into a search procedure may result in an inferior method and a frustrating experience...Our goal, however, is to present most of the strategic issues as early as possible in order to encourage future TS researchers and practitioners to incorporate these concepts into their application” (Glover and Laguna, 1997:9). This section of the paper describes some of the advanced tabu search concepts that have proved very useful in combinatorial applications.

Intensification and Diversification.

Glover and Laguna define intensification as, “Strategies based on modifying choice rules to encourage move combinations and solution features historically found good. They may also initiate a return to attractive regions to search them more thoroughly” (Glover and Laguna, 1997:96).

Intensification may be implemented by modifying appropriate choice rules found within the tabu search. For example, while conducting recency-based moves, the search may identify move combinations or solution attributes that produce good solutions. Once identified, the search could encourage the use of these moves or attributes to build ensuing neighborhoods.

Another strategy for intensification is an ability to return to promising regions found in the previous portion of the search in an attempt to find better solutions. Glover and Laguna state that, “Since elite solutions must be recorded in order to examine their immediate neighborhoods, explicit memory is closely related to the implementation of intensification strategies” (Glover and Laguna, 1997:8). In other words, if you expect to return to promising regions, you must explicitly record the solutions you may want to

revisit. In addition, this explicit bookkeeping must be done in a manner that does not hinder the computational performance of the search process.

As opposed to intensification's concentration on certain moves or promising regions, diversification encourages the search process to examine unvisited regions of the solution space to investigate solutions that differ significantly from those found previously.

The philosophy of diversification within tabu search is analogous to the diversification recommended for personal investments. Financial counselors routinely tell investors to diversify their financial portfolio by placing their money in multiple market sectors or financial instruments. Diversification protects the investor by ensuring one poorly performing sector does not destroy their financial interests.

Diversification within tabu search works much the same way, but the investment made by a tabu search algorithm is the computational effort needed to solve the problem. When a tabu search is diversified, it visits many sectors of the solution space. These sectors, defined in Section 2.2.1 as conjugacy classes, contain many individual solutions. While the investor lowers his financial risk by diversifying into multiple market sectors, the tabu search lowers its risk of not identifying very good individual solutions by visiting many of the solution space sectors.

One way to ensure diversification within the tabu search is to use long-term memory structures that track solutions or solution attributes that have occurred earlier in the search. Frequency data is a popular way to represent such long-term memory. For instance, throughout the search process the tabu search may record how many times certain sectors are visited. It may then force the search trajectory to move to sectors previously unvisited.

This research uses a balanced approach to intensification and diversification. It uses two tabu list schemes, described in Section 4.2.5, and an adaptive solution and move evaluator, described in Section 4.2.4, to promote diversification. By using these two components, the search avoids using long-term frequency information to explicitly force the trajectory to particular portions of the solution space. It implements an intensification scheme, described in Section 4.4.2, that returns to elite solutions to further search their neighborhoods for improvements. Diversification is not ignored while completing this intensification. The tabu search continues to allow movement to any solution space sector. Figure 2 below displays a typical result of the intensification and diversification approach used in this research. The number of sectors visited grows linearly as the search progresses for this problem, showing the synergy of the implemented intensification and diversification approach.

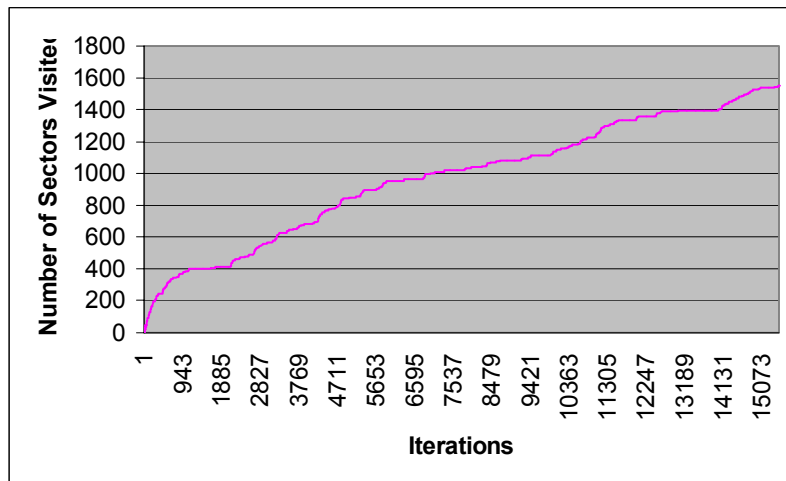


Figure 2: A Balanced Intensification & Diversification Approach

Candidate List Strategies.

As the size of the CSP grows, it is clear that neighborhoods built with moves such as the two-letter swap become astronomically large. Obviously, for such a problem, the tabu search cannot examine every possible swap within the neighborhood. Instead, candidate list strategies must be used to restrict neighborhoods to manageable sizes.

Candidate list strategies may be created using rules related to a particular problem, i.e., rules developed from the structure of the crew scheduling problem, or to general list strategies that have proved useful in past applications. Some of these general classes of candidate list strategies are Aspiration Plus, Elite Candidate List, Successive Filter Strategy, Sequential Fan Candidate List, and the Bounded Change Candidate List (Glover and Laguna, 1997:61-67). For example, the Aspiration Plus strategy works as follows:

- a) Define how the quality of a particular move is determined and establish a threshold for the move.
- b) Examine moves until the threshold has been reached, then examine a preset additional number of moves.
- c) Define a minimum and a maximum number of moves to perform to ensure neither too few nor too many moves are considered. (Glover and Laguna, 1997:61)

The time-sequenced nature of the TCSP allows the tabu search developed in this research to restrict its neighborhoods using the structure of the TCSP itself. Section 4.2.3 details this candidate list strategy.

Strategic Oscillation.

Glover and Laguna state that, “Strategic Oscillation operates by orienting moves in relation to a critical level, as identified by a stage of construction or a chosen interval of functional values” (1997:102). The critical level examined in many cases is infeasibility.

There may be times during the search process when strategically moving through an infeasible region allows the search to explore solutions with different attributes and potentially better objective function values than those found previously.

This research uses adaptive penalty weights to force the search to oscillate between areas of feasibility and infeasibility. The use of these adaptive weights is described in Section 4.2.4. Figure 3 below shows an example of the oscillation that occurred in the initial search trajectory of a tabu search applied to a small TCSP. The search starts from an initial feasible solution, shown by the solid black boxes in the figure. At iteration 16, it moves to the infeasible portion of the solution space, displayed as hollow circles on the figure, seeking to improve total waiting time. The search trajectory returns to feasibility at iteration 360, completing the oscillation.

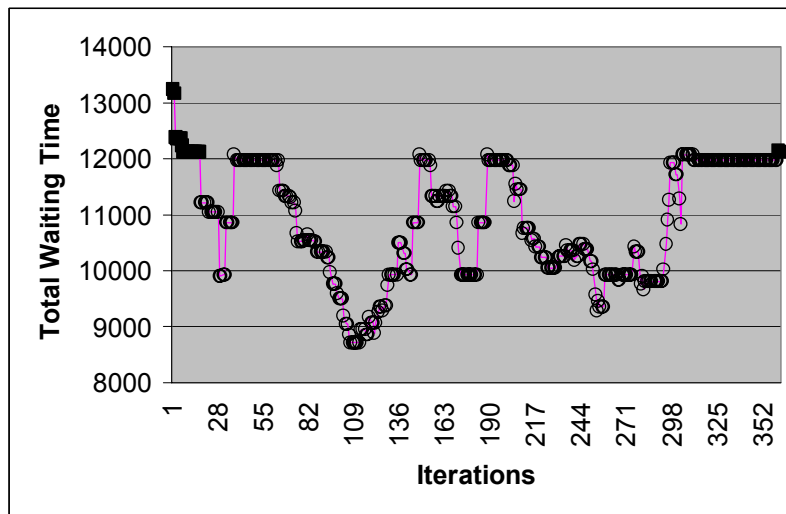


Figure 3: Strategic Oscillation

The oscillation among alternative choice rules and neighborhoods is another form of strategic oscillation. Decision rules are used to decide which type of move to select from amongst a pool of possible moves, i.e., a pool consisting of the swap move and the insertion move. At any time during the search, the move defining the incumbent solution's neighborhood may be changed from the swap to the insertion move.

Vocabulary Building.

Vocabulary building is an integral part of this dissertation research and the last advanced concept discussed in this section. Glover and Laguna (1997:252) define vocabulary building as, "Identifying meaningful fragments of solutions, rather than focusing solely on full vectors, as a basis for generating combinations." They further state, "In some settings these fragments can be integrated into full solutions by means of optimizations models."

Rochat and Taillard (1995) and Kelly and Xu (1998) successfully implemented an optimization-based type of vocabulary building as they implemented different heuristic approaches to the vehicle routing problem (VRP). Rochat and Taillard found augmenting their initial heuristic approach with a post-optimization set partitioning problem (SPP) solved with CPLEX MIP (ILOG, 2002) allowed them to match the best known results of many benchmark VRPs.

Kelly and Xu (1998) experienced this type of improvement as well, but they found the CPLEX MIP ran out of memory and failed to find solutions for many of their larger problems. They developed a two-phased approach to the VRP to overcome this limitation. In phase one, they used various heuristics to develop the columns of a SPP. These heuristics typically found, at a minimum, a feasible solution to the problem. Phase

2 entailed using a tabu search routine they developed to solve the large partitioning problems created by phase 1.

Interestingly, both groups used their vocabulary building mechanism as a post-optimization scheme rather than embedding it into their heuristic search. Kelly and Xu (1998) suggest that finding a mechanism to integrate the column generation and SPP solution phases is “an interesting avenue of research.” This research extends previous vocabulary building efforts. Section 4.3 details the methodology used to integrate SPP-based optimization within the adaptive tabu search (ATS) routine.

There are many other advanced concepts that could be covered, but the reader is referred to Glover and Laguna (1997). Now that the basics of the tabu search metaheuristic have been outlined, the next section discusses another important area of this research, group theory.

2.2 Group Theory

The following section discusses the basics of group theory, the foundation for the adaptive tabu search. Group theory provides the solution structure for the ATS, provides two operators, function composition and conjugation, for neighborhood building, and provides mechanisms to measure tabu search concepts such as diversification.

2.2.1 The Basics.

A group is a set G and a binary operation \oplus on G such that the following axioms are satisfied:

- a) (Associativity) For any elements a, b, c of G ,

$$a \oplus (b \oplus c) = (a \oplus b) \oplus c.$$

b) (Identity) There is a unique element i in G such that, for every element a of G ,

$$a \oplus i = i \oplus a = a.$$

c) (Inverses) For any element a of G , there exists a unique element a^{-1} of G such that

$$a \oplus a^{-1} = a^{-1} \oplus a = i. \text{ (Grossman and Magnus, 1975:13)}$$

This research focuses on the use of the symmetric group on n letters, S_n . Assuming that G consists of n objects labeled $1, 2, 3, \dots, n$, S_n is the group of all permutations of n objects and has the order $n!$ (Fassler and Stiefel, 1992:8). An element, m , of S_n can be represented in two forms, long and cyclic. Without loss of generality, assume that m represents a one-to-one mapping of the letters $\{1,2,3\}$ onto itself such that $1 \rightarrow 2$, $2 \rightarrow 3$, and $3 \rightarrow 1$. The left side of the mapping, x , represents its domain while the right side represents its image, $m(x)$. This mapping can be thought of as rearranging the sequence $(1, 2, 3)$ to form the sequence $(2, 3, 1)$ by replacing x with $m(x)$ (Grossman and Magnus, 1975:107). In long form, create a $2 \times N$ array with the domain placed on the top row and the image placed on the bottom row. The result is $m = \begin{pmatrix} x \\ m(x) \end{pmatrix} = \begin{pmatrix} 123 \\ 231 \end{pmatrix}$.

The cyclic form of m is written as a single-rowed array. One letter in m 's domain is chosen as the starting letter. Each letter's image is then written in the cell to its immediate right in the array, until all letters have been exhausted. For example, starting with the letter 1, the cyclic form of m is $(1,2,3)$. Note that the cyclic form of the mapping is not unique because m could have been written as $(2,3,1)$. Both of these cyclic forms represent the same element of S_3 . Therefore, to provide a consistent identification of unique elements of S_n , the convention throughout this research is to start a cycle with the smallest letter it contains, i.e. always write m as $(1,2,3)$.

Each element of S_n can be written as the product of disjoint cycles containing distinct letters. For example, a mapping such as $1 \rightarrow 4, 2 \rightarrow 2, 3 \rightarrow 5, 4 \rightarrow 6, 5 \rightarrow 3, 6 \rightarrow 1, 7 \rightarrow 8,$ and $8 \rightarrow 7$ can be written as the product of the disjoint cycles $(1,4,6), (2), (3,5),$ and $(7,8),$ resulting in the permutation $(1,4,6)(2)(3,5)(7,8)$ (Fassler and Stiefel, 1992:137). The importance of this property is reiterated in the solution structure discussion in Section 4.2.1.

The focus of this discussion changes from the elements of S_n to the binary operation that defines it, function composition (Colletti, 1999:11). Function composition, $\oplus,$ is defined as $(\alpha \oplus \beta)(x) = \beta(\alpha(x)),$ where $\alpha, \beta \in S_n, x \in 1,2,\dots,n, \alpha(x)$ is the image of x in $\alpha,$ and $\beta(y)$ is the image of y in $\beta.$ As an example, let $\alpha = (1\ 2\ 3)$ and $\beta = (1\ 3\ 2).$ Calculate $(\alpha \oplus \beta)(1)$ as $\beta(\alpha(1)) = \beta(2) = 1.$ Doing this for the other letters, the resulting composition is $\alpha \oplus \beta = (1)(2)(3),$ the identity element of $S_3.$ This research uses function composition to create template-based insert moves within the tabu search framework.

For $S_5,$ notice that seven ways exist to express permutations in terms of cyclic form: $(xxxxx), (xxxx)(x), (xxx)(xx), (xxx)(x)(x), (xx)(xx)(x), (xx)(x)(x)(x),$ and $(x)(x)(x)(x)(x).$ Representatives of each are: $(12345), (1234)(5), (123)(45), (123)(4)(5), (12)(34)(5), (12)(3)(4)(5),$ and $(1)(2)(3)(4)(5),$ respectively. Notice that the number of letters and their order does not change in each case, but, because the cyclic structures are different, there are seven distinct permutations within $S_5.$ Sets of permutations of similar cyclic structure are called conjugacy classes. Conjugation, the other symmetric group operation used in this research, must be defined.

For $g, h \in$ group G , g and h are conjugates in G iff $\exists x \in G$ such that $x^{-1}gx = g^x = h$ (Scott, 1964:52). The following useful theorem provides a convenient way to perform conjugation:

Theorem: For $g, x \in S(n)$, build g^x by replacing each letter in g with its image in x . Cycle structure of g is preserved (Colletti, 1999:26).

A conjugacy class of $g \in$ group G can now be defined as $CClass(G, g) = \{g^x : x \in G\}$.

Since the conjugation operator preserves cycle structure, it is clear that conjugacy classes contain sets of permutations with like cycle structure.

With the basics of group theory established, the next two sections discuss classes of moves built using group theory. Chapter IV details the specific moves developed within each class for this research.

2.2.2 Template-based Moves.

A template is a permutation that either fragments a given permutation or joins smaller disjoint cycles into a single cycle (Colletti, 1999:61). Splitting templates are permutations (a_1, b_1, c_1, d_1) that split larger cycles into subcycles in the manner:

$$(a_1, \dots, a_m, b_1, \dots, b_n, c_1, \dots, c_k, d_1, \dots, d_p) \oplus (a_1, b_1, c_1, d_1)^{-1} = (a_1, \dots, a_m)(b_1, \dots, b_n)(c_1, \dots, c_k)(d_1, \dots, d_p).$$

Welding templates do just the opposite. They take smaller cycles and gather them into one larger cycle in the manner:

$$(a_1, \dots, a_m)(b_1, \dots, b_n)(c_1, \dots, c_k)(d_1, \dots, d_p) \oplus (a_1, b_1, c_1, d_1) = (a_1, \dots, a_m, b_1, \dots, b_n, c_1, \dots, c_k, d_1, \dots, d_p)$$

The following four examples show the use of each type of template.

Example 1: Welding Template

$$(1)(2)(3)(4)(5) \oplus (1,2) = (1,2)(3)(4)(5) = (1,2)$$

Example 2: Welding Template

$$(1,2)(3,4) \oplus (1,3) = (1,2,3,4)$$

Example 3: Splitting Template

$$(1,2,3,4,5) \oplus (1,4)^{-1} = (1,2,3,4,5) \oplus (4,1) = (1,2,3)(4,5)$$

Example 4: Splitting Template

$$(1,2,3,4,5) \oplus (1,3,5)^{-1} = (1,2,3,4,5) \oplus (1,5,3) = (1,2)(3,4)(5) = (1,2)(3,4)$$

Clearly, splitting and welding templates can be used to traverse the various conjugacy classes of the CSP. However, it is their use in more powerful moves that makes them extremely useful. Colletti discusses the use of templates in moves such as (p,τ) and (P,T) neighborhoods, inserts, and the general cross exchange (1999:135-177).

2.2.3 Conjugation-based Moves.

Once the search process moves from one conjugacy class to another, it may be useful to focus the search in a quest for good solutions within the new conjugacy class.

Conjugation is an ideal tool for conducting such intensification because it ensures the preservation of the incumbent solution's cycle structure.

Colletti discusses using conjugation in path relinking, k -letter swaps, and the Dokov Method (1999:135-177). The next two examples show the use of conjugation in the powerful 2-letter swap neighborhood. Clearly, conjugation takes the search to different permutations within the solution space while staying in the incumbent conjugacy class.

Example 1: Swap 2 and 4

$$(1,2,3)(4,5) \wedge (2,4) = (1,4,3)(2,5)$$

Example 2: Swap 2,3 and 4,5

$$(1,2,3)(4,5) \wedge (2,4)(3,5) = (1,4,5)(2,3)$$

This chapter provided an overview of tabu search and group theory; the foundations for the adaptive tabu search developed in this research. The next chapter provides a discussion of USAF tanker fleet concerns, a review of the air crew scheduling literature, and a discussion of the analysis of metaheuristics.

III Literature Review

The first section of the chapter reviews the Air Force's concerns with tanker crew scheduling. The next section discusses various heuristic and optimization algorithms previously developed to solve crew scheduling problems, highlighting their links to group theory where appropriate. The final section reviews the use of designed experiments in validating heuristic algorithms.

3.1 U.S. Air Force Concerns

Air Force Doctrine Document 2-6.2 (AFDD 2-6.2) (1999) discusses the history of air refueling, why air refueling is important to today's operations, and how it should be employed in today's Air Force. It states that, "Even though the preponderance of the world's tanker aircraft are in the U.S. Air Force, the high demand placed on these assets makes proper employment critical" (AFDD 2-6.2, 1999:9). A significant portion of this proper employment is efficient use of tanker aircrews. The force management portion of the doctrine document specifically addresses the crew scheduling problem (AFDD 2-6.2, 1999:62). Because tanker units have a low aircrew-to-aircraft ratio (crew ratio), it is aircrew availability rather than aircraft availability that most often limits mission scheduling.

AFDD 2-6.2 states that tanker units are currently manned at 1.17-1.36 crews per aircraft. Depending on the nature of the operation, crews may deploy with a crew ratio of 1.00-1.50 (1999:62). With this low crew ratio, high operating tempos force many aircrew members to face monthly flying hour maximums. In fact, the low crew ratio creates a

situation where aircrew availability cannot keep pace with the operations tempo of the aircraft that they fly. For example, examine the intertheater refueling needed in the deployment phase of a conflict. An aircraft flown continuously on intertheater missions averaging 12 hours per sortie can fly 9.9 missions in a week, while at a crew ratio of 1.27, the aircrew assigned to the tanker can only fly 7.6 missions in a week. Aircrew capabilities become equal to aircraft capabilities at a crew ratio of 1.65. Clearly with today's crew availabilities, aircrew capabilities will always be less than aircraft capabilities.

General Walter Kross highlighted this issue in a keynote address given to the Airlift Tanker Association Annual Convention, held in Anaheim, CA on October 25, 1997. He stated, "We have big readiness issues, but the biggest is that we need more aircrews. Programmers call it increasing the crew ratio. We never broke the tanker crew ratio out of the Cold War formula—we must if we are to survive" (Kross, 1997). The problem still exists. In personal e-mail correspondence with Major David Ryer, the analyst in charge of tanker affairs at Air Mobility Command's Studies & Analysis office, Ryer stated, "As a side note, when our team briefed General Ryan (Chief of Staff of the AF) two weeks ago, we faced a barrage of crew related questions" (2000). The question still remains, "How do we efficiently operate in our aircrew-constrained environment?" The crew ratio data and each general's view clearly provide the impetus for research into improving the efficiencies of tanker crew scheduling. If there are not enough aircrews to keep up with the aircraft themselves, then it is absolutely necessary to make sure the USAF uses its aircrews wisely.

3.2 Crew Scheduling

With the USAF concerns in mind, this section transitions to a discussion of the CSP itself. It discusses the CSP from a historical perspective, concluding with a review of previous solution methodologies.

3.2.1 The Airline Crew Scheduling Problem.

Gershkoff describes the airline CSP as follows (1989:32):

- 1) The objective is to minimize the cost of flying the published schedule, subject to constraints 2-5 below.
- 2) Each flight must be covered once and only once.
- 3) Each pairing (pairings are sequences of flights a crew flies) must begin at a crew base, fly around the system, and return to the same base.
- 4) Each pairing must conform to the limitations of FAA regulations and published work rules in force at the airline.
- 5) The total number of hours flown by crews at each crew home base must be within specific minimum-maximum limits, in accordance with the airline's manpower plan.

Gershkoff details the components of crew scheduling cost for American Airlines. The U.S. Air Force incurs many of the same costs, such as the hotel and per-diem expenses resulting from scheduling layovers away from each crew's home base. Gershkoff also coins a term called pay and credit, which represents unproductive crew time that must be minimized, i.e., paying crews while they are on the ground (1989:32). Given the poor crew ratios the U.S. Air Force has, unproductive crew time is an item Air Force operational units must minimize as well.

The formulation of the mathematical model of the CSP is based on the airline's published flight schedule, which is equivalent to the USAF ATO. The published

schedule includes departure/arrival locations and times for each flight segment during a month. Flight segments are nonstop flights between pairs of cities. For tanker refueling, these flight segments consist of nonstop flights between pairs of operational bases.

Refueling waypoints exist between tanker departures and arrivals, but these mid-flight stops simply add to the length of the flight segment and do not require explicit modeling.

Constraint 2) from the airline CSP described above clearly leads to formulation of the classic set partitioning problem (SPP). In a set partitioning problem, each member of a given set, **S1**, must be assigned to or partitioned by a member of a second set, **S2**. For the air crew scheduling problem, each member of the set of flights must be assigned to a member of the set of crew rotations.

For this research, S_n provides a natural partitioning of the flights in the TCSP. Each flight is placed in one of the disjoint cycles representing a crew rotation. These disjoint cycles have a one-to-one correspondence with the columns of the set partitioning problem's constraint matrix, as seen in Figure 4 below. The disjoint cycles also represent a partial solution to the TCSP, i.e., cycle (0,4,6,9) below is one crew rotation within the solution set of crew rotations. Throughout the tabu search process, these types of partial solutions can be recorded in a pool of columns for a SPP optimizer. Section 4.3 describes how this research uses partial solutions and the SPP to improve the search process through vocabulary building.

(0,4,6,9)(1,5)(2,7)(3,8,10)

Crew 0	1	0	0	0
Crew 1	0	1	0	0
Crew 2	0	0	1	0
Crew 3	0	0	0	1
Flight 4	1	0	0	0
Flight 5	0	1	0	0
Flight 6	1	0	0	0
Flight 7	0	0	1	0
Flight 8	0	0	0	1
Flight 9	1	0	0	0
Flight 10	0	0	0	1

Figure 4: Mapping a Symmetric Group Element to the SPP

Once a set of columns or crew rotations is generated, the mathematical program for the SPP is as follows (Hoffman and Padberg, 1993:658):

Equation 1: Set Partitioning Problem (SPP) Formulation

$$\min \sum_{j=1}^n c_j x_j$$

subject to : $Ax = e_m$,

$$x_j \in \{0,1\} \text{ for } j=1, \dots, n,$$

where e_m is a vector of m ones, and n is the number of rotations that we consider. Each row of the $m \times n$ A matrix represents a flight segment, while each column represents a flight rotation with cost c_j for using it. The x_j are zero - one variables associated with each rotation, i.e. $x_j = 1$ if rotation j is flown. The A matrix is generated one column at a time, with $a_{ij} = 1$ if flight leg i is covered by rotation j , 0 otherwise.

Although the set partitioning formulation is most often used for the airline CSP, researchers have developed a few other formulations as well. Many airlines relax constraint 2) above and allow deadheading, typically for intercontinental flying

schedules. Deadheading occurs when crews are allowed to fly on a flight segment as passengers, repositioning them for better utilization later. Graves, *et al.* (1993) slightly change the formulation by modeling the problem as an elastic embedded SPP, allowing a flight segment to be uncovered but penalizing the solution if this constraint violation occurs. Finally, Desaulniers, *et al.* (1997) take an entirely different approach by modeling the CSP as an integer, nonlinear, multi-commodity network flow problem.

3.2.2 Solving the Airline CSP.

The SPP defined above is a NP-complete problem (Housos and Elmroth, 1997:70). For as few as 1,000 flight segments, billions of feasible rotations exist. Problems of this size are impossible to exhaustively enumerate and solve optimally, and have led researchers to propose a variety of solution algorithms. These algorithms can be grouped into three categories: heuristics, methods requiring a priori generation of the SPP columns, and column generation approaches.

Rubin (1973) developed the first heuristic approach to the airline crew scheduling problem. He decomposed the large problems into a series of subproblems, ultimately finding a local solution to the CSP. At each step, he recorded the last subproblem solved in a permanent “tabu” list to avoid resolving previously visited subproblems. American Airlines successfully implemented Rubin’s heuristic in their trip evaluation and improvement program (TRIP) and improvements to the methodology are discussed in later papers (Anbil, *et al.*, 1991, 1998; Gershkoff, 1989). The typical advances, driven by improvements in computer hardware technology, involve solving larger subproblems to find solutions closer to the globally optimal solution. Anbil, *et al.* implemented a

fundamental concept from tabu search as well. They attempted to avoid local optima by allowing the heuristic to initially make unimproving moves (Anbil, *et al.*, 1991:69).

Baker, *et al.* (1979, 1981), Ball and Roberts (1985), Wark, *et al.* (1997), and Levine (1996) develop heuristics distinct from Rubin. Ball and Roberts develop a graph-partitioning approach to the SPP, Wark, *et al.* create a repeated matching heuristic, and Baker, *et al.* start from an initial feasible solution and use 2-opt moves to quickly find local optimal solutions to the CSP. Chu and Chan (1998) found 2-opt moves to be extremely useful in railroad crew scheduling.

Levine's (1996) genetic algorithm (GA) appears to be the first metaheuristic applied to the airline CSP. Unfortunately, he also assumes the columns of the SPP are known prior to the use of his GA. Levine's GA seems to ignore the powerful potential of a metaheuristic: to input an existing flight schedule and develop good crew schedules without explicitly generating the columns of the SPP *a priori*. This research shows that a metaheuristic, when combined with a classical optimizer, provides an excellent column generation-type approach to SPP problems.

Although heuristics have proven successful in practice, they only guarantee convergence to locally optimal solutions. To overcome this limitation, researchers created optimization methods to solve the CSP.

The first group of optimization-based algorithms assumes the SPP columns exist *a priori* to the use of their algorithm (Chu, *et al.*, 1997; Graves, *et al.*, 1993; Hoffman and Padberg, 1993; Housus and Elmroth, 1997; Marsten, *et al.*, 1979, 1981). Marsten, *et al.* (1979, 1981) initiated the *a priori* movement by decomposing the large SPP into manageable SPPs solved using branch-and-bound. Later researchers took advantage of

the advances in computer hardware to implement algorithms that solve huge SPPs of up to approximately 1,000,000 columns (Chu, *et al.*, 1997; Graves, *et al.*, 1993; Hoffman and Padberg, 1993; Housus and Elmroth, 1997).

This *a priori* generation of the SPP columns dissatisfied researchers such as Crainic and Rousseau (1987). They felt the heuristics used to generate the set of columns still created a suboptimal situation. Their paper initiated a movement of optimization techniques toward column generation approaches (Yan and Chang, 2002; Anbil, *et al.*, 1998; Barnhart and Shenoi, 1998; Crainic and Rousseau, 1987; Desaulniers, *et al.*, 1997; Lavoie, *et al.*, 1988; Stojkovic, *et al.*, 1998). The goal of these methods is to generate the columns on the fly and eliminate the possibility of ignoring key columns in the optimal solution. Each of these methods differ in the reduced pricing schemes used to generate the columns to a linear relaxation of the SPP. They also implement a variety of branch-and-bound methodologies to form integer solutions from the relaxed solutions.

Lagerholm, *et al.* (1997, 2000) and Beasley and Cao (1998) developed vastly different approaches to the CSP. The former solve the problem using a Potts feedback neural network while the latter provide an algorithm that uses dynamic programming and tree search to solve a number of large problems to proven optimality.

3.2.3 Motivation for this Research.

While the methodologies of Section 3.2.2 solve airline crew scheduling problems well, they use two significant assumptions to reduce the computational complexity of the CSP. These assumptions are required in order to feasibly use classic optimization

techniques, do not apply to tanker crew scheduling, and provide significant motivation for the research found in this dissertation.

First, crew rotations are assumed to start and end at the same home base (Yan and Chang, 2002; Desaulnier, *et al.*, 1997; Anbil, *et al.*, 1992; Gershkoff, 1989; Baker and Fisher, 1981; Baker, *et al.*, 1979; Rubin, 1973). This is a natural assumption for civilian flight crews because returning the crews home reduces unnecessary costs such as overnight hotel stays. Returning home is generally not an option during military wartime operations. Therefore, tanker crews can be scheduled more flexibly by allowing them to end a rotation at a base different from where they started. Allowing rotations to start and end at different bases increases the number of rotations that must be considered; therefore, the computational complexity of the problem increases. The modern metaheuristic approach used in this research, tabu search, is an excellent tool for these types of combinatorial, computationally complex problems.

Second, optimization techniques assume that the flight schedule has a time horizon of length t . The flights for U.S. domestic schedules are assumed to repeat daily. Therefore, U.S. domestic optimization techniques typically solve problems with $t = 1$, named the *daily problem* (Anbil, *et al.*, 1998; Chu, *et al.*, 1997; Anbil, *et al.*, 1992; Gershkoff, 1989; Rubin, 1973). European and U.S. international schedules are more irregular than the U.S. domestic schedules, i.e., their schedules repeat weekly but not daily. Optimization techniques for these problems seek to exploit this weekly time horizon (Barnhart and Shenoi, 1998; Housos and Elmroth, 1997; Desaulnier, *et al.*, 1997; Wark, *et al.*, 1997; Lavoie, *et al.*, 1988). This time horizon assumption is critical to optimization techniques because it reduces the number of rows in their problem formulations, i.e., if flight f

repeats daily and $t = 1$, then it only needs to be covered once in the SPP. Operational military schedules are, by design, irregular. This irregularity represents the element of surprise and reduces operational risk. Tanker schedules will likely not repeat daily, weekly, or monthly, therefore a flexible optimization tool is needed! The tabu search methodology developed in this research is a time-horizon free approach to tanker crew scheduling.

This section concludes with one significant observation. No tabu search approach to the airline CSP exists in the literature! This is a noticeable absence given its success on other combinatorial optimization problems, such as the crew scheduling problems discussed in Section 3.2.4.

3.2.4 Solving Other CSPs.

Although tabu search has not been used to solve the airline CSP, it has been used to schedule other types of crews (Dowland, 1998; Lourenco, *et al.*, 1998; Shen and Kwan, 2000).

Lourenco, *et al.* (1998) and Shen and Kwan (2000) describe tabu search approaches to the bus driver CSP. Lourenco, *et al.* assume that the bus driver CSP is small enough to generate all feasible columns of the SPP *a priori* and their tabu search assumes such an approach while Shen and Kwan develop a methodology starting from an initial feasible solution, similar to Baker, *et al.* (1979, 1981).

Lourenco, *et al.* (1998) describe a solution structure with one set holding the columns that cover the bus routes and the other set holding the columns not in the solution, i.e., the

typical basic and nonbasic variables from linear programming. They use the following three moves, in sequential order, to build their neighborhood structure:

- 1) An insert move that takes one column from the nonbasic set and places it in the solution.
- 2) An exchange move that takes one column from the basic set and one column from the nonbasic set and exchanges them.
- 3) A remove move that takes one column from the basic (solution) set and places it in the nonbasic set.

Using the symmetric group easily describes their neighborhood structure and moves.

Suppose 10 columns in the SPP are partitioned into two disjoint cycles, for example $(1,2,3)(4,5,6,7,8,9,10)$, where the first disjoint cycle represents the basic variables and the second disjoint cycle represents the nonbasic variables. This solution indicates that columns 1-3 cover the bus routes. In addition, notice that move 2) above is the two-letter swap and moves 1) and 3) are the single-letter insert. Similarly, Shen and Kwan claim they use four distinct neighborhood structures to diversify their search (2000:4). When group theory is used to examine their solution structure and moves, these four neighborhoods reduce to the two-letter swap and single-letter insert neighborhoods as well. In essence, symmetric group theory has reduced the “conceptual” complexity of the neighborhood structure. This reduction in conceptual complexity should lead to streamlined coding of metaheuristic algorithms by reducing the number of neighborhoods to be coded.

3.3 Designed Experiments

Experiments are often conducted to examine how an algorithm performs against other algorithms within a certain problem class and how it performs on a variety of instances

within a particular problem class, such as the TCSP (Lin and Rardin, 1980:12).

Historically, factorial designs (Myers and Montgomery, 1995) have been proposed for this purpose (Greenberg, 1990; Hooker, 1994, 1995; Lin and Rardin, 1980).

The most commonly used factorial designs are the 2^k full factorial designs, named such because each factor of interest is held to two levels and each replicate of such a design has exactly 2^k experimental runs (Myers and Montgomery, 1995:79). When such designs create enormously costly experiments, then fractional factorial designs are used to reduce the number of runs required (Myers and Montgomery, 1995:134).

Greenberg (1990:94) states that computational tests of algorithms should demonstrate the correctness of a model or algorithm, the quality of its solution, the speed of its computation, and its robustness. Barr, *et al.* add experimental goals such as demonstrating the algorithm is high-impact, generalizable, and innovative. In addition, they appreciate experimentation that reveals insight into the heuristic or problem structure and provides theoretical contributions such as solution quality bounds (Barr, *et al.*, 1995:12).

Hooker (1994, 1995) calls for an empirical science of algorithms beyond the construction of benchmark problem sets. In this empirical science, the robustness of an algorithm is not demonstrated during the research phase by showing its ability to solve a few benchmark problems. Instead, the researcher determines how the algorithm's performance depends on the characteristics of the problem under investigation (Hooker, 1994:202).

Many algorithms contain parameters whose values must be carefully chosen to ensure their effectiveness. Hooker considers the tuning of algorithms moot because the

parameters should be part of the experimentation. He suggests running controlled experiments over a variety of parameter settings and examining the effect of these parameter settings on the algorithm's performance (Hooker, 1995:40). The implication is that once the parameters' effect on algorithm performance is known, the choice of levels is clear.

Adenso-Diaz and Laguna extend the Hooker approach with their automated fine-tuning algorithm (1998). The procedure, called CALIBRA, uses a Taguchi fractional factorial design and local search procedure to search for the best parameter settings for any algorithm. This extends Hooker's approach because CALIBRA must determine the affect of parameter settings on the algorithm's performance in order to choose the best set of parameter values. Adenso-Diaz and Laguna show CALIBRA's effectiveness over a variety of problem classes and algorithms, to include the tabu search metaheuristics (1998).

This research follows Hooker's recommendations (1994, 1995). Chapter VI uses a fractional factorial experiment to examine how the characteristics of the TCSP and the ATS affect performance measures such as the number of crews in a solution or the total waiting time of those crews. This type of analysis has not previously been done on an air crew scheduling problem. As suggested, the results from the designed experiment provide insight into the appropriate levels for important tabu search parameters. Chapter 6 also provides a methodology to calculate lower bounds for the TCSP, as suggested by Barr, *et al.* (1995). These lower bounds are used to judge the quality of the solutions found by the ATS.

This chapter discussed the USAF's tanker fleet concerns, reviewed the air crew scheduling literature, and reviewed the literature on analysis of algorithms. The next chapter details the adaptive tabu search developed in this research.

IV An Adaptive Tabu Search (ATS) Approach

This chapter outlines the methodology developed to solve the TCSP. The TCSP is discussed first, highlighting its differences from the airline CSP. Section 4.2 details the various components of our adaptive tabu search algorithm. Section 4.3 discusses using set partitioning within the tabu search framework as a vocabulary building mechanism. Section 4.4 concludes the chapter by detailing the flow of the entire search heuristic. References to U.S. Air Force crews are specifically to tanker crews.

4.1 Tanker Crew Scheduling Problem

Suppose there exists an air refueling schedule that USAF crews must fly. A *flight* within the schedule is defined as an aircraft departing one base and landing at another base, possibly the same base. A crew's *duty day* is the summed time of its initial briefing, flights flown for the day, waiting time between flights, and its final out briefing. To cover the schedule, a crew may be assigned a number of duty days. A crew *rotation* is defined as the sequence of duty days assigned to a particular crew. Finally, the set of rotations covering all flights create the *crew schedule*.

The nature of the mission of the USAF and its crew ratio difficulties create a problem similar to the airline CSP, but unique in its own right. To clarify this, examine the description of the airline CSP discussed in Chapter III:

- 1) The objective is to minimize the cost of flying the published schedule, subject to the following constraints.
- 2) Each flight must be covered uniquely.

- 3) Each pairing (pairings are sequences of flights a crew flies) must begin at a crew base, fly around the system, and return to the same base.
- 4) Each pairing must conform to the limitations of FAA regulations and published work rules in force at the airline.
- 5) The number of total hours flown from each crew base must be within specific minimum-maximum limits, in accordance with the airline's manpower plan (and constrained by union demands).

While the USAF does not account for a direct cost such as pay-and-credit, it has costs that must be measured. These costs can be described as a hierarchical objective function scheme. The first objective is to minimize the number of tanker crews needed to fly the schedule. The second objective is to maximize the efficiency of those crews. This is done by minimizing the number of hours the crews spend waiting to fly, both within a duty day and between duty days. Good schedules occur when the crews have little idle time during a duty day and receive rest as close as possible to the minimum required rest between duty days.

Scanning the list, it is clear that constraints 2) and 4) above directly correspond to the TCSP. Each flight in the schedule must be covered while meeting USAF regulations.

Table 1 below describes the four main regulatory crew constraints for this problem:

Table 1: Crew Constraints for the Tanker CSP

Constraint	Limit
Flight Duty Day	16 hours (24 with augmented crew) max
Crew Rest	12 hours min
30 Day Flying Limit	125 hours max
90 Day Flying Limit	330 hours max

An augmented crew involves two operational crews assigned to a particular flight(s), thus sharing the flying time. It extends the maximum duty day for each crew by 8 hours. Crew rest is simply the minimum amount of time a crew needs to be inactive between duty periods. The 30 and 90 day flying limits represent the maximum number of hours a crew can fly during those time periods. Since crews enter an operation with a flying history, these histories must be considered when creating a current crew schedule.

Constraint 3) is overly restrictive for the TCSP. In fact, relaxing it allows us to explore the strategic prepositioning of crews, especially once operations leave the deployment phase of a conflict and enter intra-theater operations. Prepositioning crews at bases other than the aircraft home bases allows the search to find better crew rotations by allowing one crew to deboard a tanker and rest while another crew continues the mission.

Allowing crews to deboard one aircraft and take off with another creates an additional constraint within our TCSP. Clearly, a minimum time is needed for crews to leave one aircraft and operate another. Even if crews land and take off with the same aircraft, there exists some minimum time to taxi along the runway between flights. This is modeled by adding a minimum waiting time between flights (*MWBF*) constraint to the TCSP. Since no *MWBF* exists in USAF regulations, these values must be defined by the tanker crew analyst/scheduler using the ATS metaheuristic.

The final constraint added to the model involves simple geography. If a crew arrives at base A, it must also depart from base A. To do otherwise is physically impossible.

Finally, the TCSP is not constrained by 5) above. Instead, the tabu search solution provides the distribution of crew hours needed at each base to cover the flight schedule.

In conclusion, the TCSP can be described as follows:

- 1) Minimize the number of crews required and maximize the efficiency of the crews, subject to constraints 2-7 below.
- 2) Each flight of the aerial refueling problem must be flown uniquely.
- 3) Crew duty days must not exceed 16 hours.
- 4) Once their duty day is over, a crew must rest for a minimum of 12 hours.
- 5) Crews can fly no more than 125 hours in 30 days and 330 hours in 90 days.
- 6) The user-defined *MWBF* must be met.
- 7) Bases of arrival and departure must match for each crew and aircraft.

4.2 Components of the Adaptive Tabu Search

This section describes the components of the adaptive tabu search (ATS) approach used to solve the TCSP. It discusses the solution structure for the TCSP, the heuristic that provides the initial solution, the moves used for the local search process, the methodology used to evaluate those moves, and the tabu lists used to overcome the trap of local optimality. These components comprise the elements needed to use Harder's OpenTS tabu search framework and Wiley's group theory code; the backbone of the JavaTM code developed in this research (Harder, 2002; Wiley, 2000).

4.2.1 Solution Structure.

The cyclic form of the S_n provides a compact solution structure for the TCSP. A TCSP solution is written as the product of disjoint cyclic factors, where each disjoint cycle is a single crew's rotation. The first letter in each cycle is the identification number of the crew, and each remaining letter in a cycle represents the flights flown and the order in which they must be flown.

For example, assume 5 tanker flights must be flown and there exist 5 crews to fly them. By mapping letters 1-5 to crews 1-5, mapping the letters 6-10 to the five flights, and working within S_{10} , each flight must be flown once, satisfying constraint 2) above. Some representative solutions taken from S_{10} that cover each flight once are:

(1,6,7,8)(2,9,10), (1,6,7,8 9,10), and (1,6)(2,7)(3,8)(4,9)(5,10).

Reexamine what each disjoint cyclic factor in the solutions above represents. They are the flights covered by each tanker crew in the solution. For example, (1,6,7,8)(2,9,10) means crew 1 covers flights 6-8, crew 2 covers flights 9-10, and crews 3-5 are unassigned or inactive. It is also clear that crew 1 must fly flight 6, then flight 7, and finally, flight 8.

Various components of our adaptive tabu search use long-term frequency information to perform their individual operations. As the size of the problems grow, storing and comparing information on crew rotations, solutions, or conjugacy classes becomes computationally expensive. A typical solution to this problem is to create hashing functions that map each crew rotation, complete solution, or conjugacy class to integer values (Glover and Laguna, 1997:246). These hashing functions are used to store the frequency information on the various items in hash maps. Sections 4.2.1.1-4.2.1.3 describe the hash functions developed for various components of our solution structure.

4.2.1.1 Rotation (Cycle) Hash Function.

The rotation or cycle hash function is used to capture attributive information on each individual crew rotation. This allows the search to operate on partial solutions and is

specifically used in the vocabulary building conducted by the set partitioning optimizer described in Section 4.3.

Examine the hash calculation of a member of S_{10} as described above. The process begins by generating *randhash*, an n -sized vector of unique random integers uniformly ranging from 1 to $n*n$. Each element of *randhash* maps a random integer to one of the original n letters. In the case of S_{10} , *randhash* has 10 unique elements randomly generated from the $U(1,100)$ distribution. Given a crew rotation or disjoint cycle d with m elements, define the hashing function as follows:

Equation 2: Hashing Function for a Crew Rotation

$$h_d = \prod_{i=1}^m \text{randhash}[d_i], \text{ where } d_i \text{ is the letter found in position } i \text{ of cycle } d.$$

For example, suppose we have *randhash* = [2,51,11,24,74,43,19,15,60,9] and $d = (1\ 6\ 7\ 8)$. The resulting hash value is calculated as $h_d = 2*43*19*15 = 24510$.

It is clear that h_d is specific to the TCSP because it does not account for the ordering of the elements within d . This is sufficient for the TCSP because of the manner in which the letters are assigned, the departure time ordering of the input flight schedule, and the candidate list strategies used to build the neighborhoods in Section 4.2.3. Collisions occur when two different rotations are mapped to the same hash value. The ATS explicitly avoids collisions between cycles such as (1,6,7,8), (1,6,8,7), (1,7,6,8), (1,8,6,7), and (1,8,7,6) by using candidate list strategies to disallow solutions such as the last four because of inappropriate departure time sequencing.

While h_d is specific to our problem, it is possible to slightly modify the methodology and create a generalized form for h_d . This generalized form is useful in solving combinatorial optimization problems where within-cycle ordering matters. Start by

generating *randhash*, an $n \times n$ -sized array of unique random integers uniformly ranging from 1 to $2 * n^2$. Each element of *randhash* maps the arc $i-j$ in a disjoint cycle. For example, for the disjoint cycle (1 6 7 8), *randhash*[1][6] is the random integer representing the arc 1-6 in the cycle. The trivial inactive crews such as (3) are mapped to elements *randhash*[i][i]. For S_{10} , *randhash* has 100 unique elements from the $U(1,200)$ distribution.

Given a crew rotation or disjoint cycle d with m elements, we define the generalized hashing function as follows:

Equation 3: General Hashing Function for Disjoint Cycles

$$h_d = randhash[m][1] * \prod_{i=1}^{m-1} randhash[d_i][d_{i+1}],$$

where d_i is the letter found in position i of cycle d and *randhash*[m][1] is the arc from the last letter in d to the first letter.

One obvious disadvantage with Equation 3 versus Equation 2 is the storage requirements for *randhash*. In Equation 3 the storage requirement is $O(n^2)$, while it is only $O(n)$ for Equation 2.

4.2.1.2 Solution Hash Function.

The importance of the solution hash function to the ATS cannot be overemphasized. It is used for comparisons within the tabu list and helps drive much of the adaptive scheme throughout the search. This said, a simple extension of the rotation hash function works extremely well for the TCSP. Suppose solution s exists with c disjoint cycles or crew rotations. The solution hash function is defined as follows:

Equation 4: Solution Hashing Function for the TCSP

$$h_s = \sum_{d=1}^c h_d, \text{ where } h_d \text{ is defined in Equation 2 above.}$$

If a generalized solution hash function is required for a different application, simply modify Equation 4 by using the h_d defined in Equation 3. Since the symmetric group theory code used to build the ATS contains a method to calculate hash values for group elements, it appears useful to compare the new hash function to it. Table 2 below displays the results of the comparison:

Table 2: Comparison of generalized h_s and the existing group theory hash function

n	Size of S_n	Collisions with group theory hash function	Collisions with h_s	Cum time to calculate with group theory hash (milliseconds)	Cum time to calculate h_s (milliseconds)
3	6	0	0	0	0
4	24	0	0	0	0
5	120	1	0	0	0
6	720	11	0	0	0
7	5040	555	4	47	16
8	40320	9801	35	153	109

Table 2 clearly shows h_s outperforms the existing group element hash function. Not only does it significantly reduce the number of collisions, but it calculates the hash value in less time.

4.2.1.3 Conjugacy Class Hash Function.

Knowing the conjugacy class of a solution may prove useful to general tabu search methodologies. Intensification or diversification schemes may be driven by long term conjugacy class frequency information. In our TCSP application, conjugacy class frequency information was used for two purposes. During ATS development, it was used

to determine if the search was achieving suitable diversification. This conjugacy class information, recorded using the conjugacy class hash function below, spurred changes that improved the flow of the ATS. In Chapter VI, this conjugacy class information is used to measure the degree of diversification achieved by the ATS.

To gather conjugacy class frequency information, it is useful to use a hashing function as seen with rotations and solutions above. The conjugacy class hash function is based on the typical notation for a conjugacy class:

$1^{m_1} 2^{m_2} \dots k^{m_k} \dots n^{m_n}$, where m_k is the number of cycles of length k in the solution (Sagan, 1991 : 2).

For example, the solution (1 6 7 8)(2 9 10) above (remember it contains 5 crews) is in the conjugacy class $1^3 3^1 4^1$.

Given the conjugacy class notation, we define the conjugacy class hash function as follows:

Equation 5: Conjugacy Class Hash Function

$h_{CC} = \prod_{i=1}^r k_i \cdot \text{concat}(m_{k_i})$, where $k_i \cdot \text{concat}(m_{k_i})$ is the concatenation of k_i and m_{k_i} and r is the number of distinct cycle sizes in the solution.

Therefore, the hash value of the conjugacy class $1^3 3^1 4^1$ above is $13 * 31 * 41 = 16523$.

4.2.1.4 Characterizing the TCSP Solution.

To adapt various parameters during the search, it is useful to characterize a TCSP solution in terms of feasibility. Section 4.2.1 concludes by defining three types of feasibility measures: feasible, near feasible, and poor infeasible.

Feasible solutions are those solutions that meet all TCSP constraints. These are risk free solutions for the decision maker, i.e., all USAF regulations are satisfied.

Near feasible solutions violate some of the constraints, but the amount of constraint violation is within an acceptable tolerance. By examining and recording near feasible solutions, a decision maker may examine the risks of relaxing constraints such as crew rest. The size of each constraint deviation is user-defined and preset prior to starting the solver.

Finally, a poor infeasible solution exceeds the allowable constraint violation on one or more of the TCSP constraints. These are solutions that exceed at least one of a decision maker's acceptable tolerances.

The solution structure has been discussed, three useful hashing functions have been developed, and TCSP solutions have been characterized. The next section discusses the heuristic that provides a starting point for the ATS.

4.2.2 Initial Solution Construction.

The first task in starting the tabu search is creating an initial solution. The heuristic used is very similar to the Crew Dog tool used by AMC analysts today and is clearly suboptimal. This research uses a global tabu search approach to find better solutions. Figure 5 below displays the flow of the process.

The tabu search runs in two modes: analysis or operational. The analysis mode allows AMC analysts to study questions such as, "What is the proper crew ratio for a given scenario and how does the structure of the schedule affect this?" The operational mode assumes that AMC crews are physically mobilized for a deployment or other operation. It searches the solution space to find extremely good flight assignments for these crews. Each mode considers all crew constraints as defined in Section 4.1.

The only component of the ATS affected by these two modes is the initial solution heuristic. Once an initial solution is constructed, the tabu search operates identically for each mode.

In analysis mode, the heuristic assumes it is given an aircraft schedule sorted in order of increasing flight departure, i.e., the first flight in the list departs the earliest. The heuristic then creates an initial crew and populates its 30 and 90 day flying histories in a Java™ array list. The flying histories are populated using two monte carlo draws. The first uses a user-supplied input parameter, $prob_{fly}$, to determine whether or not a crew flew on any of its previous 90 days. If a crew did fly, then another draw is made and compared to the cumulative flying time distribution in the AMC furnished *crewProbabilities.txt* file to determine the flight duration. The $prob_{fly}$ and *crewProbabilities.txt* allow an analyst to study how historical operations tempo affects current warfighting.

Once the first crew is created, the heuristic begins to iterate through each flight in the schedule. For each flight, it examines each crew by order of creation. It checks all constraints and determines if a crew can feasibly cover the flight. If so, the heuristic assigns the flight to the crew with the smallest identification number. Otherwise, the heuristic creates a new crew, populates the 30 and 90 day flying histories, and determines whether or not the new crew can cover the flight. New crews are created until all flights in the aircraft schedule are covered. The heuristic ensures an initial feasible solution when running the tabu search in analysis mode.

The operational mode heuristic is slightly different. It assumes the same type of flight schedule as described above, but it also assumes the existence of a *crewHistory.txt* file.

This file contains the 30 and 90 day flying histories of each mobilized crew. Instead of creating crews on the fly, the heuristic immediately instantiates the given number of crews and reads their crew histories from the text file.

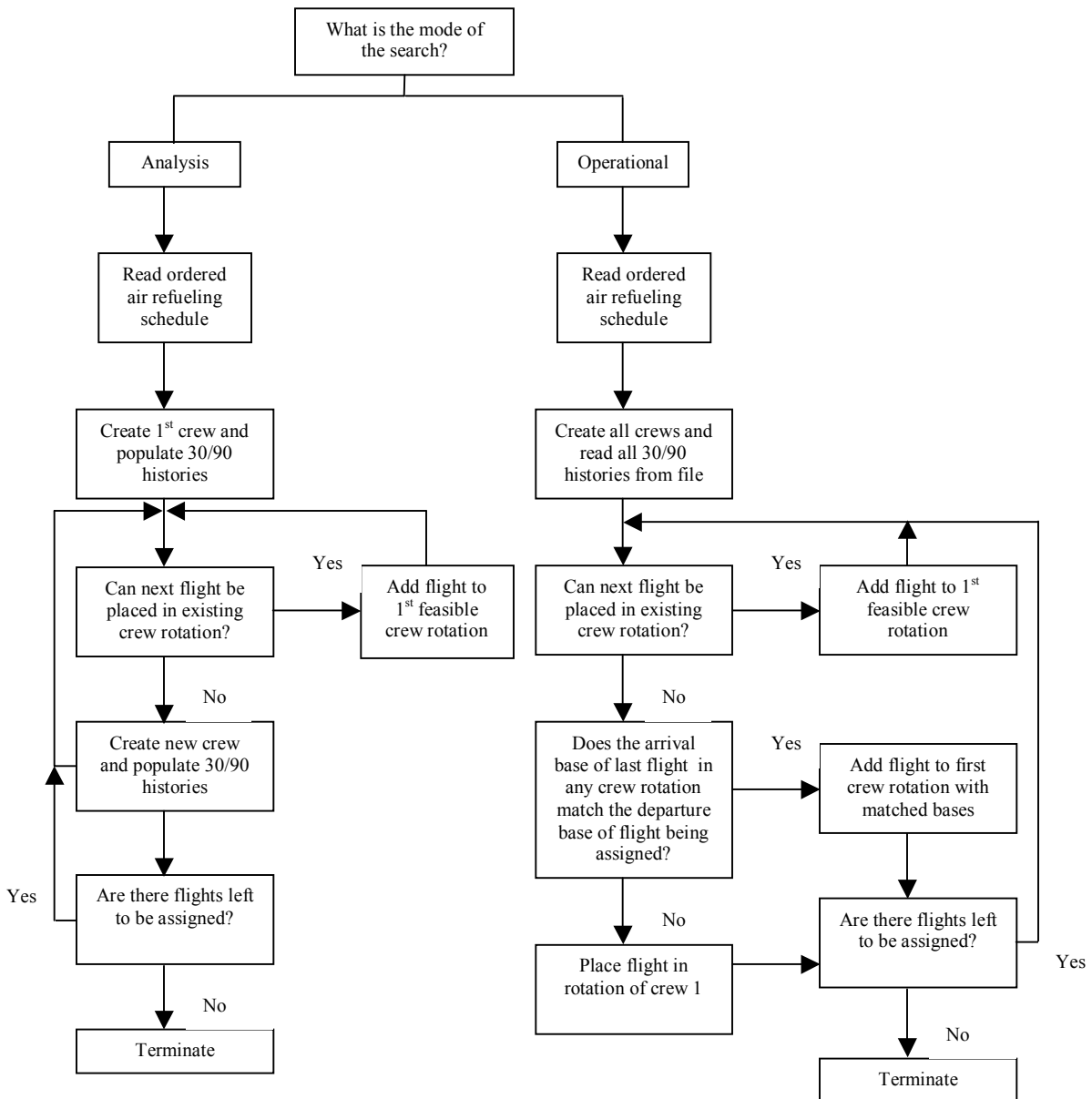


Figure 5: Initial Solution Heuristic

The heuristic then begins iterating through the flights. For each flight, the heuristic checks the TCSP constraints and determines if one of the existing crews can cover it. If so, the flight is assigned to the crew with the smallest identification number. If not, it is clear that the initial solution is infeasible. It then ignores every constraint other than matching the arrival and departure bases. It assigns the flight to the crew with the smallest identification number whose last arrival base matches the flight's departure base. If no arrival-departure base matches are available, the heuristic places the flight in the rotation of crew one. If this occurs, the initial solution contains a physical dislocation and becomes severely infeasible.

Once an initial solution is built, the tabu search must examine its neighborhood to determine the next incumbent solution. The next section discusses the neighborhoods built within the ATS, as well as the candidate list strategies used to restrict the neighborhood size.

4.2.3 Restricted Neighborhood Construction.

The local search examines the current neighborhood of an incumbent solution, and chooses a move to a different solution. This section defines the moves used to create the neighborhood structure.

For scheduling problems, it is well known that good tabu search algorithms have been developed using swap and insert moves (Barnes, *et al.*, 1995; Lourenco, *et al.*, 1998; O'Rourke, *et al.*, 2001; Wiley, 2001). For the TCSP, a swap is defined as exchanging

flights in two crew's rotations and an insert is defined as taking a flight from one crew's rotation and placing it in another crew's rotation.

As problem size increases, individual swap and insert neighborhoods can become excessively large. For example, the complete swap neighborhood for 1000 flights consists of $1000(999)/2 = 499,500$ members. This research used a TCSP specific candidate list strategy to reduce neighborhoods of this size. The ATS uses the following restrictions to create its Restricted Swap Neighborhood:

- 1) Only swap flights between disjoint cycles or rotations.
- 2) Only swap flights that maintain proper base of arrival-departure matching.
- 3) Only swap flights that maintain increasing letter order within each affected rotation.

Given the time-sequenced nature of the TCSP, it does not make sense to swap flights within a crew's rotation. Doing so creates a situation where a crew's departure for one flight occurs later than the departure time for a subsequent flight in its rotation. For example, in the solution (1,3,4,6)(2,5,7,8), it is not realistic to swap flights 4 and 6 to obtain (1,3,6,4)(2,5,7,8) because it violates departure time sequencing.

Swap restriction 2) ensures that crews are physically able to fly the given rotations. Swap restriction 3) is similar to 1) in that it avoids inappropriate time sequencing in the rotations. Unlike 1), swaps between two disjoint cycles are examined to determine if a poor sequencing results. Let us return to the solution (1,3,4,6)(2,5,7,8). Exchanging flights 4 and 8 results in the solution (1,3,8,6)(2,5,7,4). Clearly, both crews now have inappropriate time-sequenced rotations.

Similarly, the Restricted Insert Neighborhood is created using the following restrictions:

- 1) Only insert a flight from one crew rotation to another.
- 2) Only allow inserts that maintain proper base of arrival-departure matching.
- 3) Only allow inserts that maintain increasing letter order within each affected rotation.

Allowing inserts within cycles creates the same sequencing problem as the within cycle swaps described above. Insert restriction 2) maintains geographical feasibility. Insert restriction 3) is similar to the swap restriction as well. Given (1,3,4,6)(2,5,7,8), the search disallows inserting flight 7 in front of 4 to create (1,3,7,4,6)(2,5,8) because it creates inappropriate departure time sequencing for the first crew.

With the Restricted Swap and Insert Neighborhoods created, it may appear enticing to use them sequentially, i.e., use an insert to take us to a different solution, and then explore the solution's conjugacy class with the swap neighborhood. But previous tabu search methods have demonstrated better performance by examining the neighborhoods simultaneously (Barnes, *et al.*, 1995). Therefore, the ATS uses a Combined Restricted Swap/Insert neighborhood (CRSIN).

The ATS can periodically become trapped in areas of poor infeasibility during the search process. The ATS responds to this situation by changing the structure of the CRSIN described above. It does this in two ways. First, it allows mismatches between arrival and departure bases. Second, the neighborhood targets the crews that are currently infeasible. We call this neighborhood the Targeted Combined Restricted Swap-Insert Neighborhood (TCRSIN). The TCRSIN is vital for escaping the trap of poor

infeasibility. Once the ATS determines the solution trajectory is trapped in poor infeasibility, as explained in Section 4.4.2, it uses the TCRSIN until, at a minimum, near feasibility is restored.

Once the CRSIN or TCRSIN is built, the next move cannot be chosen until all members of each neighborhood are evaluated. The next section describes the adaptive methodology used to evaluate each neighborhood move.

4.2.4 Solution and Move Evaluation.

This section describes how individual solutions and solution/move pairs are evaluated during the ATS. It begins by discussing the evaluation of individual TCSP solutions and solution/move pairs. It then details the scheme used to adapt the evaluation function's numerous penalty weights. It concludes by describing the methodology used to calculate the penalties for the TCSP constraints.

To evaluate the initial solution or a solution generated from a restart, Equation 6 is used:

Equation 6: Solution Evaluation

$$\begin{aligned} eval_{solution} = & \text{waiting time} + \rho_{crews} * (\# \text{ crews}) + \rho_{rest} * (\text{rest penalties}) + \\ & \rho_{duty} * (\text{duty day penalties}) + \rho_{MTBF} * (MTBF) + \rho_{30} * (\text{thirty day penalties}) \\ & + \rho_{90} * (\text{ninety day penalties}) + \rho_{bases} * (\text{mismatched base penalties}) \end{aligned}$$

Notice that the evaluation function clearly captures the objectives and constraints that compose the TCSP: a crew variable to capture the number of crews in the solution, a waiting time variable to capture a measure of the efficiency of the schedule, and penalty variables relating to violations of each TCSP constraint.

With the swap and insert moves used, only two crews are affected at any iteration of the search. Therefore, instead of using Equation 6 for each move evaluation, the ATS uses a well-known incremental means of evaluating moves. First, the ATS calculates the difference in the number of crews between the incumbent solution and the solution created by the move. It isolates the two crews affected by the move, and calculates the differences in each remaining variable for those crews alone. Of course, the crew waiting time and constraint penalties must be stored and updated each iteration.

The resulting move evaluation function is as follows:

Equation 7: Move evaluation

$$eval_{move} = \Delta waiting\ time + \rho_{crews} * \Delta(\# crews) + \rho_{rest} * \Delta(rest\ penalties) + \rho_{duty} * \Delta(duty\ day\ penalties) + \rho_{MTBF} * \Delta(MTBF) + \rho_{30} * \Delta(thirty\ day\ penalties) + \rho_{90} * \Delta(ninety\ day\ penalties) + \rho_{bases} * \Delta(mismatched\ base\ penalties)$$

Given $eval_{move}$, OpenTS uses the following criteria to choose a move:

- 1) Choose the move with the smallest evaluation value, to include an unimproving move.
- 2) If two move values are equal, choose the move occurring first in the neighborhood.

Equations 6 and 7 contain seven penalty parameters that the ATS must continuously adapt. These parameters allow the ATS to control its strategic oscillation between the feasible, near feasible, and poor infeasible areas of the solution space. The ATS implements the self-adjusting scheme proposed by Gendreau, *et al.* (1996) and used successfully by O'Rourke, *et al.* (2001). This research shows the scheme can successfully control a significantly larger number of parameters, nearly four times the number of penalties adjusted for O'Rourke's vehicle routing problems. Each of the

penalty parameters described in Equations 6 and 7 are independently adjusted every five iterations as follows:

Equation 8: Penalty parameter adjustment

$$\rho_i \rightarrow \rho_i * 2^{\text{penalty}/5-1}, \text{ where } i = \text{crews}, \text{rest}, \dots \text{bases}.$$

The value of *penalty* in Equation 8 varies depending on the parameter being adjusted.

For ρ_{crews} , *penalty* is the number of feasible or near feasible solutions in the last ten iterations. Therefore, if the last ten iterations have all been feasible or near feasible solutions, ρ_{crews} doubles and induces the search to move to smaller crew solutions. If the last ten iterations have all produced poor infeasible solutions, the value of ρ_{crews} is halved and the search moves towards solutions with a larger number of crews.

For the parameters relating to the TCSP constraints, *penalty* refers to the number of *i* infeasible solutions found in the last ten iterations, i.e., for $i = \text{rest}$, the number of infeasible solutions that violated crew rest. As with the ρ_{crews} , if constraint *i* is violated during each of the last ten iterations, ρ_i doubles and provides an incentive for the constraint to be satisfied. Likewise, ρ_i halves if *i* was not violated during the last ten iterations. When the violation counts are greater than zero and less than ten, the search adjusts the penalty between ½ and 2 times the current penalty.

A description of the method used to quantify the number of active crews and constraint penalties found in Equations 6 and 7 concludes this section. When evaluating a complete solution, the ATS simply counts the number of nontrivial disjoint cycles in the group element and records this value as the number of active crews in the solution. When determining the number of active crews created by a move, the ATS first checks

the type of move evaluated. If the move is a swap, the ATS recognizes that conjugation maintains the number of active crews. If the move is an insert, one of three cases may arise and the ATS recognizes such:

- 1) The insert leaves the number of active crews the same.
- 2) The insert takes the only assigned flight from one active crew and places it in another crew's rotation. This deactivates the crew that lost the flight and reduces the number of active crews by one.
- 3) The insert takes a flight from an active crew with multiple flights and places it in a previously inactive crew's rotation. This activates the crew and increases the number of active crews by one.

When evaluating a complete solution, the ATS first initializes a penalty array for each constraint. It then performs the linear operation described in Figure 6 to calculate and record penalties for each constraint and each crew. For each constraint, the crews' penalties are summed for use in Equation 6. For subsequent move evaluations, the linear operation is performed for the two crews affected by the move and the crews' recorded penalty information is used to calculate the differences found in Equation 7.

A simple example is now used to describe the algorithm displayed in Figure 6. Assume crew 0 covers flights 1-4, so the crew rotation is (0,1,2,3,4). The ATS first penalizes the solution for any 30 or 90-day flying history violations, as described below.

It initializes the first flight in the rotation and first flight in the duty day to flight 1. The ATS assumes the schedule starts with the initial briefing that occurs before the schedule's first flight departure. The briefing length is a user-defined value, set to forty-five minutes for this research. The time between the departure of flight 1 and the schedule's start time is added to crew 0's waiting time. In this case, flight 1 is the first flight in the schedule so no waiting time would be added. If more flights exist, the flight

to examine is incremented by one. In this case, flight 2 is the next flight to examine. The waiting time from the arrival of flight 1 to the departure of flight 2 is added to crew 0's waiting time array. The ATS then determines if the minimum wait time between flights 1 and 2 is satisfied, linearly penalizing if necessary. Linear penalties are used for every constraint and calculated as such:

Equation 9: Linear Penalties for TCSP Constraints

$penalty = | actual\ value - desired\ value |$, where *actual value* is the value calculated by the algorithm and *desired value* is the target value of the particular constraint; for example, the algorithm may calculate 11 hours rest between two flights and the rest constraint states 12 hours are required.

After checking the *MWBF* constraint, the ATS determines if the departure base of flight 2 matches the arrival base of flight 1. If the bases are different, a penalty of 1 is added to crew 0's mismatched base penalty array. Notice that while *MWBF* is described in time units, the mismatched bases penalty is a binary, unitless value that simply states whether or not a mismatch occurred. The adaptive penalty scheme previously described allows the smooth integration of these two types of penalties.

Next, the ATS determines if the minimum amount of rest occurs between flights 1 and 2. If sufficient rest exists, the examined flight is set as the start of the next duty day and the next existing flight is set as the flight to examine. In this case, the ATS sets flight 2 as the first flight in the next duty day and sets flight 3 as the flight to examine. If insufficient rest exists, the ATS checks the duty day constraint.

The length of the duty day is calculated between the first flight in the duty day, in this case flight 1, and the arrival flight being examined, in this case flight 2. If the duty day constraint is satisfied, the ATS increments the flight to examine by one and restarts the

process at the waiting time calculation. In this case, the flight to examine would be incremented to 3 while the first flight in the duty day remained 1. If the duty day constraint is violated, the ATS performs a local optimization by determining the minimum of the proposed rest and duty day penalties. In developing the ATS, we found the following reasons to integrate this local optimization within the algorithm:

- 1) If both constraints are penalized, the solution is unduly penalized and the search fails to seek solutions with a smaller number of crews.
- 2) The particular constraint penalized drives the duty day flow, as we describe now.

Suppose the ATS determines crew rest is the least violated constraint. The ATS then flows to a new duty day and sets the flight being examined, in this case 2, as the first flight in that duty day. The flight to examine is set to flight 3, and the ATS restarts processing the constraint penalties.

Suppose the ATS determines duty day length is the least violated constraint. In this case, the ATS completes the existing duty day with the flight being examined, i.e., completes the duty day with flight 2, and starts a new duty day with the next existing flight, flight 3. The algorithm records the waiting time between the departure of the first flight in the next duty day and the arrival of the last flight examined. It must also check all constraints but the duty day constraint. In this case, the waiting time between flights 2 and 3 is recorded and all constraints but the duty day constraint are checked. This flow is seen in the lower right hand corner of Figure 6. With this complete, the ATS sets the flight to examine as the next existing flight, i.e., flight 4, and restarts the process.

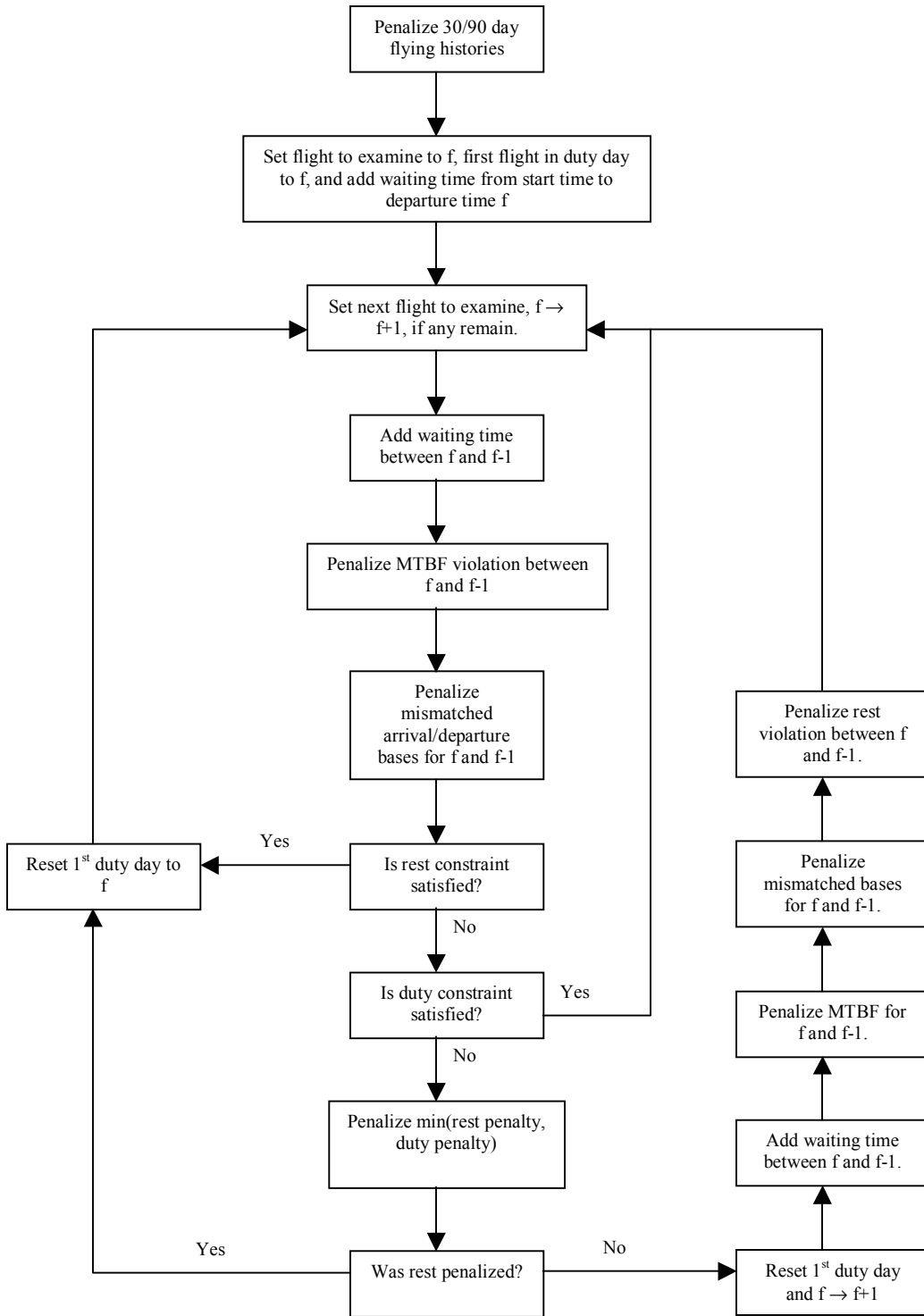


Figure 6: Evaluation of a Single Crew

In Figure 6, notice the ATS calculates the 30 and 90 day flying history penalties before starting its loop to determine the remaining penalties. The calculation of the history penalties is another operation approached separately. While calculating the other penalties, the ATS kept track of the rest and duty day structure of the crew rotation. When calculating the flying history penalties, the ATS must track the 30 and 90 calendar day windows.

The approach to the problem is straightforward. To evaluate the crew's rotation, the flying history array list is updated to recognize additional flying time and recognize the passing of time. Whenever the algorithm transitions to a new calendar day, it determines whether or not to penalize the 30 or 90-day flying history constraints. There is one exception to this rule. When there are idle days between flights, the ATS does not attempt to penalize the histories as the array list transitions. Idle days added to the 30 or 90-day history cannot create either constraint violation, and the ATS would double penalize for previous flights if it checked the histories again.

The logic required to implement the approach is presented below, and its discussion is broken into two parts: calculation of the 30 and 90-day flying history penalties for the first flight and calculation of the 30 and 90-day flying history penalties for all remaining flights.

Figure 7 displays the process used to calculate the 30 and 90-day flying histories for the first assigned flight. First, the flying history array list is updated to account for idle time between the schedule start time and the departure time of the first flight in the crew's rotation. For example, if there are three idle days before the crew starts its

rotation, the top three elements of the array list are removed and three flying days of zero are added to the end of the list.

The second step determines if the first flight departs and arrives on the same day. If so, it removes the first member in the list and adds the first flight time to the bottom. If no other flights exist in the rotation, penalties for the 30 and 90-day flying histories are calculated and the algorithm terminates. If other flights exist, the ATS moves to examine the next flight in the rotation.

If the first flight's departure and arrival days are different, a separate sequence of events occurs. First, the ATS removes the top member of the array list and adds the flying time occurring on the day of departure to the bottom of the list. Since the algorithm removed a day from the history list and added the most recent day, it checks the crew history and calculates history penalties. The ATS removes the top member of the list again and adds the flying time occurring on the day of arrival to the bottom of the list. At this point, the ATS makes another decision. If no other flights exist in the rotation, it calculates history penalties and the algorithm terminates. If other flights exist, history penalties are not calculated because the flying day may not be finished. The ATS simply moves to examine the next flight in the rotation.

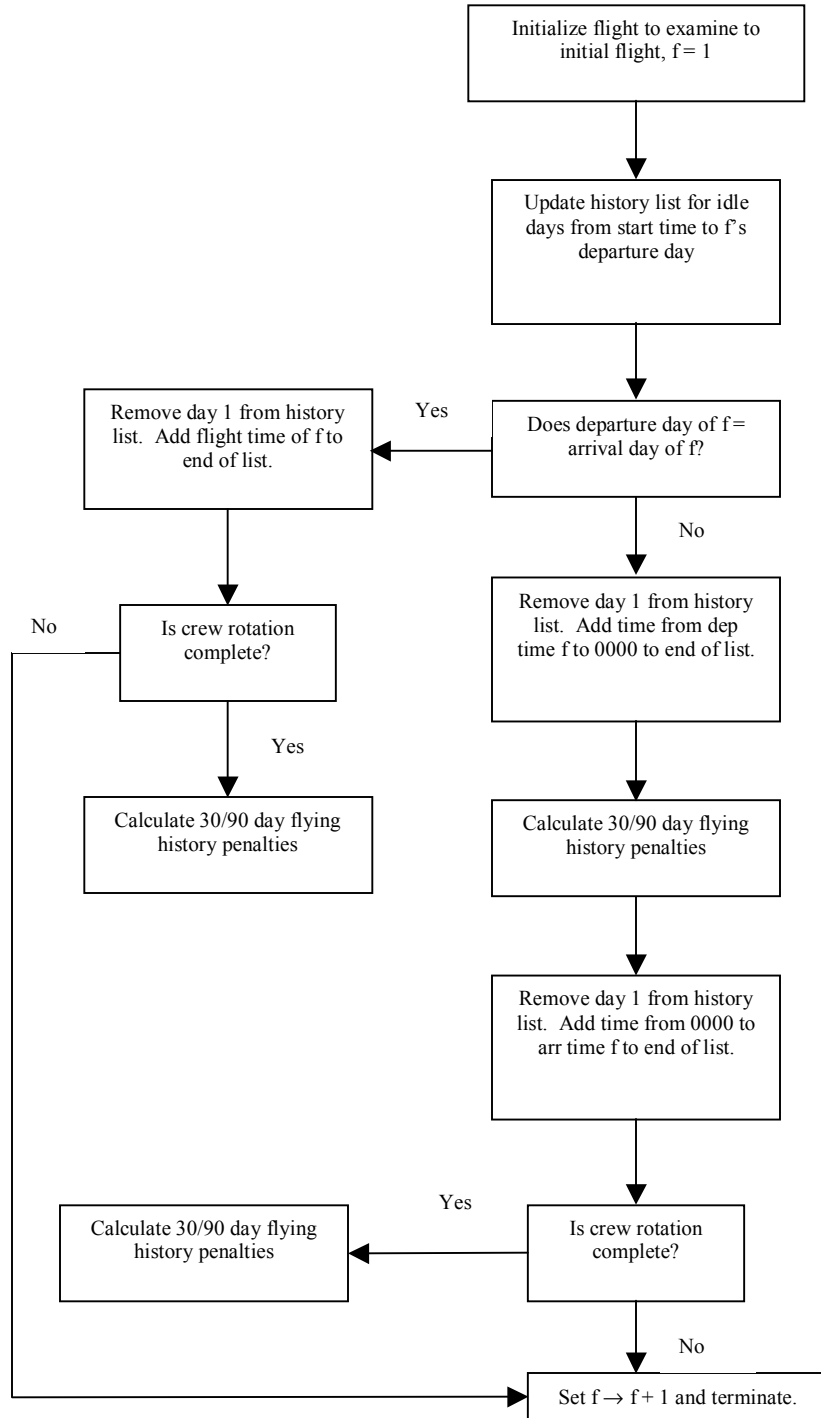


Figure 7: Evaluation of 30/90 Day Flying History for First Flight

Figure 8 below displays the logic used to evaluate the remainder of the crew's flights. The ATS first determines if the previous flight arrives on the same day the current flight departs. If not, the flying day previously left open is complete and history penalties are calculated. The history list is updated for idle days between the previous flight's arrival and the current flight's departure. Once the list is updated for idle days, the logic is identical to that described for the first flight.

If the previous flight's arrival day and the current flight's departure day are identical, the logic changes. The ATS first determines if the current flight's departure and arrival days are the same. If they are, the current flight is completed on the same day the previous flight finished. Therefore, no days are added to or removed from the history list.

The current flight time is simply added to the flying time of the last day on the history list. If the current flight completes the rotation, history penalties are calculated and this part of the algorithm terminates. If not, the ATS returns to evaluate the next flight in the rotation.

If the current flight's departure and arrival days are different, the ATS first updates the last day in the history list by adding the flying time occurring during the current flight's departure day. Note, the top member of the history list is not removed because the current flight's departure day flying time occurs on the same day as the previous flight's arrival. Once this update occurs, the ATS calculates history penalties. It removes the first member of the history list and adds the current flight's arrival day flying time to the end of the list. If the crew rotation is complete, the history penalties are calculated and this part of the algorithm terminates. If other flights exist, the ATS returns and evaluates the next flight in the rotation.

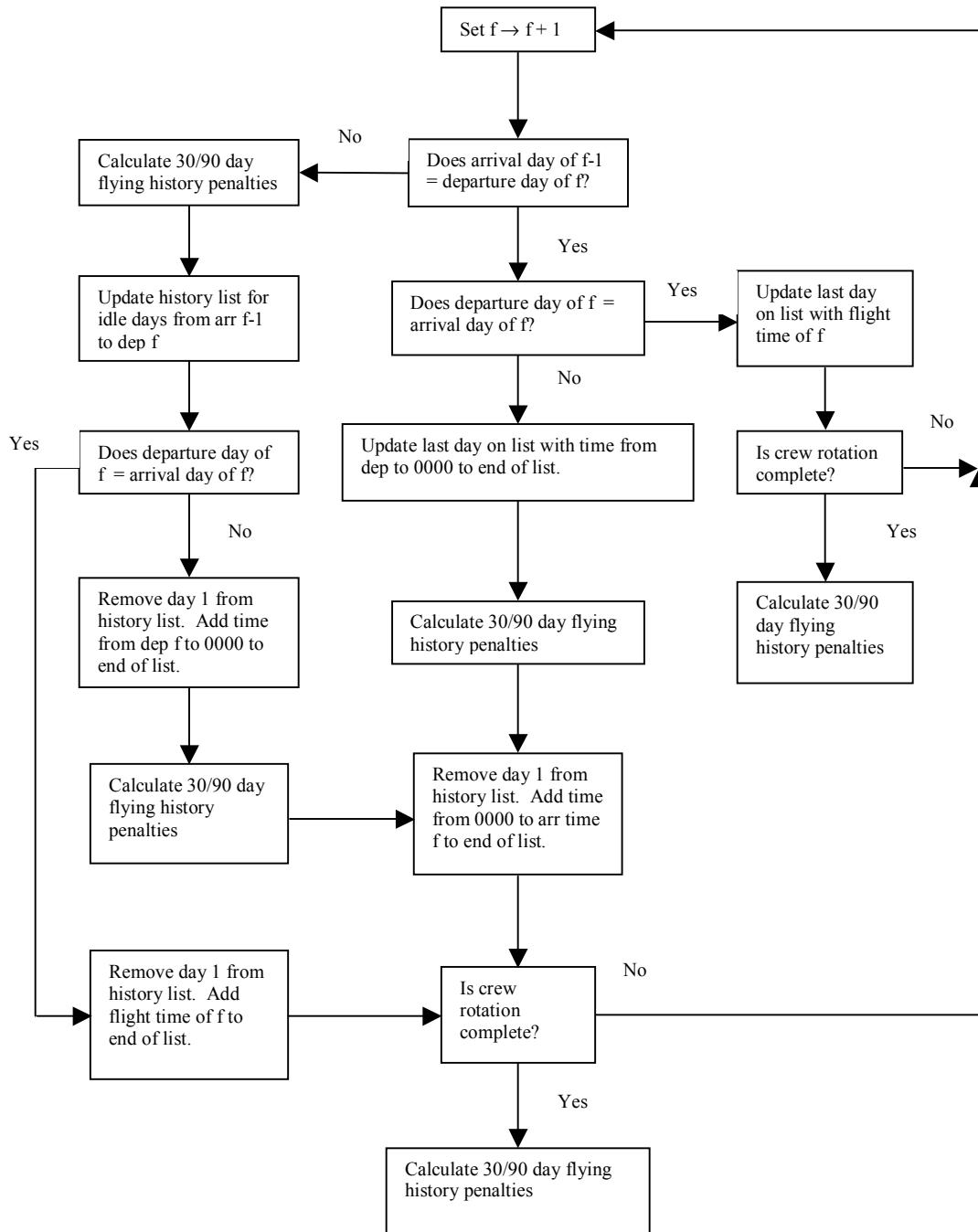


Figure 8: Evaluation of 30/90 Day Flying History for Other Flights

4.2.5 Tabu List.

Now that a procedure exists to calculate solution and move values, this section describes the tabu lists created for the ATS. Recall that tabu search uses tabu lists to avoid becoming trapped at local optimum.

The ATS uses a solution-based tabu list. The search records the hash value of each solution visited in a JavaTM array list. The tabu tenure is implemented in two ways. The statistical analysis in Chapter VI provides a comparison of their utility.

The first approach makes every solution visited tabu for the rest of the search. Morton and Pentico (1993) suggest this tenure is robust for a wide variety of scheduling problems. This is simple to implement, but it may significantly restrict the tabu search and may be computationally expensive.

This implementation restricts the search because of its interaction with the move evaluation function previously described. Suppose the ATS arrives at solution x , at iteration 100, with a set of penalty weights as defined in Section 4.2.4. If the ATS allowed a return to solution x at iteration 1000, the penalty weights would likely be different and could possibly send the trajectory into a part of the solution space superior to the area originally visited from x . Making all previously visited solutions tabu would prevent x from being revisited, and could restrict the tabu search.

An adaptive tabu tenure is the second scheme studied in this research. Assume the tabu tenure at a particular iteration is t . The ATS searches the last t elements of the array list previously described to determine tabu status. The ATS adapts the tenure using the following rules:

- 1) If the current solution is a revisited solution, the tabu tenure doubles.

2) If the current solution is unique, the tenure decreases by one.

Rule one should allow the search to quickly escape cycling and provides a diversification mechanism for the search. Rule two should provide a means to reduce the severe tabu restriction of a long list when cycling ceases.

4.3 Vocabulary Building With Set Partitioning

This research extends the heuristic/post-optimization approach discussed in Section 2.1.2 by developing an integrated tabu search/SPP optimizer. This section describes the SPP portion of the optimizer, while the next section describes how the SPP optimization is embedded within the overall tabu search scheme.

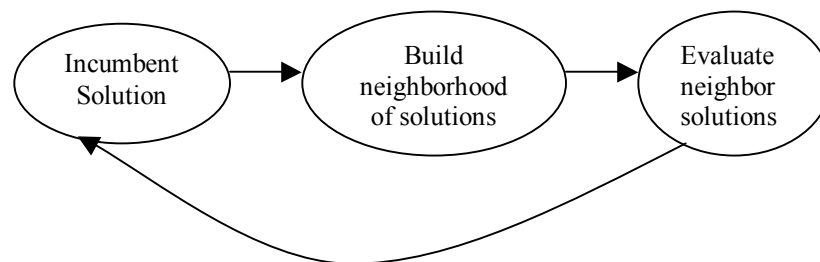


Figure 9: Typical Local Search

Figure 9 displays the typical flow of a local search algorithm. From an incumbent solution, a neighborhood of solutions is built and evaluated, with a new incumbent solution chosen from the neighborhood.

Kelly and Xu note that some of their heuristic solutions to the VRP are infeasible, but these infeasible solutions contain good partial solutions that should be included in the pool of columns sent to the SPP optimizer (Kelly and Xu, 1998:4). This research extends

this idea by developing a pool that contains good partial solutions from the initial solution and good partial solutions from the series of created neighborhoods.

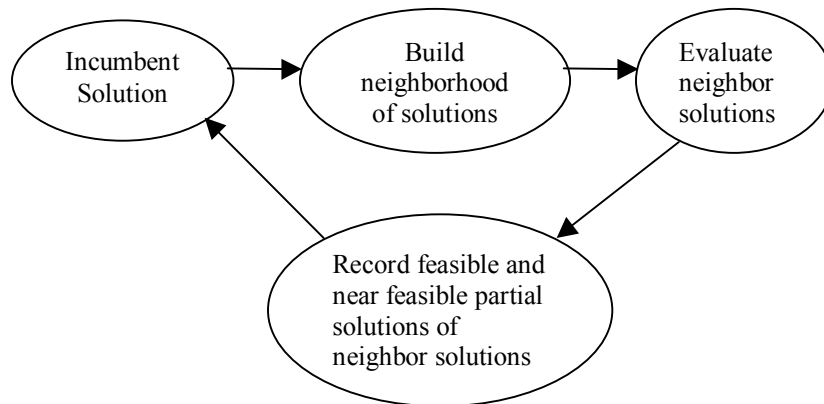


Figure 10: ATS Local Search

Figure 10 shows the ATS method for collecting partial solutions. To initialize the pool, all the feasible or near feasible crew rotations from the ATS initial solution are added to a Java™ hashmap that stores their hash value as the key and a rotation/waiting time pair as the value. Near feasible rotations may initially occur when no feasible starting solution exists for a problem solved in the operational mode.

Once the pool is initialized with the individual crew rotations from the starting solution, crew rotations may be added with each neighborhood move evaluation. Since the neighborhoods created within this research consist of swaps and inserts, only two crews are affected by any move. If the crew rotations of either affected crew are feasible or near feasible partial solutions, and the partial solutions have not been previously recorded, the hashmap is updated with the appropriate rotation/waiting time pair.

At various times during the search, the ATS solves a near feasible or feasible SPP using the Java Concert Technology embedded within ILOG CPLEX 7.5. The near feasible SPP contains crew rotations that are both feasible and near feasible. The feasible SPP has columns whose crew rotations are all feasible. This ensures the solution created by solving a feasible SPP is itself feasible. The next section describes exactly when the ATS chooses to solve the two types of problems. The SPP was defined in Equation 1. In this case, the waiting time of each rotation represents its cost coefficient. There are two reasons for using waiting time despite its minimization being the ATS's secondary objective:

- 1) Solving a SPP that minimizes the number of active crews causes the ATS to converge prematurely to poor solutions. These solutions characteristically have poor waiting times AND an unnecessarily large number of active crews.
- 2) Feasible solutions often occur in the vicinity of near feasible solutions. Minimizing waiting times moves the search to near feasible solutions with increasingly fewer active crews. The tabu search itself finds smaller-crewed feasible solutions near these infeasible solutions. The ATS uses the SPP optimizer to vocabulary build. The SPP's main role is to provide the ATS with excellent points at which to restart the search.

Finally, note that many of the SPP problems the ATS creates are too large for CPLEX to efficiently solve. In some cases, the solution time for CPLEX either overwhelms the overall search time or CPLEX runs out of memory and fails to report a feasible answer. Therefore, the ATS actually uses CPLEX in a heuristic manner. It places a ten-minute threshold on the SPP solution process. If an optimal solution is not found in ten minutes, CPLEX reports the best solution found so far.

4.4 Completing the ATS Framework

With the discussion of the components of the ATS and SPP optimizer complete, this section completes the chapter by describing how the overall tabu search process functions. The first section describes an iteration of the adaptive tabu search, as driven by Harder's OpenTS software (2002). The second section discusses the first variant of the ATS, an adaptive search that includes an intensification scheme. The final section completes the chapter by discussing the integrated ATS/SPP optimizer.

4.4.1 One Iteration of the ATS.

Figure 11 below displays an iteration of the OpenTS tabu search framework (Harder, 2002). This basic sequence is repeated throughout the ATS process, except in the special case where the SPP optimizer completes the iteration. It is important to note that the OpenTS architecture provides none of the fundamental methods needed to solve a TCSP. All the methods described in Section 4.2 were coded independently, and OpenTS simply provided tabu search bookkeeping services.

The process is as follows: the ATS starts from an initial solution built using the greedy heuristic of Section 4.2.2. It builds the neighborhood of restricted moves described by Section 4.2.3. These neighborhoods are adaptive, meaning the neighborhoods change from iteration to iteration depending on the current incumbent solution and long-term frequency memory. Once the moves are created, they are sent to the objective function evaluator. The objective function evaluator uses the methods described in Section 4.2.4 to evaluate the neighborhood. The best non-tabu move amongst the moves in the neighborhood is chosen next. The determination of the best

move is an adaptive process for the ATS with intensification, and it is described in the next section. Finally, the move is used to operate on the current solution. If the move is a swap, the ATS uses conjugation to move to the new current solution. If it is an insert move, the ATS uses the function composition operator. These are the conjugative and template-based moves described in Section 2.2.1. With a new incumbent solution found, the process repeats.

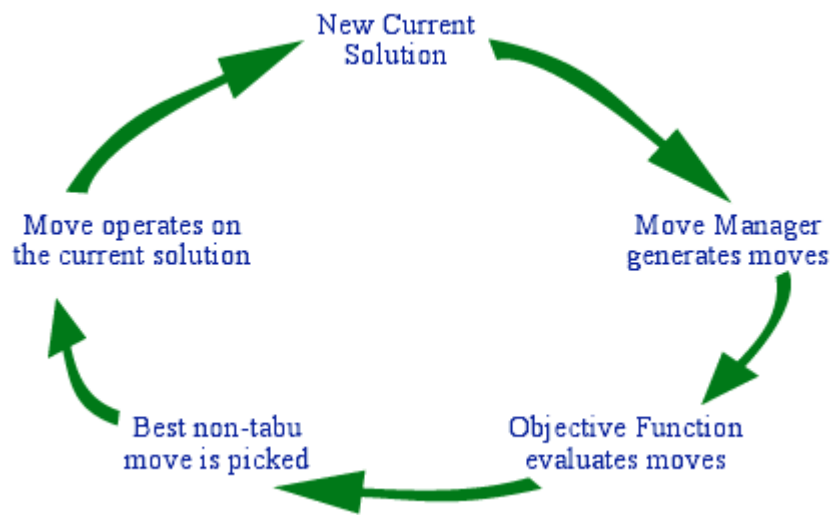


Figure 11: One Iteration of OpenTS (Harder, 2002)

4.4.2 The ATS with Intensification.

This section on ATS with intensification begins by defining the elements that drive the search process. The ATS maintains two elite lists of size five; one for the best feasible solutions and one for the best near feasible solutions found throughout the search. The elements in these elite lists are ordered by number of active crews first and total waiting time second. Closely related to the elite lists is the counter, *ISGS*, the number of iterations since finding a good solution, i.e., the number of iterations since updating either

elite list. The second counter used to coordinate the search is *CP*, the number of consecutive poor infeasible solutions the ATS visits.

CFIM, choose the first improving move, is the final variable defined. It is a boolean variable. When its value is true, the first improving move, as described by the move evaluation, is chosen as the best move. When its value is false, every move in the neighborhood is evaluated and the best move is chosen. For the ATS with intensification, the ATS uses *CFIM* with a true value in the early stages of the search. This is done for two reasons:

- 1) At the beginning of the search, the ATS is diversifying and therefore, seeking a larger sampling of the solution space.
- 2) When insert moves are placed first in the neighborhood and the swaps second, the likelihood of the first improving move taking the ATS to a smaller-crewed solution increases. The likelihood increases for two reasons. One, only inserts can decrease the number of active crews in a solution. Two, since the inserts are placed first in the neighborhood, the objective function evaluator finds an insert as the first improving move, if one exists, before evaluating any swaps.

Note that these four elements are not the lone drivers of the search space trajectory. Every five iterations, the search adapts the penalty weights for the solution and move evaluation equations, as described in Section 4.2.4. In addition, the neighborhoods themselves adapt to change the search trajectory, as described below.

The first phase of the ATS uses the elite lists, *ISGS*, *CP*, *CFIM*, and *CRSIN* to coordinate the search in a straightforward manner. After each iteration, the ATS attempts to update the elite lists. If either of the lists is updated, the *ISGS* is reset to zero. If neither is updated, *ISGS* increases by one. The ATS also characterizes the solution as feasible, near feasible, or poor infeasible. If the solution is poor infeasible, *CP* increases by one; otherwise, *CP* is reset to zero. If the search performs a preset number of *CP*

iterations, a value studied in Chapter VI, it identifies the search as trapped in a poor infeasible space and changes the neighborhood used to the TCRSIN. When the search returns to a near feasible or feasible solution, it changes the neighborhood back to the CRSIN.

When *ISGS* equals its preset limit, another value studied in Chapter VI, phase two intensification begins. *CFIM* becomes false, and the ATS evaluates the entire neighborhood of each incumbent solution. A restart list is then created from each solution on the elite lists. The ATS starts a new phase one-type search from each member of the restart list. *CFIM* remains false for these intensified searches. When *ISGS* equals its preset limit during phase two, the next member on the restart list is chosen until the list is exhausted. Once the list is exhausted, the ATS determines if either elite list was updated during phase two. If so, phase two is repeated; otherwise, the ATS terminates.

4.4.3 A Hybrid ATS/SPP Optimizer.

This section completes the hybrid ATS/SPP optimizer discussion. The two-phased approach is detailed, noting the similarities to the ATS with intensification scheme. The merits of this vocabulary-building approach are discussed in Chapter VI.

Phase one of the ATS/SPP hybrid is identical to the ATS with intensification. The differences occur when *ISGS* reaches its specified maximum. With the ATS/SPP hybrid, *CFIM* remains true. Changing *CFIM* to false creates very large SPPs that do not improve the overall quality of the search.

Once the *ISGS* reaches its limit, the ATS starts phase two by calling the CPLEX solver. A near feasible SPP is always solved first. This keeps the ATS/SPP moving towards smaller-crewed solution space regions. If the solution found is unique, a new phase one-type search starts from the near feasible solution produced and the solver is recalled once *ISGS* reaches its maximum. If the near feasible SPP solution is a revisit, then a feasible SPP is solved. If the solution to this problem is unique, the search restarts from the feasible solution. Finally, if the near feasible and feasible SPP problems both find previously visited solutions, the ATS/SPP terminates.

In conclusion, this chapter detailed the adaptive tabu search and vocabulary building methodologies developed in this research. The next chapter describes the flight schedule generator created during this research. This generator allowed creation of the flight schedules needed to conduct the analysis of the ATS in Chapter VI.

V A JavaTM-based Flight Schedule Generator

This chapter describes the flight schedule generator developed in this research. The first section discusses the motivation for creating the generator. The second section describes the components of the generator. The final section details the algorithm used to create flight schedules. Appendix A details the JavaTM framework for the generator and Appendix B shows how to use the generator to create a small example schedule.

5.1 Motivation

The most basic component of any air crew scheduling problem is the flight schedule. Unfortunately, it seems to be the problem's most ignored component in the literature. The rules for generating the flight schedules are usually well documented, but no benchmark flight schedules exist. Maybe this is due to the airlines desire to keep their own schedules proprietary. Instead, airline crew scheduling benchmarks are typically large SPPs developed heuristically from the flight schedules of various airlines (Beasley, 1990, 2002). These airline crew scheduling benchmarks are generic SPP benchmarks and do not allow comparison of algorithms that use a flight schedule as input. Even if benchmarks did exist, they likely would not allow the type of statistical analysis conducted in Chapter VI.

The goals of the flight schedule generator research are as follows:

- 1) Develop a flight schedule generator that allows efficient and rigorous analysis of the ATS.
- 2) Develop the generator so it can create any type of flying schedule, i.e., for both military and civilian applications.

3) Develop the generator so an analyst with average programming skills can reuse it.

5.2 The Flight Schedule Generator Components

The flight schedule generator is composed of four Java™ classes and three Java™ interfaces. A class is a template for an object and the object itself is an instance of a class (Schildt, 2001:130). In other words, the class defines a data type and allows you to instantiate objects of that type. Classes contain instance variables and methods that drive the behavior of any object instantiated with it.

Interfaces are similar to classes, but they do not contain instance variables, and its methods are all empty. Using interfaces allows us to set characteristics of the flight schedule generator without making prior assumptions on their implementation (Schildt, 2001: 236), i.e., the software will not run without the creation of an aircraft base network, but it does not predefine the characteristics of this network.

The various classes and interfaces that compose the generator are described below. The descriptions highlight what are important factors when developing a flight schedule. For any given scenario, only a subset of these factors may be significant. The generator, coupled with a sound statistical analysis, should allow analysts to identify this subset of significant factors.

5.2.1 Java Classes.

The four Java™ classes contained in the generator drive the flight scheduler. Although they provide information useful to users, no extensions or modifications are required for their implementation. A discussion of each follows.

Aircraft Pool.

The Aircraft Pool class models the aircraft used to fly the flight schedule. Throughout the scheduling process, the Aircraft Pool maintains a record of where each aircraft is located and when each aircraft is ready to depart for its next mission. A user may choose to populate the pool with aircraft, but this is not a requirement. When unmodified, the pool creates aircraft as needed and assigns unique identification numbers to them.

Day Of Schedule.

The Day Of Schedule class tracks time for the flight schedule generator. This class allows users to model dynamic flight scheduling, such as periods of surge operations and down days due to poor weather.

Schedule.

The Schedule class models the flight schedule itself, the fundamental input to the crew scheduling process. The flight schedule is maintained in a Java™ array list, and methods are provided to add/delete flights from the schedule.

Flight Scheduler.

The Flight Scheduler class provides the engine for the flight schedule generator. It contains the algorithm used to generate a schedule, and writes the flight schedule produced each iteration to output files.

5.2.2 Java Interfaces.

The three Java™ interfaces detailed below are vital to the flight schedule generator. They define empty, abstract methods that the user must override when implementing an interface. The interfaces allow the generalization of the generator. By overriding the

abstract methods, users create flight schedules representing their own scenario. The characteristics of the schedule may be as simple or complicated as the user desires.

Rotation.

The Rotation interface models an aircraft rotation, defined as a series of flights ending with a required period of aircraft rest. By creating these rotations, the generator constructs the aircraft schedule. Users must define a rotation's length, home base, departure time, and return base.

The rotation length is the number of flights contained within each rotation. This value may be probabilistic, i.e., probability of being length one may be 0.75 while the probability of being length two may be 0.25. Rotation lengths may also vary depending on the day of schedule.

The home base is simply the rotation's base of departure. This base must be contained within the network defined below. The departure time fixes the time at which the rotation leaves the home base. The generator provides significant flexibility in modeling departures. For example, departures could be uniform over the entire day or could be clustered in a particular time frame, i.e., military analysts could model a schedule of nighttime operations between 0000 and 0400 hours. The return base variable provides the rotation's base of termination. It is common for aircraft to return to their base of departure, but it is not required for this generator. For example, aerial refueling schedules may be created with rotations departing base A and terminating 10% of the time at base B.

In addition to the individual rotation characteristics, users must provide a method to determine the number of rotations to be initiated each day. This allows modeling

phenomena such as the early surge in military deployment schedules or weekday/weekend operations in civilian aircraft schedules.

Finally, aircraft down time must be modeled. This variable represents the amount of time an aircraft must rest before it begins another rotation. It allows modeling situations such as routine aircraft maintenance and overnight commercial stops.

Flight.

The flight interface models an individual aircraft flight, defined as a departure and arrival of an aircraft, with some quantity of flying time defined between the events.

Users must define a flight's extension time, arrival base, and aircraft turn time.

Obviously, there exists a flight time between two bases. The flight time extension models deviations from this base-to-base flight time. The deviations could represent things such as refueling time for USAF tankers, time added due to no fly zones between two bases, or bad weather conditions occurring during the flight.

The arrival base variable provides the identification number of the landing base for each flight. No method is provided to determine departure bases because they are already defined by the problem structure. The rotation object initiates the departure base of the first flight. The flight object tells this first flight where to land. Once the arrival base is set, the departure base is determined by geography, i.e., an aircraft must depart from where it arrived.

Finally, users must define aircraft turn times. These times represent the amount of time it takes to turn an aircraft after a flight and prepare it for its next flight. For example, in a civilian airline schedule, time is needed to unload the passengers, clean the cabin, and then load the new set of passengers.

Base Network.

This interface models the network in which the aircraft operate. Users must define the base network in a two-dimensional integer array containing the flying times between the bases.

5.3 The Flight Schedule Generator Algorithm

Figure 12 shows the flow of the algorithm used to generate flight schedules. The algorithm starts the iteration by generating the base network, creating the aircraft pool, and initializing the day of schedule counter to zero. Next, the day of schedule counter is incremented by one. The number of rotations generated on day i is determined and an array of departure times ordered from smallest to highest is created.

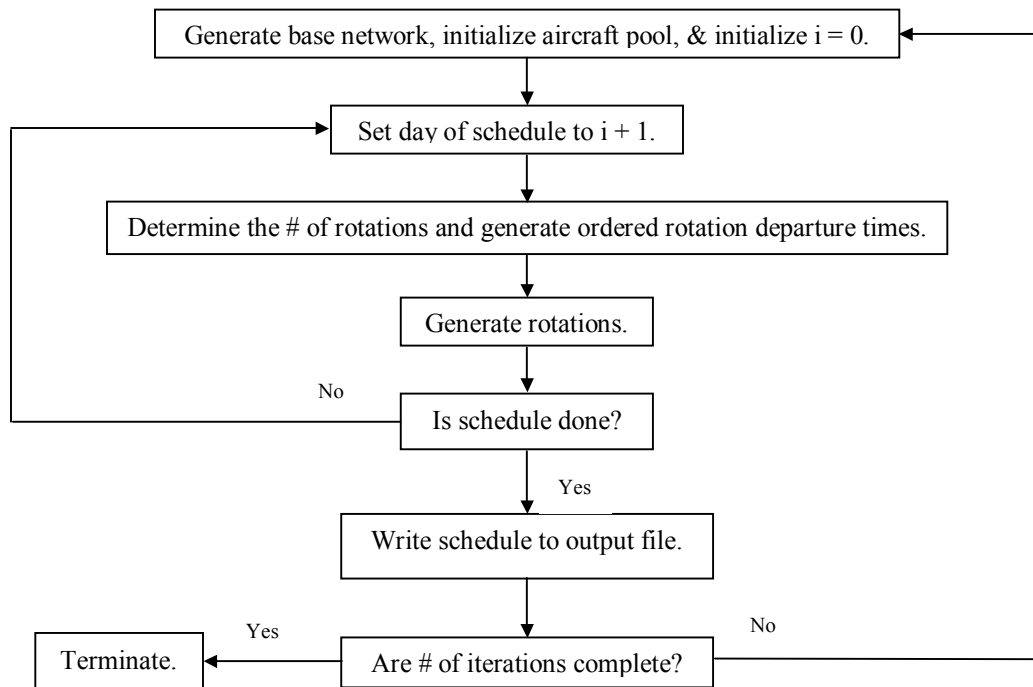


Figure 12: Generating the Flight Schedules

Next, the algorithm generates the rotations, a process described in Figure 13. Once the rotations for day i are generated, the algorithm determines if the schedule is done. If not, it moves to the next day of the schedule and creates additional rotations. If the schedule is done, it writes the schedule to the output file. Finally, it determines if the number of schedules to be generated is satisfied. If so, the generation process is terminated. If not, it repeats the process for the next iteration.

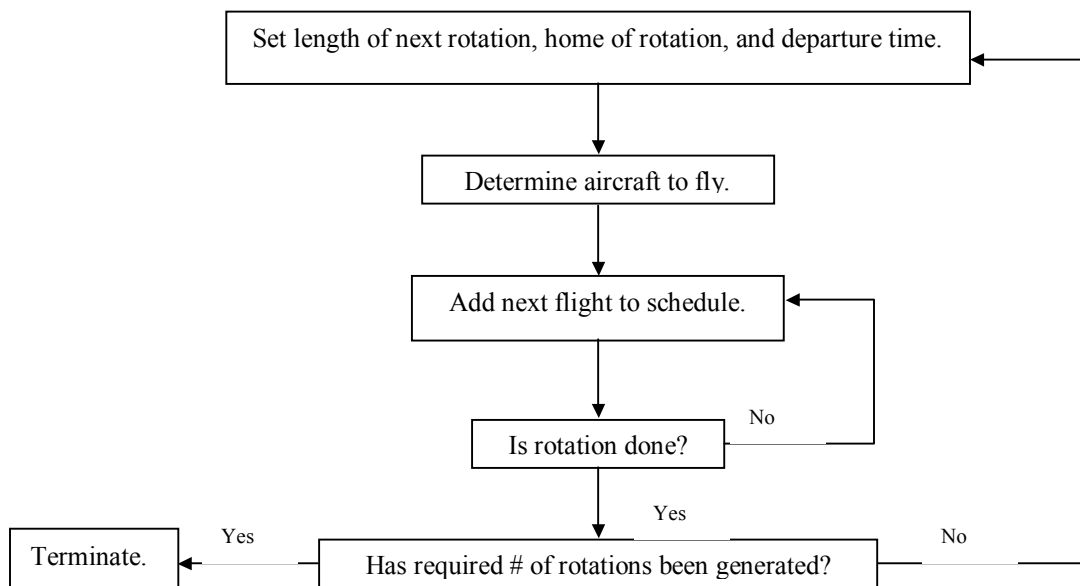


Figure 13: Generating Aircraft Rotations

Figure 13 shows the flow of the algorithm used to generate the aircraft rotations. The algorithm first sets the length of the rotation, the aircraft's home, or departure base, and its departure time. It queries the aircraft pool to choose the aircraft to fly the rotation. It begins adding flights to the rotation using the methods available in the Rotation and Flight interfaces. With the addition of each flight, the algorithm determines if the

rotation is complete. If not, it continues to add flights. If so, it determines if the number of rotations to be generated on this day is complete. If a sufficient number of rotations have been generated, the process terminates. Otherwise, the algorithm moves to the next rotation and continues.

In conclusion, this research created the first generalized flight schedule generator. Now there exists a mechanism by which researchers can compare their competing air crew scheduling algorithms. The generator is used extensively in conducting the analysis presented in Chapter VI. Without the generator, this type of systematic analysis would have been time prohibitive.

VI Analysis of the ATS and Experimental Results

This chapter analyzes the performance of the ATS search process. The first section discusses the objectives for the analysis. The second section describes the experimental design used for the analysis. A discussion of the IP lower bounds used to measure the effectiveness of the ATS follows in the third section. The fourth section discusses the experimental results, to include comparison of the ATS solutions to the lower bound. It provides, through solution space enumeration, optimal solutions to a few smaller TCSPs. These solutions are compared to the ATS solutions to further illustrate the excellence of the ATS process. It concludes by demonstrating the performance of the ATS on a large TCSP.

6.1 Objectives

Before beginning any computational study, it is important to clearly state the objectives of the experimentation. These objectives help define the study's variables of interest, and help determine the type of data that should be collected on important performance measures. From this point forth, we refer to the variables of interest as factors and the performance measures as responses.

This said, the objectives of the analysis completed in this chapter are as follows:

- 1) Determine how the characteristics of the TCSP affect a number of responses: the number of crews and waiting time in the best feasible and near feasible solutions, the number of iterations of the ATS required to solve the problem, the total solution time of the ATS, the number of conjugacy classes visited during the search process, the average neighborhood size built using the restricted neighborhood schemes, and the average tabu tenure used for recency-based memory.

- 2) Determine how the tabu search factors CP and ISGS affect the responses described in 1 above.
- 3) Determine which tabu tenure strategy performs best.
- 4) Determine if vocabulary building significantly improves the solution process and if so, the magnitude of the improvement.
- 5) Measure the quality of the ATS process by comparing the best solutions found to IP lower bounds for the TCSP.
- 6) Measure the quality of the ATS process by comparing the best solution found to the known optimal solution for a number of smaller TCSPs.
- 7) Demonstrate the performance of the ATS on a very large TCSP.

6.2 Experimental Design

The following section describes the experimental design used for this analysis. It begins by discussing the factors chosen for evaluation. A discussion of the responses listed in 1 and 2 above follows. The section concludes by presenting the fractional factorial design used for experimentation.

6.2.1 Design Factors.

Table 3 below lists the factors studied in this research. Notice the factors are divided into three categories: flight schedule, crew, and tabu search. The flight schedule factors relate to the underlying tanker aerial refueling schedule. Most of the factors were already described in the discussion on the problem generator. The crew factors relate to the physical tanker crews awaiting assignment. Finally, the tabu search factors correspond to the variables or components used to drive the ATS search process.

The values for the flight schedule factors were set to model two refueling scenarios. The first scenario is the deployment schedule, where assets must be taken from their home bases and escorted to the theater of operations. Wiley's aerial fleet refueling problem describes this type of scenario (Wiley, 2001). The second scenario is intratheater employments, where the tankers are within the theater of operations and support current operations through aerial refueling. For intratheater employment, the tankers are scheduled daily through the air tasking order (ATO) process.

The following flight schedule factors tell the flight schedule generator what kind of schedule to generate. *Rot/day* is the number of tanker rotations generated each day of the schedule. The two levels of the factor allow study of higher tempo operations versus lower tempo operations. *NumBases* is the number of bases in the tanker base network. Closely related to this factor is *MDIBN*, the maximum distance between any two bases in the network. The low level for *MDIBN* models a tighter base network likely to be seen in intratheater operations, while the high level models the larger networks typical of intertheater deployments. The *MDIBN* is measured by the time it takes to fly from one base to another, in minutes. *TBF* is the time between tanker flights, or the time from a tanker landing on one flight and taking off on another within a rotation. *TBR* is the time between rotations. This is the time the tanker is scheduled for rest or maintenance after it finishes a rotation. The *TBR* for this study varies between 12 and 24 hours. *RS* is the rotation size. Low rotation size models tankers returning to their base of departure to complete their rotation. Its high level allows the tankers to escort an aircraft to another base and land, typically for refueling itself, before returning to its home base. *RT* is the refueling time, modeled as a triangular distribution for this study. The low level

simulates refueling smaller aircraft or refueling a small number of aircraft. The high level simulates refueling aircraft with large fuel tanks or a large number of smaller aircraft. The final flight schedule factor is *RDT*, the departure time for each aircraft rotation. The low level of *RDT* models aircraft rotations departing uniformly across the entire 24-hour day. The high level models intensified operations, such as nighttime operations, where the aircraft depart only within a given time window. The time window for this study was 0000-0600.

Table 3: Experimental Design Factors

Source	Factor	Low	High
Flight Schedule	Rot/day	25	50
Flight Schedule	NumBases	4	8
Flight Schedule	TBF	120 min	360 min
Flight Schedule	TBR	720 min	1440 min
Flight Schedule	NumDIS	1	7
Flight Schedule	MDIBN	325 min	645 min
Flight Schedule	RS	1	75% 1 / 25% 2
Flight Schedule	RT	T(0,75,150) min	T(180,240,300) min
Flight Schedule	RDT	Uniform	Clustered
Crew	PCF	0.25	0.50
Crew	MWBF	30/120 min	60/240 min
Tabu Search	Tenure	Adaptive	# iterations completed
Tabu Search	ISGS	250	500
Tabu Search	CP	25	50
Tabu Search	Intensification/VB	Intensification	VB

The crew related factors were discussed in Chapter IV. *PCF* is the probability that a crew, during its previous 90 days, flew on any given day. The low value of 0.25 means the crew flew, on average, once every four days. The higher level of 0.50 models higher operational tempos, where the crew flew, on average, every other day. *MWFB* is the minimum time a crew must wait between flights. The low level is the minimum wait time required when a crew lands and departs in the same aircraft. The high level is the

minimum wait time required when a crew lands in one aircraft and departs in a different aircraft. For example, if the crew changes aircraft at the low level they have to wait 120 minutes between flights. If the crew did not change aircraft at the high level, they have to wait 60 minutes.

The tabu search factors were discussed in Chapter IV. *Tenure* represents the type of tabu tenure used during the ATS process. At the low level, the ATS uses the adaptive tenure scheme. At the high level, each solution visited is tabu for the remainder of the search process.

ISGS is the number of iterations between finding good solutions, or solutions that are placed on the feasible or near feasible elite list. The levels of this factor allow the study of response times for the ATS, as does, *CP*, the number of consecutive poor infeasible solutions found during the search. The goal is to determine how the ATS is affected by the length of time it is trapped in poor infeasible regions of the solution space, or by long periods of time where improved elite solutions are not found. The final tabu search factor simply describes whether the ATS uses intensification or vocabulary building. This factor is used to study the contribution of vocabulary building to the ATS search process.

6.2.2 Responses Studied.

Nine responses were listed in the discussion of the objectives of this analysis. The first four responses directly relate to the two objectives of the ATS search process, minimizing the number of crews needed to fly the schedule and minimizing their waiting time during their scheduled rotations. The four responses are the number of crews and waiting time found in the best feasible and near feasible solutions. Studying these

responses with respect to the factors described above allows determination of a variety of things. First, the flight schedule characteristics that significantly affect the two objectives can be identified. Second, the crew characteristics that significantly affect the objectives can be identified. Finally, the ATS components that affect the solution quality with regard to the objectives are identified.

The fifth response is the number of iterations the ATS ran before termination. This is a machine-independent measure used to measure the speed at which the ATS processed. As problems increase in size, the neighborhoods become larger and the time to evaluate them grows. Therefore, if either the intensification or vocabulary-building scheme decreases the number of iterations needed to find excellent solutions, the scheme improves the solution process. While developing the ATS with vocabulary building, an observation was made that CPLEX often had difficulty solving the SPPs. It is the reason that a 10-minute time limitation was placed on the CPLEX solver. This number of iterations to termination allows the study of the speed of the two ATS schemes without biasing the vocabulary building with the CPLEX difficulties. In fact, building a better SPP solver is discussed in Chapter VII as an avenue of further research. Furthermore, the number of iterations to termination allows an examination of the ATS independent of the computer processing it.

While a time-independent measure was just described, it is also useful to study the time it took to solve the generated problems on one particular machine. While the CPLEX solver may have problems with solving the given SPPs, the vocabulary-building scheme may be so influential it overcomes this limitation and reduces the total solution time, measured in seconds. Total solution time of the ATS is the sixth response studied.

The seventh response is the number of conjugacy classes visited during the search process, a measure of how quickly the ATS moves to good portions of the solution space and a measure of the diversification of the search. The conjugacy classes represent partitions of the solution space within the S_n . The number of conjugacy classes increases as the number of flights in the schedule and crews in the solution increases. It seems the ATS may respond to larger problems by increasing its diversification and visiting a larger number of conjugacy classes. But the ATS may find very good portions of the solution space in the early stages of the search, regardless of the size of the solution space. In this case, the number of conjugacy classes would remain small. This response helps to evaluate the factors that affect the ATS's movement through the solution space.

Response eight is the average neighborhood size evaluated during the search process. Since neighborhood evaluation is rather expensive, examination of this response should give further insight into why certain factors affect the total solution time. In addition, it should lend insight into the affect of the tabu search factors on the restricted neighborhood schemes.

The final response is the average tabu tenure used during the search process. This response is used to determine if the adaptive scheme, since it is biased toward preventing cycling by doubling the tenure when revisits occur, is truly different than the scheme that makes all visited solutions tabu. In addition, the effects of the flight schedule and crew factors can be measured to determine if certain characteristics of the underlying TCSP influence the tabu tenure. It could also provide further insight into the total solution time. If the adaptive scheme lowers the average tabu tenure, then a smaller list of solutions needs to be scanned for tabu status, and the solution time should decrease.

6.2.3 The Fractional Factorial Design.

There are a total of 15 factors considered in this dissertation. A full factorial design for 15 factors contains 32768 design points, or combinations of the levels of the factors. Obviously, a design of this size is impractical for the problems produced by the flight schedule factors of Table 3. Some of the problems are small, but many are large and require a significant amount of solution time. The average solution time for problems in the testing phase of this research was 36 minutes.

Since the full factorial design is impractical, attention focused on the use of a good fractional factorial design (Myers and Montgomery, 1995:140). JMP 4.0.4, a statistical software package that contains an experimental design module, was used to evaluate prospective Resolution IV designs and choose the final design (JMP, 2002).

A resolution IV fractional factorial is a design with all main effects independent of two-factor interactions, but some two-factor interactions are aliased with each other (Myers and Montgomery, 1995:172). Aliasing occurs when two factors cannot be differentiated (Myers and Montgomery, 1995:172). For example, in the final design chosen for this study, the two-factor interactions *Rot/day*NumBases* and *PCF*MWBF* are aliased. Therefore, if this aliased pair is shown to be significant for one of the responses described above, there exists no way to mathematically show which interaction is truly the important one. While there may exist no mathematical means to differentiate the two interactions, knowledge of the problem domain may lend insight into which interaction is likely significant.

Since two-factor interactions are aliased in any Resolution IV design, efforts focused on identifying a design that could evaluate the main factor effects on the described

responses while allowing for replication of the overall design. Replication was necessary because early evaluation of the TCSP showed that different randomly generated flight schedules within a particular combination of factor levels could produce significant differences in the initial and final TCSP solution.

Appendix C displays the resulting Resolution IV design used in this dissertation, along with its aliasing structure. The design contains 64 combinations or design points, with each replicated three times. The aliasing structure shows that no main effect is aliased with another effect. While there are no two-factor interactions that can be estimated freely, it is important to note that this design can be the starting point of additional analysis. It is possible to fold over Resolution IV designs to separate aliased two-factor interactions (Myers and Montgomery, 1995:172). This sequential experimentation could be completed until all significant two-factor interactions were clear from aliasing and is an area for further research.

6.3 Determining Lower Bounds for the TCSP

As noted in Chapter 2, Barr, *et al.* appreciate analysis that provides theoretical contributions such as solution quality bounds (Barr, *et al.*, 1995:12). This section describes an integer programming based approach to finding solution bounds for the TCSP. It extends an approach used to find bounds for general crew scheduling problems (Mingozzi, *et al.*, 1999: 877).

The existing bounding procedure is extended by relaxing two significant constraints in the problem definition of Mingozzi, *et al.* (1999:877). One, they assumed that M crews should be used to cover the schedule. The approach developed in this section determines

the number of crews that need to be assigned. Two, they assumed that all crews leave and return to the same home base. The approach developed here relaxes the assumption and allows tanker crews to leave home base and end a rotation at a different base.

The extended approach must make two assumptions itself to create a tractable integer program. First, the procedure assumes the crew flying histories are insignificant for the problem being bounded. This is true for the problems solved in this dissertation's designed experiment, as seen in the next section. This is a reasonable assumption because flying histories for the TCSP are not likely to be significant until the flying schedule has a much larger time horizon, such as a 30-day schedule. Bounds calculated for these much larger problems are likely to be very weak and yield little information on the power of the metaheuristic. This said, the next section shows the bounding procedure performs very well for the problems generated for this experiment. Note that by assuming insignificant crew histories, the solution associated with the bound does not assign flights to a particular crew, i.e., crew 1 must fly flights 5 and 10. Instead, the solution shows the number of crews needed to fly the schedule, i.e., one crew is needed to fly flights 5 and 10.

Second, the bounding procedure assumes a pair-wise examination of the flights is sufficient for building the duty day structure of a rotation. By viewing flights pair-wise, there is no need to enumerate all feasible duty days.

With these assumptions in mind, a graph-based view of the TCSP is used to develop the bounding procedure. Suppose there exists graph $G(\mathbf{V}, \mathbf{A})$, where $\mathbf{V} = \{0, 1, \dots, n\}$ is the set of $n + 1$ vertices and \mathbf{A} is a set of directed arcs. Vertex 0 of \mathbf{V} is an artificial vertex representing the start of a flight schedule and the remaining vertices represent the flights

that must be flown. \mathbf{A} contains all arcs $(0,i)$ for $i \in \mathbf{V} - \{0\}$. The remainder of \mathbf{A} consists of all arcs (i,j) , $i,j \in \mathbf{V} - \{0\}$, that satisfy the following constraints:

- 1) The departure base of j = the arrival base of i .
- 2) The *MWBF* is satisfied for flights i and j .
- 3) Flights i and j may be flown in the same duty day or there exists sufficient crew rest between flights i and j .

Given $G(\mathbf{V},\mathbf{A})$, the integer program used to find the bounds for the two TCSP objectives is formulated as follows:

Equation 10: Integer Program Used to Calculate TCSP Lower Bounds

$$\begin{aligned} & \text{Min } \sum_{(i,j) \in \mathbf{A}} c_{ij} x_{ij} \\ \text{s.t. } & \sum_{i \in \mathbf{V}} x_{ij} = 1, \quad j \in \mathbf{V} - \{0\} \end{aligned} \quad (1)$$

$$\sum_{j \in \mathbf{V} - \{0\}} x_{ij} \leq 1, \quad i \in \mathbf{V} - \{0\} \quad (2)$$

$$x_{ij} \in \{0,1\}, \quad (i,j) \in \mathbf{A} \quad (3)$$

where $x_{ij} = 1$ if the optimal solution contains arc $(i,j) \in \mathbf{A}$

w_{ij} = wait time associated with arc (i,j) , in minutes,

$$c_{ij} = \begin{cases} w_{ij} + Z, & i = 0 \\ w_{ij}, & \text{otherwise} \end{cases}, \text{ and } Z \text{ is a large positive integer.}$$

Constraint (1) states that only one arc may enter each flight vertex in the graph.

Constraint (2) states that at most one arc may leave each flight vertex in the graph. If an arc does not leave a flight vertex in the graph, then the flight represents the termination point of a crew rotation. Constraints (1) and (2) together ensure that each flight is assigned to only one crew.

The definition of c_{ij} allows the simultaneous optimization of both objectives (Mingozi, *et al.*, 1999: 874). Every c_{ij} contains the wait time associated with the arc

(i,j) , and the Z value added to the cost of each arc leaving vertex 0 forces the optimizer to use the smallest number of crew rotations possible. A Z value of $1.0 \cdot 10^9$ was used for this study.

Appendix F shows the solution bound for design point 1. It is clear that only 13 arcs leave vertex 0; therefore, the lower bound for required crews is 13. Furthermore, the total cost of the objective function is $1.3000011980 \cdot 10^{10}$. Thus, the waiting time bound is calculated as $1.3000011980 \cdot 10^{10} - 13 \cdot 1.0 \cdot 10^9 = 11980$ minutes.

6.4 Experimental Results

The following section presents the results for the experimental design discussed in Section 6.2. The discussion has two parts. Part one examines the factor effects on the various responses previously discussed. Part two measures the quality of the ATS solutions by comparing them to lower bounds calculated with the approach discussed in Section 6.3.

6.4.1 Examination of the Factor Effects.

Appendix G contains the analysis of variance (ANOVA) calculations for the nine responses studied in this dissertation. To determine the significant factors for each response, the following hypothesis test was conducted for each mean effect e_{ij} , where i is an element of the set of design factors and j is an element of the set of responses:

Equation 11: Hypothesis Test for Factor Effects

$$H_0 : e_{ij} = 0$$

$$H_1 : e_{ij} \neq 0$$

The p-value of each e_{ij} was used as the test statistic for the hypothesis test. It is a standard test statistic and is defined as follows:

The p-value is the smallest level of significance, α , at which H_0 would be rejected when a specified test procedure is used on a given data set. Once the p-value has been determined, the conclusion at any particular level α results from comparing the p-value to α :

- 1) p-value $\leq \alpha \Rightarrow$ reject H_0 at level α .
- 2) p-value $> \alpha \Rightarrow$ do not reject H_0 at level α . (Devore, 1991:315)

Analysis of variance was used on each data set, hence the p-value relates to a standard F-test conducted for each factor/response combination. An α value of 0.05 was used for all hypothesis tests performed in this research.

Table 4 shows the mean effects of each design factor with respect to the number of crews and total waiting time (WT) in the ATS's best feasible (F) and best near feasible (NF) solutions. Table values of X indicate that H_0 above was not rejected, hence the factor was found to be insignificant for that particular response.

It is clear that, for the TCSP's two objectives, the characteristics of the flight schedule dominate the solution. Especially significant are the number of rotations generated each day and the length of the schedule. This is to be expected--longer schedules and higher operational tempos require more crews and increase the amount of wait time for those crews.

As the maximum distance in the base network and refueling times increased, so did the number of crews required and the waiting time of the crews. This appears to be a function of crew reusability. The increased distances and refueling times create longer

refueling flights; hence the crews are busy for longer periods of the duty day and cannot be assigned to other flights.

The rotation departure time also has a notable effect on the two objectives. When the rotation departure time is clustered, it significantly tightens the schedule. Crews cannot be reused because there are a large number of flights taking off in the same time period. Since rotation departures are clustered, the waiting time increases because once a crew completes their duty day, operations do not restart until 0000 hours the next day. When departures are uniform throughout the day, the crews are reused more quickly and their waiting time on the ground is reduced.

PCF is insignificant for all the responses. This supports the intuition that crew flying histories will likely not affect the two objectives until the flying schedules examined are larger, i.e. 30+ day schedules.

The type of tabu tenure used and the value for the ISGS counter do not significantly affect the ATS solutions, but the higher value for the CP counter increases the total waiting time in feasible and near feasible ATS solutions. This is to be expected. When the search trajectory becomes severely entrenched in areas of poor infeasibility, it is difficult to escape and the ATS must use the TCRSIN for a larger number of iterations. This targeted neighborhood directs the trajectory toward feasibility, but in the process, it appears to hinder the model's ability to find the better waiting time solutions. The obvious solution is to use the low CP value and not allow the trajectory to delve so deeply into areas of poor infeasibility.

Finally, the intensification scheme performs as well as the ATS with vocabulary building for all responses but the total waiting time in near feasible solutions. The main

contribution of the vocabulary building scheme is its ability to solve the TCSP much more quickly than the ATS with intensification, as discussed below.

Table 4: Factor Effects for the TCSP objectives

Factor	ATS F Crews	ATS NF Crews	ATS F WT	ATS NF WT
Average Value	40.151	37.557	165491	156037
Rot/day	21.302	19.990	81514	78895
NumBases	5.781	5.302	27520	25023
TBF	X	X	X	X
TBR	X	X	X	X
NumDIS	19.177	18.740	302248	286065
MDIBN	1.823	2.198	X	X
RS	7.802	7.219	31964	28913
RT	10.177	10.656	29776	31765
RDT	12.073	11.656	26500	26197
PCF	X	X	X	X
MWBF	3.990	4.865	19046	23645
Tenure	X	X	X	X
ISGS	X	X	X	X
CP	X	X	18608	17086
Intensification/VB	X	X	X	-15546

With a discussion of the two TCSP objectives complete, the remainder of this section examines the affect of the design factors on various ATS performance measures. Table 5 displays the mean effects for each of the factors.

As seen for the TCSP objectives, many of the ten flight schedule factors significantly affect tabu search performance measures such as total solution time and the number of conjugacy classes visited. When the number of daily rotations generated and number of days in the schedule increase, the size of the resulting flight schedules increases. Table 5 shows that as the size of these flight schedules increase, there is more opportunity to improve the initial solution and the number of iterations and the total solution time increases.

As the flight schedule sizes increase, the size of the solution space, S_n , increases. The ATS appears to respond to an increased solution space size by increasing the tabu tenure. This limits cycling and forces the search to different parts of the solution space. This increase in diversification corresponds to visiting a larger number of conjugacy classes.

Notice that clustering rotation departure times decreases the values of all tabu search responses but the average neighborhood size. This supports the intuition that flight schedules with clustered departures are much tighter, meaning there is much less opportunity to improve the initial solution. In effect, the clustered departure times prune a significant portion of S_n from consideration. This solution space reduction is seen as a large decrease in the number of conjugacy classes visited. Since the ATS does not diversify often, it terminates sooner, decreasing the number of iterations and total solution time. The number of iterations completed bounds the tabu tenure, i.e., if 10 iterations have been completed, the tabu tenure is effectively 10 at the high level. Therefore, decreasing the number of iterations decreases the average tabu tenure.

The tabu search factors *ISGS* and *CP* significantly affect the ATS performance. As *ISGS* increases, the number of iterations and total solution time increases, as does the average tabu tenure. This larger average tabu tenure indicates that the ATS tends to cycle when the solution does not improve for long periods of time. Note that this increase in computational cost comes with no improvement in the two TCSP objectives.

When the search is permitted to stay in areas of poor infeasibility too long, the number of conjugacy classes visited severely decreases. The search becomes trapped in a smaller region of the solution space. This seems to explain the degradation of the total waiting time in feasible and near feasible ATS solutions at the high *CP* level.

Vocabulary building clearly improves the performance of the adaptive tabu search developed in this research. It is the most significant factor with respect to the number of iterations completed, reducing termination by 8459 iterations. This is over twice the magnitude of the next most significant mean effect. While CPLEX took a significant amount of time to solve the vocabulary building SPPs, the strategy worked so well that it overcame this limitation and still reduced the TST by over 28 minutes. This is very significant considering the average TST is approximately 36 minutes. Where the intensification scheme forces the ATS to traverse a large number of conjugacy classes to find good solutions, vocabulary building avoids these classes and moves rapidly to excellent areas of the solution space.

Table 5: Factor Effects for Number of Iterations, Total Solution Time, Number of Conjugacy Classes Visited, Ave Neighborhood Size, and Ave Tabu Tenure

Factor	Iterations	TST	Num CC Visited	Ave NS	Ave Tabu Tenure
Average Value	6089	2149.1	895.6	1822.3	2541
Rot/day	2207	2832.8	X	1887.5	1031
NumBases	X	X	X	-439.8	X
TBF	X	X	X	X	X
TBR	X	X	X	X	X
NumDIS	3845	4103.8	1742.9	2643.3	1339
MDIBN	X	X	X	117.3	X
RS	X	X	395.9	X	X
RT	X	X	-470.3	X	X
RDT	-1980	-1299.1	-705.5	X	-760
PCF	X	X	X	X	X
MWBF	X	X	X	X	X
Tenure	X	X	X	X	737
ISGS	3721	1039.9	X	X	1474
CP	X	X	-544.1	X	X
Intensification/VB	-8459	-1687.5	-642.2	X	-4116

As discussed in Section 3.3, Hooker suggests that once controlled experiments are run over a variety of parameter settings and the effects of the parameter settings examined,

the choice of levels should be clear (1995:40). This appears true for the ATS developed in this research.

Clearly, vocabulary building should be used within the ATS framework. At the high level, *ISGS* increases computational time while providing no improvement in finding good feasible or near feasible solutions. Thus, *ISGS* should be set to the low level of 250. While the values for *CP* do not affect computational time, they clearly hinder the performance of the ATS by terminating at solutions with increased waiting time. Therefore, *CP* should also be set at the low level. Finally, either tabu tenure scheme appears robust and could be implemented.

6.4.2 Comparing the ATS Solutions to Lower Bounds.

To measure the quality of the ATS solutions, the following section examines the number of assigned crews and total waiting time for the initial and best feasible ATS solutions with respect to the lower bounding scheme developed in Section 6.3. The starting solutions are examined for two reasons:

- 1) To show that the initial heuristic finds good solutions.
- 2) To examine the amount of improvement gained by implementing the ATS.

The performance measure used is the percentage distance from the respective bound:

Equation 12: Calculating % Distance from the Lower Bound

$$\% dist_{ij} = \frac{(actual\ value_{ij} - bound\ value_j)}{bound\ value_j},$$

where $i \in \{ATS\ Solution, Starting\ Solution\}$,
 $j \in \{Number\ of\ Crews, Total\ Waiting\ Time\}$.

Appendix E contains the data on the respective *% distance* calculations. In addition to reducing the *% distance* as compared to the starting solution, the ATS solutions are much less variable. Table 6 below summarizes the data on the average and standard deviation for each respective *% distance*.

The heuristic used to create starting solutions for the ATS appears to create good initial solutions. It provides solutions, on average, within 7.71 of the crew bound and within 13.51 percent of the waiting time bound. The ATS does an excellent job of improving these solutions. With respective percentage distances of 3.78 and 5.03, the ATS reduces the distance from the crew bound by more than half and reduces the distance from the waiting time bound by nearly 63%. In addition to reducing the mean *% distance*, it is clear that the ATS solutions are much less variable as well, nearly halving the standard deviation in each TCSP objective.

Table 6: Ave and Standard Deviation for % Distance with Respect to the Lower Bounds

	ATS Num Crews	ATS Wait Time	Starting Num Crews	Starting Wait Time
Ave % dist	3.78	5.03	7.71	13.51
SD % dist	5.82	7.27	10.58	14.35

The table in Appendix E shows many instances where the ATS solution matches the lower bounds on number of crews and total waiting time. Since all ATS solutions shown are feasible, and the lower bounds show that no smaller crew or waiting time solution exists, these ATS solutions are optimal. Indeed, the ATS can be shown to find the optimal solution for nearly 40% of the problems solved in the designed experiment.

The lower bounding scheme does not guarantee that the bound found is a feasible solution. The ATS may be finding optimal solutions although its solution does not match the lower bounds. Therefore, the 40% optimality described above is a lower bound on the percentage of problems for which the ATS finds the optimal solution. The next section identifies design points where the ATS solution does not match the lower bound but is the optimal solution.

6.4.3 Comparing ATS Solutions to Known Optimal Solutions.

The following section examines a number of smaller TCSPs. These problems allow enumeration of all feasible crew rotations. For each problem, the known optimal solution is found by solving two SPPs, with each feasible crew rotation a column of the SPP. The first SPP minimizes the number of crews in the solution. The number of crews in the optimal solution to the first SPP is added as a constraint to the second SPP, which minimizes total waiting time.

Forty-four of the problems in the experimental design are small enough to find the optimal solution. Appendix H summarizes each design problem's *% distance* from the optimal solution, and indicates whether the ATS solution is optimal or sub-optimal. This is calculated as in Equation 12, but the bound value is replaced by the optimal value. The results show that the ATS finds the optimal solution to 40 of the 44 problems. The 40 optimal ATS solutions are not shown to be optimal by the lower bounds. Therefore, adding them to the previous list of known optimal solutions, the ATS finds the optimal solution for nearly 60% of all problems in the experimental design.

Of course, the ATS is a metaheuristic and is not guaranteed to find the optimal solution. Table 7 below summarizes the results for the four problems out of 44 where the ATS solution is not optimal. The results show the ATS still found excellent solutions. The average % *distance* from the optimal number of crews and optimal waiting time is only 0.86% and 1.00%, respectively.

Table 7: Summary of Four Sub-optimal ATS Solutions in the Experimental Design

Design Point	Optimal # Crews	Optimal Wait Time	ATS # Crews	ATS Wait Time
101	26	21321	26	21352
102	25	25094	25	25342
121	30	23102	30	23232
134	29	27503	30	28138

While the ATS performed well for the problems found in the designed experiment, a natural follow-on question is, “How will the ATS perform on a problem found outside the design space or a problem of significantly larger size?” The next section addresses this issue.

6.4.4 Solving a Very Large TCSP.

The following section discusses the ATS performance on a very large TCSP. The problem simulates a 30-day deployment scenario. The deployment surges in the first week, generating 40 rotations each day. The tempo slows for the remainder of the schedule, generating only 15 rotations per day for the last three weeks. Table 8 displays a complete listing of the problem characteristics. The resulting schedule contains 1269 flights. This schedule is three times the size of the largest schedule in the experimental

design, and over 11.5 times the size of the schedule produced by Wiley’s largest deployment scenario (Wiley, 2001).

Table 8: Characteristics of a Large Deployment Operation

Factor	Value
Rot/day	40 1 st week, 15 weeks 2-4
NumBases	8
TBF	60 min
TBR	360 min
NumDIS	30
MDIBN	485 min
RS	25% 1, 50% 2, 25% 3
RT	T(180,240,300) min
RDT	Uniform
PCF	0.50
MWBF	60/240 min

An ATS with vocabulary building scheme is used to solve the problem. *ISGS* is set to 250, *CP* to 25, *PCF* to 0.50, and the *MWFB* to 60/240 minutes. The ATS produces a feasible initial solution with 118 crews and 3334175 minutes of total waiting time.

Figure 14 shows the progress of the ATS with respect to minimizing the number of crews in a feasible solution. Figure 15 shows the progress with respect to minimizing total waiting time. The square boxes on the graphs represent points of vocabulary building. At the beginning of the search, little progress is made in terms of the number of crews in the solution, but total waiting time of those crews is being reduced significantly.

By iteration 365, about 27 minutes after starting the solution process, a feasible solution with 3087760 minutes of waiting time is found. This is a 7.4% reduction in waiting time, a savings of 246415 minutes or about 171 days.

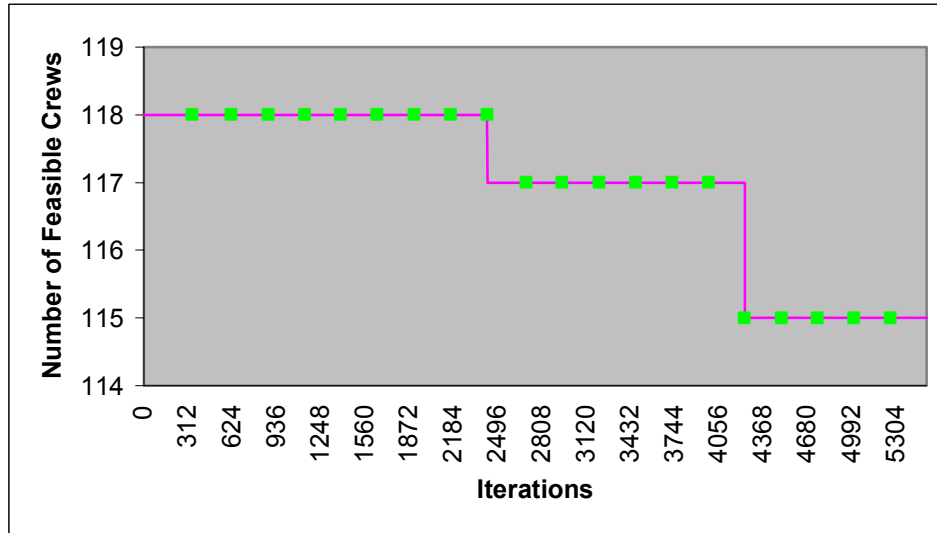


Figure 14: Finding the Smallest Feasible Number of Crews in a Large TCSP.

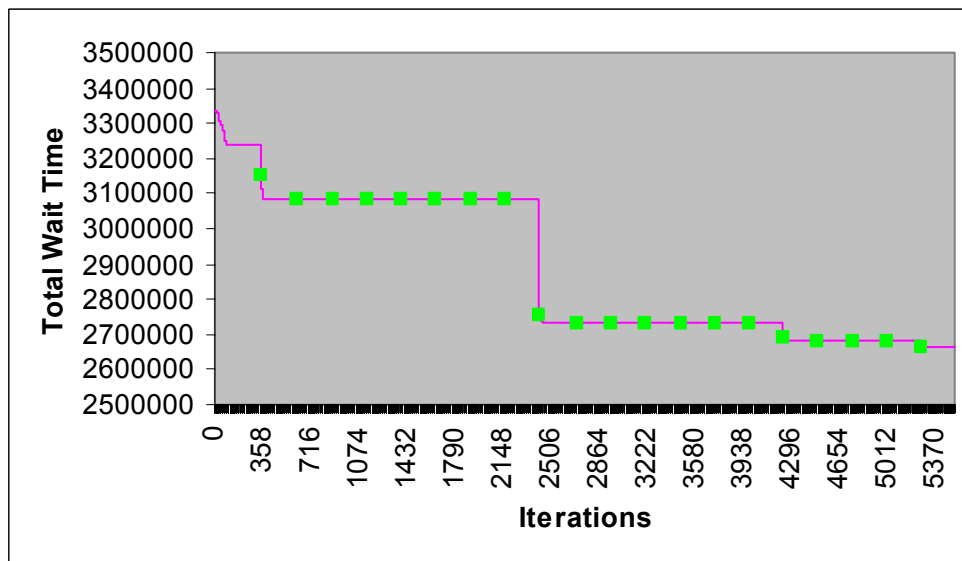


Figure 15: Finding the Smallest Total Wait Time in a Large TCSP.

At this point, the ATS seems to stall and no crew or waiting time improvements are made for a long period of time. But the ATS does not terminate at any time during this stretch because the vocabulary building continues to improve the best near feasible

solutions. At iteration 2421, about 3.5 hours into the solution process, vocabulary building sends the trajectory of the search into a significantly better portion of the solution space. A 17 crew feasible solution is found in the next neighborhood evaluation. The total waiting time of this solution is 2754589. At this point in the search, total waiting time has been reduced by 17.38%, a savings of 579586 minutes or about 402 days.

The ATS continues to improve the solution until at iteration 5263, the best solution is found by solving a SPP. The best solution has 15 crews and 2667124 minutes of total waiting time. This is a savings of 3 crews and a reduction in total waiting time of 20%, a savings of 667051 minutes or about 463 days! The ATS terminates 255 iterations after finding the best solution. The total solution time is just over 8 hours.

In conclusion, this chapter met all its objectives. It examined various factors of the TCSP and ATS to determine their effects on solution quality and ATS performance. It clearly showed the effectiveness of embedding SPP-based vocabulary building within the ATS. It then provided a lower bounding scheme to measure the quality of ATS solutions. It compared ATS solutions to known optimal solutions, supporting the excellence of the approach. Finally, it showed the effectiveness of the ATS on a large-scale deployment schedule.

VII Concluding Remarks

This chapter details the major contributions of this research and discusses future avenues of research for the TCSP and the methodologies developed.

7.1 Major Contributions

This section discusses the many contributions produced by this research. It begins by discussing the contributions to the general operations research community and concludes by discussing the various USAF contributions.

7.1.1 Operations Research Contributions.

This research presents the first metaheuristic approach to the complete air crew scheduling problem. It simultaneously pairs flights and rosters them to individual crews. Although the excellence of the tabu search approach has been shown with application to tanker crew scheduling, FAA and airline rules and objectives could be substituted for the Air Force regulations and objectives to obtain a tabu search suitable for their needs. Furthermore, the methodology can be extended to any scheduling problem that requires a time-dependent assignment of one set of resources to another set of resources. The underlying theoretic tabu search mechanisms remain identical.

This research presents the first use of dynamic, integrated, set-partitioning based, vocabulary building within a metaheuristic search. The effectiveness of the integrated vocabulary builder within the adaptive tabu search has clearly been shown. This methodology can be extended to any problem that has an underlying set partitioning or set covering solution structure.

This research defined and created the first general flight schedule generator. This new generator will allow future researchers to create benchmark data sets when studying their air crew scheduling problems. The generator allowed the creation of the benchmark data set used to conduct a statistical analysis of our ATS, an area routinely ignored by other researchers. This analysis included the development of integer programming-based lower bounds that helped measure the quality of the ATS process.

This research demonstrates the effective use of group theory as a tabu search foundation. It shows group theory provides an excellent solution structure for combinatorial problems such as the TCSP. It develops effective solution and conjugacy class hash functions. It demonstrates the effectiveness of template-based inserts and conjugation-based swaps. Finally, it provides a new measure of tabu search diversification by using conjugacy class frequency information.

7.1.2 USAF Contributions.

The methodology developed in this research provides a rigorous analytic foundation for determining the number of crews required to fly aircraft schedules, as opposed to the back-of-the-envelope calculations so often used. Air Force analysts can develop a variety of scenarios and determine crew ratios using the ATS or ATS/SPP hybrid.

The ATS provides a means for air mobility analysts to conduct deeper analyses. In addition to answering questions on the number of crews required, they can also study problems such as:

- 1) How does operations during peace affect our crew operations during war?
- 2) How should crews be distributed within a base network to most effectively utilize them?

Besides peacetime planning, the tool can be used during operations. Given an air refueling schedule, the ATS provides a good crew schedule. Within an air operations center, crew schedulers could use the tool to answer “what if” questions like: Is the air refueling schedule produced feasible given the flying history of our crews? Coupled with an air refueling scheduler, it should allow a more intense flying schedule or detect severe risks in the given schedule. Finally, the tabu search is easily extended to other Air Force problems, such as scheduling crews for the airlift community.

7.2 Avenues for Future Research

While completing this research, many future avenues of research appeared. This section provides a description of these avenues.

A novice programmer created the Java™ code for this research. While it finds excellent solutions in a reasonable amount of time, there likely are inefficiencies to be found in the code. An in-depth analysis by an expert programmer could uncover such and reduce solution times.

During vocabulary building, as the set partitioning problems become large, the time to solve the SPP portion of the problem begins to overwhelm the search. The ten-minute solution time limit is routinely reached by CPLEX, and heuristic solutions are ultimately produced. Research should be conducted to find a faster SPP solver within the hybrid scheme. One alternative may be to embed a SPP metaheuristic solver within the hybrid. A second would be to examine a previously developed large-scale SPP solver and develop Java™ wrappers or a Java™ version of it.

The ATS uses a relatively simple insert and swap neighborhood to conduct its search. This neighborhood performed excellently, but follow-on research could examine the utility of implementing more complicated neighborhoods. Future research could also examine other adaptive tabu search schemes, or extend the adaptive scheme to the reactive tabu search developed by Battiti and Tecchiolli (1994). It would be interesting to compare the reactive tabu search to the ATS with vocabulary building, and to study whether or not vocabulary building increases the effectiveness of the reactive tabu search.

This research directly follows Wiley's Aerial Refueling dissertation (2001). Wiley's tabu search provides the tanker refueling input for our crew scheduler. The two tools produced by these efforts need to be combined. One solution is a sequential approach where the aerial fleet refueling problem is solved, feeds the resulting schedule to the crew scheduler, and the TCSP is solved. An alternative approach is to solve the aerial fleet refueling problem and TCSP simultaneously. The objectives and constraints of each problem could be combined to form a larger problem suitable for metaheuristic search. The combined problem may yield solutions unattainable by the sequential approach.

This research focused on solving the TCSP. The ATS approach developed can clearly be applied to other USAF flying communities. Demonstration of this would be beneficial, along with further extension to the airlines' crew scheduling problem.

Extensions can be made to the flight schedule generator. For example, to generate random variates from different probability distributions, users have to rely on outside JavaTM objects. Embedding such a probability class within the generator itself would alleviate the need for this.

7.3 Conclusions

This research contributes significantly to the operations research community. It provides the first metaheuristic approach for solving the complete air crew scheduling problem. This methodology can be extended to other crew scheduling problems. It provides the first dynamic, integrated, set-partitioning based vocabulary building scheme. This vocabulary building methodology may be exploited by other problems that have underlying set partitioning or set covering solution structures. It provides a general, reusable flight schedule generator. The research highlights the insights to be gained when conducting statistical analysis on metaheuristics. Finally, it opens many avenues for future research. Future researchers should be able to extend the methodologies provided and build better approaches to other combinatorial problems.

APPENDIX A: Java™ Components of the Flight Schedule Generator

Java Classes

The four Java™ classes described below drive the flight scheduler. Although they provide information useful to users, no extensions or modifications are required for their implementation. They are structured as follows:

1. AircraftPool. This class models the aircraft that fly the flight schedule.
 - a. Constructor: AircraftPool().
 - b. Instance variable: aircraftPool, a TreeMap that contains the aircraft identification number as the key, and the aircraft's current base location and current time availability pair as the value.
 - c. Public methods:
 - i. initializePool(): places one aircraft in the pool, available from any base immediately, with identification number zero. Once the pool is initiated, the user may populate it with aircraft of his choice. Otherwise, the generator creates new aircraft as needed.
 - ii. getNextAvailableAircraft(int departureBase, int departTime): given an upcoming rotation departure, this method assigns the first available aircraft.
 - iii. updatePool(int aircraftID, int baseLocation, int newAvailableTime): updates an aircraft's location and time availability.
 - iv. getAircraftPool(): returns the existing aircraft pool;
 - v. setAirCraftPool(TreeMap tempAircraftPool): sets the aircraft pool to the temporary pool value specified.
 - vi. writePool(): writes the aircraft pool to the monitor.
2. DayOfSchedule. This class tracks time for the flight schedule generator and allows dynamic flight scheduling, i.e., modeling surges, down days due to weather, etc.
 - a. Constructor: DayOfSchedule(int lengthOfSchedule).

- b. Instance variables:
 - i. dayOfSchedule: an integer that represents the current day of the schedule.
 - ii. lengthOfSchedule: an integer that represents how many days the aircraft should fly.
 - c. Public methods:
 - i. getDayOfSchedule(): allows access to the current day by any class.
 - ii. getLengthOfSchedule(): allows access to the length of schedule.
 - iii. setDayOfSchedule(int newDay): sets the flight schedule day.
 - iv. setLengthOfSchedule(int length): sets the length of the aircraft schedule.
3. Schedule. This class models the flight schedule itself, the fundamental input to the crew scheduling process.
- a. Constructor: Schedule().
 - b. Instance variable: flightSchedule, a Java™ ArrayList representing the aircraft flight schedule.
 - c. Public methods:
 - i. addFlight(int[] flight): this method adds a flight to the schedule.
 - ii. getFlightSchedule(): returns the flight schedule at any point in time.
 - iii. setFlightSchedule(ArrayList tempFlightSchedule): sets the flight schedule to the arraylist passed as a parameter.
 - iv. printToScreen(): prints the flight schedule to the monitor.
 - v. clearFlightSchedule(): clears the flight schedule, primarily used when randomly generating multiple flight schedules.
4. FlightScheduler. This class provides the engine for the flight schedule generator. It contains the algorithm used to generate a schedule, and writes each iteration to output files.
- a. Constructor: FlightScheduler (AircraftPool aircraftPool, DayOfSchedule timeKeeper, Rotation rotation, Flight flight, BaseNetwork network, Schedule flightSchedule, int scheduledDays, int numberOfIterations, String outputDirectory).

- b. Instance variables:
 - i. aircraftPool: an instantiation of the aircraft pool.
 - ii. timekeeper: an instantiation of the DayOfSchedule object.
 - iii. flightSchedule: an instantiation of the flight schedule.
 - iv. scheduledDays: an integer representing the length of the flight schedule.
 - v. numberOfIterations: an integer representing the number of flight schedules generated.
 - vi. outputDirectory: a string declaring where the output files should be placed.

The following represent instantiations of objects using the interfaces described below.

- vii. rotation: an instantiated Rotation object
- viii. network: an instantiated base network.
- ix. flight: an instantiated Flight object.

- c. Public methods: generateFlightSchedule(): this method generates the flight schedules using the generator algorithm described in Chapter V.

Java Interfaces

The three JavaTM interfaces detailed below describe the characteristics of the flight scheduler. They contain no constructors or instance variables. Instead, they simply define empty, abstract methods that the user must override when implementing an interface. The interfaces allow the generalization of the generator. By overriding the abstract methods, users create flight schedules representing their own scenario. The characteristics may be as simple or complicated as the user desires.

1. Rotation. This interface models an aircraft rotation. The following abstract methods must be overridden to implement the Rotation interface:
 - a. getRotationLength(): returns an integer representing the number of flights contained in each rotation.
 - b. getRotationHomeBase(): returns an integer representing the base of departure of the rotation.
 - c. getRotationDepartureTime(): returns an integer representing the time at which the rotation departs.

- d. `getRotationReturnBase()`: returns an integer representing the base on which the rotation terminates.
 - e. `getNumberOfRotations()`: returns an integer representing the number of rotations to be initiated each day.
 - f. `getAircraftDownTime()`: returns an integer representing the amount of time an aircraft must rest before it begins another rotation.
2. **Flight**. This interface models an aircraft flight. A flight is simply a departure and arrival of an aircraft, with some quantity of flying time defined between the events. The following methods must be overridden to implement the interface:
- a. `getFlightTimeExtension()`: This method returns an integer representing deviations added to the flight time between bases.
 - b. `getArrivalBase()`: returns an integer representing the arrival base of the flight.
 - c. `getAircraftTurnTimes()`: returns an integer representing the amount of time it takes to turn an aircraft after a flight. For example, in a civilian airline schedule time is needed to unload the passengers, clean the cabin, and then load the new set of passengers.
3. **BaseNetwork**. This interface represents the network in which the aircraft operate. It contains one method that must be overridden, `generateBaseNetwork()`. This method returns a two-dimensional integer array containing the flying times between the bases.

APPENDIX B: Using the Flight Schedule Generator

While it is important to understand the inner workings of the flight schedule generator, an issue likely more important to the typical user is, “How do we implement the flight schedule generator for our application?” The following section discusses implementation issues, step-by-step, by way of a small example.

Suppose a flight schedule with the following characteristics needs to be created:

1. All flights depart and arrive at a single base.
2. The schedule length is two days.
3. Five rotations of length two are initiated each day.
4. The rotations depart uniformly throughout the day.
5. Time between flights in a rotation is sixty minutes.
6. Down time between rotations is 360 minutes.
7. Each flight generated from the base is 240 minutes long.

This example is obviously simplistic, but it allows demonstration of the basic steps required to use the generator.

The first step for implementation is creating the class files that implement the BaseNetwork, Rotation, and Flight interfaces. The following is the code required to implement each and serves as a framework for more complicated classes.

Base Network Implementation:

```
import combs.flightscheduler.*;

public class ExampleBaseNetwork implements BaseNetwork{
    public ExampleBaseNetwork(){
    }

    public int[][] generateBaseNetwork(){
        int[][] baseNetwork = {{0}};
        return baseNetwork;
    }
}
```

```
}
```

Notice the first statement in the ExampleBaseNetwork class, import `combs.flightscheduler.*`. The flight schedule generator is packaged in a Java Archive (JAR) file called `flightscheduler.jar`. Each of the three user-defined classes described above must have this import statement to use the generator. The base network class simply creates a base network of size one with zero inter-base flying time.

Rotation Implementation:

```
import combs.flightscheduler.*;
import drasys.or.prob.*;

public class ExampleRotation implements Rotation{
    //Instance variables
    private DayOfSchedule exampleDayOfSchedule;
    private DiscreteUniformDistribution rotationDepartTime;

    //Create a constructor
    public ExampleRotation(DayOfSchedule dayOfSchedule){
        rotationDepartTime = new DiscreteUniformDistribution(0,1,1440,1);
        this.exampleDayOfSchedule = dayOfSchedule;
    }

    //Implement the various rotation methods
    public int getRotationLength(){
        return 2;
    }
    public int getRotationHomeBase(){
        return 0;
    }
    public int getRotationDepartureTime(){
        int day = exampleDayOfSchedule.getDayOfSchedule();
        int departureTime = (1400*(day-1) + rotationDepartTime.getRandomInteger());
        return departureTime;
    }

    public int getRotationReturnBase(){
        return 0;
    }
}
```

```

public int getNumberOfRotations(){
    return 5;
}
public int getAircraftDownTime(){
    return 360;
}
}

```

The Rotation class demonstrates another advantage of building the generator with an object-oriented language such as Java™. Users can build their own schedules using previously built classes, such as the probability classes found in OR-Objects on www.opsresearch.com (2002). The ExampleRotation class uses the DiscreteUniformDistribution class to spread departures uniformly throughout each scheduled day.

Flight Implementation:

```

import combs.flightscheduler.*;

public class ExampleFlight implements Flight {
    //Constructor
    public ExampleFlight(){
    }

    //Implement the various flight methods
    public int getFlightTimeExtension(){
        return 240;
    }
    public int getArrivalBase(){
        return 0;
    }
    public int getAircraftTurnTimes(){
        return 60;
    }
}

```

Once the implementation classes are built, a main class has to be built to instantiate all objects and run the flight schedule generator. The main class for this example follows.

Main Class:

```
import combs.flightscheduler.*;

public class ExampleScheduler
{

    public static void main(String args[])
    {
        //Set the # of days in the schedule
        int scheduleLength = 2;
        //Set the # of iterations
        int numberIterations = 1;
        //Instantiate an aircraft pool object
        AircraftPool aircraftPool = new AircraftPool();
        //Instantiate a day of schedule object
        DayOfSchedule exampleDayOfSchedule = new DayOfSchedule(scheduleLength);
        //Instantiate a flight schedule object
        Schedule exampleFlightSchedule = new Schedule();
        //Instantiate a flight object
        ExampleFlight exampleFlight = new ExampleFlight();
        //Instantiate a rotation object
        ExampleRotation exampleRotation = new
            ExampleRotation(exampleDayOfSchedule);
        //Instantiate a base network object
        ExampleBaseNetwork exampleBaseNetwork = new ExampleBaseNetwork();
        //Instantiate a flight scheduler object
        FlightScheduler exampleFlightScheduler = new FlightScheduler(aircraftPool,
            exampleDayOfSchedule, exampleRotation, exampleFlight, exampleBaseNetwork,
            exampleFlightSchedule, scheduleLength, numberIterations,
            "/ExampleScheduler/");

        exampleFlightScheduler.generateFlightSchedule();
    }
}
```

The ExampleScheduler class follows a sequence that must be done for any application:

1. Set the schedule length and number of iterations desired.
2. Instantiate all flight schedule classes. Before running the scheduler, ensure that the output directory specified in the FlightScheduler object already exists in the specified location.
3. Call the generateFlightSchedule() method to generate the flight schedule(s).

Once these four classes are created, the user is ready to generate flight schedules. We recommend placing all jar and class files in the same directory when running the generator. A good location is a user-defined directory within the bin directory of the Java™ software. Once this is done, the code must be compiled and run. The commands for this example are:

1. `javac -classpath .;flightscheduler.jar;or124.jar.zip *.java`
2. `java -classpath .;flightschedule.jar;or124.jar.zip ExampleScheduler`

The example schedule produced captures the desired characteristics.

Table 9: Example Flight Schedule

Aircraft ID	Departure Base	Departure Time	Flight Time	Arrival Base	Arrival Time
0	0	229	240	0	469
0	0	529	240	0	769
1	0	701	240	0	941
1	0	1001	240	0	1241
2	0	776	240	0	1016
2	0	1076	240	0	1316
3	0	1109	240	0	1349
3	0	1409	240	0	1649
0	0	1393	240	0	1633
0	0	1693	240	0	1933
1	0	1796	240	0	2036
1	0	2096	240	0	2336
2	0	1823	240	0	2063
2	0	2123	240	0	2363
3	0	2093	240	0	2333
3	0	2393	240	0	2633
0	0	2298	240	0	2538
0	0	2598	240	0	2838
1	0	2787	240	0	3027
1	0	3087	240	0	3327

APPENDIX C: Resolution IV Experimental Design

DP = Design Point

A = Rot/day

B = NumBases

C = TBF

D = TBR

E = NumDIS

F = PCF

G = ISGS

H = CP

I = MDIBN

J = RS

K = RT

L = RDT

M = MWBF

N = tenure

O = Intensify/VB

DP	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O
1	-1	-1	-1	-1	-1	-1	-1	-1	-1	1	-1	-1	-1	1	1
2	-1	-1	-1	-1	-1	-1	-1	-1	-1	1	-1	-1	-1	1	1
3	-1	-1	-1	-1	-1	-1	-1	-1	-1	1	-1	-1	-1	1	1
4	-1	-1	-1	-1	-1	1	1	1	1	1	1	1	1	1	-1
5	-1	-1	-1	-1	-1	1	1	1	1	1	1	1	1	1	-1
6	-1	-1	-1	-1	-1	1	1	1	1	1	1	1	1	1	-1
7	-1	-1	-1	-1	1	-1	1	1	1	-1	-1	-1	-1	1	-1
8	-1	-1	-1	-1	1	-1	1	1	1	-1	-1	-1	-1	1	-1
9	-1	-1	-1	-1	1	-1	1	1	1	-1	-1	-1	-1	1	-1
10	-1	-1	-1	-1	1	1	-1	-1	-1	-1	1	1	1	1	1
11	-1	-1	-1	-1	1	1	-1	-1	-1	-1	1	1	1	1	1
12	-1	-1	-1	-1	1	1	-1	-1	-1	-1	1	1	1	1	1
13	-1	-1	-1	1	-1	-1	1	-1	-1	-1	1	-1	-1	-1	-1
14	-1	-1	-1	1	-1	-1	1	-1	-1	-1	1	-1	-1	-1	-1
15	-1	-1	-1	1	-1	-1	1	-1	-1	-1	1	-1	-1	-1	-1
16	-1	-1	-1	1	-1	1	-1	1	1	-1	-1	1	1	-1	1
17	-1	-1	-1	1	-1	1	-1	1	1	-1	-1	1	1	-1	1
18	-1	-1	-1	1	-1	1	-1	1	1	-1	-1	1	1	-1	1
19	-1	-1	-1	1	1	-1	-1	1	1	1	1	-1	-1	-1	1
20	-1	-1	-1	1	1	-1	-1	1	1	1	1	-1	-1	-1	1
21	-1	-1	-1	1	1	-1	-1	1	1	1	1	-1	-1	-1	1
22	-1	-1	-1	1	1	1	1	-1	-1	1	-1	1	1	-1	-1

23	-1	-1	-1	1	1	1	1	-1	-1	1	-1	1	1	-1	-1
24	-1	-1	-1	1	1	1	1	-1	-1	1	-1	1	1	-1	-1
25	-1	-1	1	-1	-1	-1	-1	1	-1	-1	-1	1	-1	-1	-1
26	-1	-1	1	-1	-1	-1	-1	1	-1	-1	-1	1	-1	-1	-1
27	-1	-1	1	-1	-1	-1	-1	1	-1	-1	-1	1	-1	-1	-1
28	-1	-1	1	-1	-1	1	1	-1	1	-1	1	-1	1	-1	1
29	-1	-1	1	-1	-1	1	1	-1	1	-1	1	-1	1	-1	1
30	-1	-1	1	-1	-1	1	1	-1	1	-1	1	-1	1	-1	1
31	-1	-1	1	-1	1	-1	1	-1	1	1	-1	1	-1	-1	1
32	-1	-1	1	-1	1	-1	1	-1	1	1	-1	1	-1	-1	1
33	-1	-1	1	-1	1	-1	1	-1	1	1	-1	1	-1	-1	1
34	-1	-1	1	-1	1	1	-1	1	-1	1	1	-1	1	-1	-1
35	-1	-1	1	-1	1	1	-1	1	-1	1	1	-1	1	-1	-1
36	-1	-1	1	-1	1	1	-1	1	-1	1	1	-1	1	-1	-1
37	-1	-1	1	1	-1	-1	1	1	-1	1	1	1	-1	1	1
38	-1	-1	1	1	-1	-1	1	1	-1	1	1	1	-1	1	1
39	-1	-1	1	1	-1	-1	1	1	-1	1	1	1	-1	1	1
40	-1	-1	1	1	-1	1	-1	-1	1	1	-1	-1	1	1	-1
41	-1	-1	1	1	-1	1	-1	-1	1	1	-1	-1	1	1	-1
42	-1	-1	1	1	-1	1	-1	-1	1	1	-1	-1	1	1	-1
43	-1	-1	1	1	1	-1	-1	-1	1	-1	1	1	-1	1	-1
44	-1	-1	1	1	1	-1	-1	-1	1	-1	1	1	-1	1	-1
45	-1	-1	1	1	1	-1	-1	-1	1	-1	1	1	-1	1	-1
46	-1	-1	1	1	1	1	1	1	-1	-1	-1	-1	1	1	1
47	-1	-1	1	1	1	1	1	1	-1	-1	-1	-1	1	1	1
48	-1	-1	1	1	1	1	1	1	-1	-1	-1	-1	1	1	1
49	-1	1	-1	-1	-1	-1	-1	-1	1	-1	-1	-1	1	-1	-1
50	-1	1	-1	-1	-1	-1	-1	-1	1	-1	-1	-1	1	-1	-1
51	-1	1	-1	-1	-1	-1	-1	-1	1	-1	-1	-1	1	-1	-1
52	-1	1	-1	-1	-1	1	1	1	-1	-1	1	1	-1	-1	1
53	-1	1	-1	-1	-1	1	1	1	-1	-1	1	1	-1	-1	1
54	-1	1	-1	-1	-1	1	1	1	-1	-1	1	1	-1	-1	1
55	-1	1	-1	-1	1	-1	1	1	-1	1	-1	-1	1	-1	1
56	-1	1	-1	-1	1	-1	1	1	-1	1	-1	-1	1	-1	1
57	-1	1	-1	-1	1	-1	1	1	-1	1	-1	-1	1	-1	1
58	-1	1	-1	-1	1	1	-1	-1	1	1	1	1	-1	-1	-1
59	-1	1	-1	-1	1	1	-1	-1	1	1	1	1	-1	-1	-1
60	-1	1	-1	-1	1	1	-1	-1	1	1	1	1	-1	-1	-1
61	-1	1	-1	1	-1	-1	1	-1	1	1	1	-1	1	1	1
62	-1	1	-1	1	-1	-1	1	-1	1	1	1	-1	1	1	1
63	-1	1	-1	1	-1	-1	1	-1	1	1	1	-1	1	1	1
64	-1	1	-1	1	-1	1	-1	1	-1	1	-1	1	-1	1	-1
65	-1	1	-1	1	-1	1	-1	1	-1	1	-1	1	-1	1	-1
66	-1	1	-1	1	-1	1	-1	1	-1	1	-1	1	-1	1	-1
67	-1	1	-1	1	1	-1	-1	1	-1	-1	1	-1	1	1	-1
68	-1	1	-1	1	1	-1	-1	1	-1	-1	1	-1	1	1	-1

69	-1	1	-1	1	1	-1	-1	1	-1	-1	1	-1	1	1	-1
70	-1	1	-1	1	1	1	1	-1	1	-1	-1	1	-1	1	1
71	-1	1	-1	1	1	1	1	-1	1	-1	-1	1	-1	1	1
72	-1	1	-1	1	1	1	1	-1	1	-1	-1	1	-1	1	1
73	-1	1	1	-1	-1	-1	-1	1	1	1	-1	1	1	1	1
74	-1	1	1	-1	-1	-1	-1	1	1	1	-1	1	1	1	1
75	-1	1	1	-1	-1	-1	-1	1	1	1	-1	1	1	1	1
76	-1	1	1	-1	-1	1	1	-1	-1	1	1	-1	-1	1	-1
77	-1	1	1	-1	-1	1	1	-1	-1	1	1	-1	-1	1	-1
78	-1	1	1	-1	-1	1	1	-1	-1	1	1	-1	-1	1	-1
79	-1	1	1	-1	1	-1	1	-1	-1	-1	-1	1	1	1	-1
80	-1	1	1	-1	1	-1	1	-1	-1	-1	-1	1	1	1	-1
81	-1	1	1	-1	1	-1	1	-1	-1	-1	-1	1	1	1	-1
82	-1	1	1	-1	1	1	-1	1	1	-1	1	-1	-1	1	1
83	-1	1	1	-1	1	1	-1	1	1	-1	1	-1	-1	1	1
84	-1	1	1	-1	1	1	-1	1	1	-1	1	-1	-1	1	1
85	-1	1	1	1	-1	-1	1	1	1	-1	1	1	1	-1	-1
86	-1	1	1	1	-1	-1	1	1	1	-1	1	1	1	-1	-1
87	-1	1	1	1	-1	-1	1	1	1	-1	1	1	1	-1	-1
88	-1	1	1	1	-1	1	-1	-1	-1	-1	-1	-1	-1	-1	1
89	-1	1	1	1	-1	1	-1	-1	-1	-1	-1	-1	-1	-1	1
90	-1	1	1	1	-1	1	-1	-1	-1	-1	-1	-1	-1	-1	1
91	-1	1	1	1	1	-1	-1	-1	-1	1	1	1	1	-1	1
92	-1	1	1	1	1	-1	-1	-1	-1	1	1	1	1	-1	1
93	-1	1	1	1	1	-1	-1	-1	-1	1	1	1	1	-1	1
94	-1	1	1	1	1	1	1	1	1	1	-1	-1	-1	-1	-1
95	-1	1	1	1	1	1	1	1	1	1	-1	-1	-1	-1	-1
96	-1	1	1	1	1	1	1	1	1	1	-1	-1	-1	-1	-1
97	1	-1	-1	-1	-1	-1	-1	-1	-1	1	1	1	1	-1	-1
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99	1	-1	-1	-1	-1	-1	-1	-1	-1	1	1	1	1	-1	-1
100	1	-1	-1	-1	-1	1	1	1	1	1	-1	-1	-1	-1	1
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191	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
192	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1

Alias Structure (up to order 2)

I
Rot/day
num_Base
TBF
TBR
num_DIS
PCF
ISGS
CP

MDIBN
 RS
 RT
 RDT
 MWBF
 tenure
 C/I
 Rot/day*num_Base + PCF*MWBF
 Rot/day*TBF + PCF*RDT
 Rot/day*TBR + PCF*RT
 Rot/day*num_DIS + ISGS*RT + CP*RDT + MDIBN*MWBF + RS*tenure
 Rot/day*PCF + num_Base*MWBF + TBF*RDT + TBR*RT + RS*C/I
 Rot/day*ISGS + num_DIS*RT
 Rot/day*CP + num_DIS*RDT
 Rot/day*MDIBN + num_DIS*MWBF
 Rot/day*RS + num_DIS*tenure + PCF*C/I
 Rot/day*RT + TBR*PCF + num_DIS*ISGS
 Rot/day*RDT + TBF*PCF + num_DIS*CP
 Rot/day*MWBF + num_Base*PCF + num_DIS*MDIBN
 Rot/day*tenure + num_DIS*RS
 Rot/day*C/I + PCF*RS
 num_Base*TBF + CP*MDIBN + RDT*MWBF
 num_Base*TBR + ISGS*MDIBN + RT*MWBF
 num_Base*num_DIS + PCF*MDIBN
 num_Base*ISGS + TBR*MDIBN
 num_Base*CP + TBF*MDIBN
 num_Base*MDIBN + TBF*CP + TBR*ISGS + num_DIS*PCF + tenure*C/I
 num_Base*RS + MWBF*C/I
 num_Base*RT + TBR*MWBF
 num_Base*RDT + TBF*MWBF
 num_Base*tenure + MDIBN*C/I
 num_Base*C/I + MDIBN*tenure + RS*MWBF
 TBF*TBR + ISGS*CP + RT*RDT
 TBF*num_DIS + PCF*CP
 TBF*ISGS + TBR*CP
 TBF*RS + RDT*C/I
 TBF*RT + TBR*RDT
 TBF*tenure + CP*C/I
 TBF*C/I + CP*tenure + RS*RDT
 TBR*num_DIS + PCF*ISGS
 TBR*RS + RT*C/I
 TBR*tenure + ISGS*C/I
 TBR*C/I + ISGS*tenure + RS*RT
 num_DIS*C/I + PCF*tenure
 ISGS*RS + RT*tenure

ISGS*RDT + CP*RT
ISGS*MWBF + MDIBN*RT
CP*RS + RDT*tenure
CP*MWBF + MDIBN*RDT
MDIBN*RS + MWBF*tenure

APPENDIX D: Raw Data on Experimental Design

Design Pt	ATS crews	ATS WT	ATS GI Crews	ATS GI WT	ITER	TST	CC Visited	Ave NS	Ave Tenure
1	14	12130	11	9804	1189	6	57	130	594
2	12	8831	10	7239	949	6	119	187	474
3	17	11843	14	10351	790	5	115	187	395
4	29	9083	29	9083	3012	34	6	409	1504
5	28	6063	27	5653	8071	109	6	420	4028
6	30	7968	28	6981	5658	77	4	425	2824
7	18	136298	16	123655	15505	1900	1550	1540	7738
8	18	129373	17	125618	10801	1463	1604	1685	5391
9	19	130902	18	129163	6204	1235	2661	2346	3097
10	35	226231	35	226231	286	23	66	1121	143
11	35	217389	35	217389	275	26	108	529	138
12	39	246233	39	246233	308	19	125	1053	154
13	14	10418	13	9337	10864	118	12	90	5003
14	18	10384	14	7511	5662	45	18	146	1982
15	16	8776	15	8370	5584	43	10	114	2384
16	24	4623	24	4623	256	2	6	355	90
17	25	3859	24	3704	523	5	2	381	85
18	23	3339	22	3255	526	4	2	292	81
19	40	258132	39	242432	2221	474	1050	1960	55
20	40	274595	36	231090	3454	1492	1286	1867	72
21	38	230364	36	214217	1717	284	492	1650	133
22	35	240329	35	231418	27815	3916	10259	1184	8634
23	32	208104	30	193651	10576	1743	2237	1401	4304
24	38	250875	35	229088	15869	2652	1981	1747	7416
25	19	3653	17	3466	7868	79	4	181	3594
26	21	3051	19	2772	5346	50	4	230	2506
27	20	3189	19	2887	1764	11	2	185	826
28	16	12665	15	11370	1033	5	4	127	18
29	19	11400	18	10512	1060	6	16	160	33
30	18	9684	17	9123	1093	5	14	127	34
31	38	249123	34	214141	6002	1221	1986	1813	169
32	32	216545	27	182777	4295	1324	1863	1745	68
33	36	191600	31	168569	6989	1245	1905	1496	241
34	41	280630	40	269248	11022	2095	988	1749	4804
35	41	292733	40	280756	10843	2179	1052	2004	4742
36	39	256829	39	248448	8455	1647	868	2064	2646
37	29	9285	28	8964	1076	10	5	402	538
38	26	5199	24	4749	1097	9	3	330	548
39	31	9997	28	8309	1516	17	7	468	758

40	19	19607	17	17520	5974	52	40	177	2977
41	14	11402	13	10663	7984	82	28	173	3977
42	19	16261	18	15353	3001	28	60	202	1496
43	35	226231	35	226231	1537	153	71	1134	766
44	35	216216	33	201729	5320	544	263	1241	2650
45	39	246233	37	233507	2826	276	538	1161	1408
46	23	168470	20	149167	3297	2328	440	1906	1646
47	20	145140	19	131202	2836	3771	1623	1927	1416
48	23	167578	19	139926	3496	3857	1666	2247	1745
49	15	13593	14	12231	5577	47	22	140	2713
50	16	10237	15	9918	2782	16	53	122	1277
51	16	11379	16	11379	1511	7	28	74	659
52	25	4727	24	4456	528	4	2	281	74
53	25	3859	25	3859	506	3	2	292	37
54	25	3530	24	3253	527	4	2	283	74
55	36	244288	34	220799	7179	783	2965	1070	127
56	33	233638	31	216184	5705	1481	1259	1399	124
57	35	230486	33	221189	1264	188	525	1991	84
58	56	338356	54	324973	13510	2816	2630	1945	6577
59	55	341325	52	322016	3217	490	630	1228	1206
60	55	298381	52	288308	10785	1843	1166	1399	4309
61	25	23514	23	22117	523	3	9	102	262
62	22	14848	20	13413	528	3	18	151	264
63	31	24900	29	23522	552	7	4	408	276
64	22	4878	18	4320	2790	20	9	164	1390
65	21	3565	19	3239	2783	16	8	148	1387
66	24	4507	21	4099	2787	19	10	155	1389
67	42	256593	37	243395	10488	1402	1212	1789	5224
68	37	236127	34	218406	15984	1943	1360	1361	7962
69	43	261692	40	250678	5487	785	659	1843	2734
70	35	228176	30	204119	2067	179	243	933	1032
71	32	208743	31	196621	1062	87	196	861	531
72	38	214130	33	178358	2712	280	249	1221	1354
73	29	9517	27	9052	525	5	12	408	262
74	25	5695	22	5236	325	2	9	264	163
75	31	11054	30	10930	272	3	8	403	136
76	24	22809	21	19164	5537	49	4	210	2764
77	20	13473	18	12491	10831	111	24	128	5406
78	28	24421	23	19331	11819	189	15	288	5900
79	44	277216	42	268570	16200	2083	943	1403	8085
80	38	252911	37	246467	5840	678	1441	1231	2915
81	44	263109	41	248925	10576	1384	297	1603	5278
82	38	234771	33	212679	2244	3842	1003	1925	1119
83	33	200482	31	186050	2478	3908	1199	1117	1235
84	39	226671	33	203866	1939	230	814	1645	967
85	25	4727	25	4727	3011	26	2	292	1288

86	25	3859	25	3859	3011	24	2	292	1364
87	25	3530	25	3530	3011	27	2	294	1364
88	12	11499	11	9991	523	2	40	134	19
89	14	9855	13	9320	765	4	37	140	23
90	14	9984	12	9045	272	1	24	99	10
91	52	318998	51	311798	1367	196	719	1604	16
92	53	342764	49	312559	1942	322	749	1435	56
93	53	312982	52	299215	1391	180	410	1338	81
94	39	273802	37	255801	15918	2208	2718	989	7467
95	37	269029	35	259167	10624	1634	1459	1586	4493
96	36	236945	35	222518	23455	4127	7662	1684	6599
97	57	13835	51	10787	5569	288	14	1568	2416
98	52	11470	50	10371	2787	99	8	979	1050
99	52	12158	51	11631	2782	109	2	1179	1291
100	27	23390	23	18906	2278	40	220	605	97
101	26	21352	24	17472	2286	57	102	638	67
102	25	25342	22	21378	2091	47	75	659	129
103	68	436584	68	436584	565	294	46	4597	117
104	72	424930	72	424930	578	358	55	4912	126
105	69	428980	69	428980	559	317	49	4868	46
106	27	203200	26	194612	16898	11506	8527	6231	4991
107	30	221511	28	212705	8553	5764	4802	6731	3653
108	30	211391	28	199859	11165	5481	6567	5072	3532
109	43	8062	38	7289	1034	31	6	1033	517
110	45	7743	41	7127	1525	53	5	1216	762
111	48	9286	43	8744	1057	40	6	1415	528
112	30	22313	28	20894	5863	112	10	495	2922
113	29	18774	28	17739	16782	369	7	350	8361
114	31	23851	29	22126	5421	123	10	630	2701
115	72	480921	70	472558	5457	5087	858	7004	2719
116	68	433639	66	431530	8141	5940	493	5625	4056
117	69	428302	65	416681	11151	8342	1734	5990	5557
118	59	369509	55	325669	5641	9834	2104	4671	2817
119	59	346672	54	310960	3766	7408	1551	5574	1880
120	54	316411	53	304011	2885	3956	1290	4255	1441
121	30	23232	30	23161	288	5	4	438	144
122	32	21465	28	19011	562	9	5	459	281
123	34	27422	29	23402	788	16	8	557	393
124	34	6606	33	6496	5539	109	5	514	2765
125	33	5915	27	4967	20668	525	18	541	10314
126	36	7726	30	6548	10562	300	13	670	5271
127	71	452913	69	444345	35488	30999	8278	6464	17714
128	71	431181	70	426438	10949	9028	631	5943	5465
129	65	394082	64	388780	23138	19075	5078	6257	11549
130	57	384401	51	320611	3509	4772	2021	5768	1749
131	54	336819	47	299687	3582	3667	1619	4184	1785

132	53	338693	46	299262	2990	4192	1518	3923	1490
133	27	25002	26	23394	11717	343	89	593	5292
134	30	28138	28	26668	5602	201	41	792	1969
135	30	31097	27	28826	22786	1061	74	838	10812
136	54	15706	47	13600	906	19	20	741	12
137	63	22911	57	21057	563	19	9	1562	15
138	54	17802	50	15457	847	26	8	1089	26
139	35	254662	35	253579	1857	4977	1117	6786	20
140	37	270566	36	271280	1333	3079	787	6205	16
141	36	267899	33	246388	1625	2591	1015	5522	32
142	68	436584	65	413638	10656	5564	154	4673	2885
143	72	418052	65	406480	15629	9192	285	5586	6745
144	69	428760	67	414342	25770	14274	420	5182	12522
145	50	8636	46	7594	602	19	6	1174	301
146	49	7908	46	7113	530	15	4	1048	265
147	49	9147	48	8916	347	9	5	1097	174
148	26	23654	24	20781	10937	172	43	264	5459
149	26	19814	24	18636	28832	1091	76	413	14391
150	27	25271	25	23524	5675	90	58	449	2833
151	91	538437	87	522027	25891	18194	1366	3419	12921
152	81	481728	81	473358	11432	7099	1906	3180	5706
153	85	490110	81	476631	11105	7080	872	2881	5543
154	64	428160	61	403610	2927	6062	1409	3567	1460
155	69	421350	62	378433	4523	7836	2633	5921	2254
156	65	405450	59	371522	4819	6620	2774	4323	2401
157	40	11246	37	9842	11298	362	70	569	4583
158	43	12768	40	11182	13718	438	56	523	5596
159	43	12359	38	10682	17088	587	34	596	7880
160	42	32980	38	29319	643	16	10	637	127
161	48	37881	39	29152	750	18	21	752	32
162	43	38522	39	34796	695	17	9	709	46
163	59	380790	49	318256	2458	2315	1120	3633	86
164	55	366502	46	307800	1925	855	849	2970	74
165	54	345459	46	309790	1911	928	941	3110	89
166	63	392745	59	382328	26475	14277	2198	4921	6897
167	60	394703	57	384131	23462	12616	4459	4534	7213
168	58	359886	56	350548	22285	11490	4674	4546	8539
169	39	33214	38	32766	6205	171	21	599	2943
170	49	43950	44	39584	8369	339	20	864	3667
171	43	44154	40	41111	8143	272	26	775	3637
172	47	12091	40	10538	1563	49	16	916	201
173	48	14441	45	13437	1541	49	9	849	173
174	47	13430	43	12744	1784	39	23	739	88
175	58	350809	52	318730	4961	8110	1609	4103	110
176	56	360187	53	327198	3954	5411	2116	4203	34
177	52	325544	49	299433	4170	6913	2099	4702	78

178	75	491258	69	471013	10454	5890	850	4917	4253
179	70	475082	67	472023	5373	2883	194	4559	1950
180	70	456738	68	446777	5368	2817	948	4616	2400
181	20	18832	19	17026	1126	10	36	198	563
182	22	16845	18	13900	1537	17	37	231	768
183	21	18673	21	18554	540	7	64	462	270
184	50	8636	50	8636	1511	44	11	1032	753
185	50	8117	50	8117	1511	49	7	1220	753
186	50	9346	50	9346	1511	49	6	1215	753
187	53	378835	51	362222	14671	8277	4958	3493	7308
188	52	354332	51	343410	8189	4954	2856	4364	4080
189	53	348452	52	345083	16892	11705	6355	5171	8417
190	95	576533	91	542598	2264	1661	649	3342	1131
191	88	525069	86	497137	3580	2922	725	3027	1788
192	92	522419	88	494198	2744	1743	888	3127	1371

APPENDIX E: Raw Data on Crew Bounds

Design Pt	Crew Bound	WT Bound	% Distance ATS Crews	% Distance ATS WT	% Distance SP Crews	% Distance SP WT
1	13	11980	0.076923077	0.012520868	0.076923077	0.105926544
2	11	8194	0.090909091	0.07773981	0.272727273	0.447522577
3	15	10230	0.133333333	0.157673509	0.2	0.65259042
4	29	9083	0	0	0	0.003743257
5	28	6063	0	0	0	0
6	30	7968	0	0	0	0.0249749
7	15	119911	0.2	0.136659689	0.333333333	0.339718625
8	16	114434	0.125	0.130546865	0.3125	0.310117622
9	18	117773	0.055555556	0.111477164	0.222222222	0.404956994
10	35	226231	0	0	0	0.009927906
11	35	217389	0	0	0	0.012576533
12	39	246233	0	0	0	0.014616237
13	13	9778	0.076923077	0.065453058	0.076923077	0.142769483
14	15	8369	0.2	0.240769507	0.2	0.405185805
15	16	8735	0	0.004693761	0.0625	0.155352032
16	24	4623	0	0	0	0
17	25	3859	0	0	0	0
18	23	3339	0	0	0	0.005390836
19	38	239998	0.052631579	0.075558963	0.078947368	0.152563771
20	40	272452	0	0.007865606	0.025	0.088914745
21	36	205235	0.055555556	0.12244013	0.138888889	0.222120983
22	35	239193	0	0.004749303	0.028571429	0.070119109
23	31	199750	0.032258065	0.041822278	0.032258065	0.078042553
24	38	246455	0	0.017934308	0	0.053380942
25	19	3653	0	0	0	0
26	21	3051	0	0	0	0.034742707
27	20	3114	0	0.024084778	0	0.024084778
28	16	12665	0	0	0	0.01444927
29	18	10754	0.055555556	0.060070671	0.111111111	0.210526316
30	18	9684	0	0	0.055555556	0.136307311
31	38	247646	0	0.005964159	0.052631579	0.0730034
32	31	207540	0.032258065	0.043389226	0.064516129	0.094054158
33	34	182797	0.058823529	0.048157245	0.058823529	0.241519281
34	39	263922	0.051282051	0.063306583	0.051282051	0.111775449
35	41	288983	0	0.012976542	0.024390244	0.063979542
36	37	237250	0.054054054	0.082524763	0.162162162	0.210023182
37	29	9285	0	0	0	0
38	26	5199	0	0	0	0
39	31	9997	0	0	0	0.017605282
40	19	19523	0	0.004302617	0	0.029606106
41	14	10610	0	0.07464656	0.071428571	0.189255419
42	19	15386	0	0.056869882	0	0.257961783
43	35	226231	0	0	0	0.009927906

44	35	216216	0	0	0	0.013972139
45	39	246233	0	0	0	0.014981745
46	19	149513	0.210526316	0.12679165	0.315789474	0.221813488
47	18	134731	0.111111111	0.077257647	0.222222222	0.201928287
48	21	143384	0.095238095	0.168735703	0.142857143	0.255174915
49	15	13593	0	0	0.066666667	0.08916354
50	15	9758	0.066666667	0.049087928	0.133333333	0.203627793
51	16	10904	0	0.043561996	0	0.043561996
52	25	4727	0	0	0	0
53	25	3859	0	0	0	0
54	25	3530	0	0	0	0
55	34	223596	0.058823529	0.092541906	0.088235294	0.184515823
56	31	206200	0.064516129	0.133064985	0.193548387	0.371741028
57	33	197336	0.060606061	0.167987595	0.181818182	0.408815421
58	56	336092	0	0.006736251	0	0.044154577
59	55	341093	0	0.000680166	0.018181818	0.039792667
60	55	298334	0	0.000157542	0.018181818	0.089600917
61	25	23514	0	0	0	0
62	21	14289	0.047619048	0.039121002	0.095238095	0.128210512
63	31	24900	0	0	0	0.023654618
64	22	4878	0	0	0	0.099630996
65	21	3565	0	0	0	0.217391304
66	23	4287	0.043478261	0.051317938	0.043478261	0.380219268
67	40	242313	0.05	0.058932042	0.1	0.10821128
68	37	234381	0	0.007449409	0.027027027	0.072996531
69	40	240184	0.075	0.089548013	0.125	0.183459348
70	35	228176	0	0	0	0.008642451
71	32	208743	0	0	0	0.011142889
72	38	214130	0	0	0	0.012609163
73	29	9517	0	0	0	0
74	25	5695	0	0	0	0.025460931
75	31	11054	0	0	0	0.028767867
76	23	22142	0.043478261	0.030123747	0.043478261	0.059434559
77	18	12335	0.111111111	0.092257803	0.111111111	0.191811917
78	28	24421	0	0	0	0.019982802
79	44	277216	0	0	0	0.011647957
80	38	252911	0	0	0	0.011276694
81	44	263109	0	0	0	0.0145339
82	35	212292	0.085714286	0.105887174	0.142857143	0.171843499
83	32	189460	0.03125	0.058175868	0.09375	0.210904676
84	34	202410	0.147058824	0.119860679	0.235294118	0.269789042
85	25	4727	0	0	0	0
86	25	3859	0	0	0	0
87	25	3530	0	0	0	0
88	12	11499	0	0	0.083333333	0.109139925
89	13	9376	0.076923077	0.051087884	0.153846154	0.220883106
90	14	9408	0	0.06122449	0	0.06122449
91	52	318899	0	0.000310443	0.019230769	0.073339835
92	53	339247	0	0.010367078	0.018867925	0.058688802
93	53	312592	0	0.001247633	0.018867925	0.044946768
94	34	226659	0.147058824	0.207990859	0.147058824	0.24582302

95	34	237677	0.088235294	0.131910113	0.205882353	0.278533472
96	36	222363	0	0.065577457	0.083333333	0.238776235
97	57	13835	0	0	0	0
98	52	11470	0	0	0	0.080470793
99	52	12158	0	0	0	0.087761145
100	26	21538	0.038461538	0.085987557	0.153846154	0.316788931
101	22	17573	0.181818182	0.215045809	0.454545455	0.631024868
102	24	24060	0.041666667	0.053283458	0.291666667	0.312635079
103	68	436584	0	0	0	0.010918861
104	72	424930	0	0	0	0.013981126
105	69	428980	0	0	0	0.011263928
106	21	158447	0.285714286	0.282447759	0.571428571	0.581399458
107	27	189568	0.111111111	0.168504178	0.37037037	0.452164922
108	26	178301	0.153846154	0.18558505	0.307692308	0.383149842
109	43	8062	0	0	0	0
110	45	7743	0	0	0	0.003487021
111	48	9286	0	0	0	0
112	28	19631	0.071428571	0.136620651	0.178571429	0.297947124
113	28	17450	0.035714286	0.075873926	0.035714286	0.202234957
114	28	22419	0.107142857	0.063874392	0.285714286	0.313484098
115	69	457963	0.043478261	0.050130687	0.086956522	0.115225466
116	66	393006	0.03030303	0.103390279	0.03030303	0.143944367
117	66	400261	0.045454545	0.070056788	0.045454545	0.146594347
118	52	313329	0.134615385	0.179300352	0.192307692	0.327470486
119	50	266393	0.18	0.301355516	0.26	0.477140916
120	49	252305	0.102040816	0.25408137	0.183673469	0.408307406
121	30	21466	0	0.082269636	0.066666667	0.161418056
122	31	20858	0.032258065	0.029101544	0.032258065	0.101543772
123	33	26636	0.03030303	0.029508935	0.060606061	0.084810032
124	34	6606	0	0	0	0.040720557
125	33	5915	0	0	0	0.064243449
126	36	7726	0	0	0	0.00673052
127	69	437738	0.028985507	0.034666856	0.086956522	0.140999868
128	70	413047	0.014285714	0.043902994	0.042857143	0.122533271
129	63	371023	0.031746032	0.062149786	0.095238095	0.174986456
130	52	347689	0.096153846	0.105588615	0.192307692	0.235638746
131	53	310388	0.018867925	0.08515471	0.037735849	0.200809954
132	51	314215	0.039215686	0.077902073	0.039215686	0.154381554
133	26	23732	0.038461538	0.053514242	0.115384615	0.157677398
134	26	23952	0.153846154	0.174766199	0.307692308	0.358132933
135	29	30984	0.034482759	0.003647044	0.206896552	0.22669765
136	54	15706	0	0	0	0.024640265
137	63	22911	0	0	0.015873016	0.017022391
138	54	17802	0	0	0	0.006010561
139	30	206209	0.166666667	0.234970346	0.366666667	0.557419899
140	34	239814	0.088235294	0.128232714	0.264705882	0.293335668
141	33	234735	0.090909091	0.141282723	0.212121212	0.313370396
142	68	436584	0	0	0	0.011743445
143	72	418052	0	0	0	0.015526777
144	69	428760	0	0	0	0.011689523
145	50	8636	0	0	0	0

146	49	7908	0	0	0	0
147	49	9147	0	0	0	0
148	25	22083	0.04	0.071140696	0.04	0.090069284
149	24	19372	0.083333333	0.022816436	0.083333333	0.116405121
150	27	25271	0	0	0.148148148	0.184955087
151	91	532356	0	0.011422807	0	0.041203631
152	81	468504	0	0.028226013	0.012345679	0.058012312
153	85	475749	0	0.030186086	0	0.070476239
154	55	351159	0.163636364	0.219276738	0.236363636	0.377265
155	63	370244	0.095238095	0.138033297	0.174603175	0.28349953
156	60	361515	0.083333333	0.121530227	0.15	0.282168098
157	40	11084	0	0.014615662	0.025	0.061349693
158	42	12541	0.023809524	0.01810063	0.023809524	0.090662627
159	43	12351	0	0.000647721	0	0.040725447
160	41	32666	0.024390244	0.009612441	0.048780488	0.060460418
161	48	37343	0	0.014406984	0	0.041399995
162	43	38522	0	0	0.046511628	0.122345673
163	59	380790	0	0	0	0.014349116
164	55	366502	0	0	0	0.013372369
165	54	345459	0	0	0	0.014959807
166	57	342380	0.105263158	0.147102634	0.157894737	0.274586717
167	58	378528	0.034482759	0.042731317	0.068965517	0.154775869
168	54	323767	0.074074074	0.111558621	0.148148148	0.23148437
169	38	32543	0.026315789	0.020618873	0.105263158	0.123805427
170	49	43950	0	0	0.020408163	0.093219568
171	42	43917	0.023809524	0.005396543	0.071428571	0.067536489
172	47	12091	0	0	0	0.037135059
173	48	14372	0	0.004801002	0.020833333	0.145978291
174	47	13286	0	0.010838477	0	0.118846907
175	51	304716	0.137254902	0.151265441	0.196078431	0.311890416
176	53	338244	0.056603774	0.064873287	0.132075472	0.187231703
177	48	289706	0.083333333	0.123704721	0.229166667	0.275061614
178	75	491258	0	0	0	0.013469501
179	70	475082	0	0	0	0.010979157
180	70	456738	0	0	0	0.015124645
181	20	18291	0	0.029577388	0.05	0.085506533
182	21	16402	0.047619048	0.027008901	0.047619048	0.109376905
183	19	17398	0.105263158	0.073284286	0.315789474	0.391884125
184	50	8636	0	0	0	0
185	50	8117	0	0	0	0
186	50	9346	0	0	0	0
187	42	274204	0.261904762	0.381580867	0.285714286	0.456685533
188	46	302908	0.130434783	0.169767718	0.173913043	0.263892007
189	42	258787	0.261904762	0.346481856	0.333333333	0.475139787
190	95	575748	0	0.001363444	0.010526316	0.039366181
191	88	525046	0	4.38057E-05	0.011363636	0.040379319
192	92	519702	0	0.005227996	0.010869565	0.065260476

APPENDIX F: Example TCSP Bound Solution

Arcs in the solution:

X0-1,1.0
X1-21,1.0
X0-2,1.0
X2-5,1.0
X0-3,1.0
X3-9,1.0
X0-4,1.0
X4-12,1.0
X5-13,1.0
X0-6,1.0
X6-27,1.0
X0-7,1.0
X7-16,1.0
X0-8,1.0
X8-18,1.0
X0-10,1.0
X10-25,1.0
X0-11,1.0
X11-19,1.0
X12-20,1.0
X0-14,1.0
X14-26,1.0
X0-15,1.0
X15-24,1.0
X16-22,1.0
X0-17,1.0
X21-29,1.0
X22-28,1.0
X0-23,1.0
X25-30,1.0

The cost is: 1.300001198E10

APPENDIX G: ANOVA Calculations for the Designed Experiment

Analysis of Variance for ATS Crews

Source	DF	Seq SS	Adj SS	Adj MS	F	P
Rot/day	1	21781.4	21781.4	21781.4	671.38	0.000
numBase	1	1604.3	1604.3	1604.3	49.45	0.000
TBF	1	9.6	9.6	9.6	0.30	0.587
TBR	1	0.6	0.6	0.6	0.02	0.889
numDIS	1	17652.5	17652.5	17652.5	544.12	0.000
PCF	1	0.4	0.4	0.4	0.01	0.909
ISGS	1	2.8	2.8	2.8	0.08	0.771
CP	1	11.5	11.5	11.5	0.35	0.552
MDIBN	1	159.5	159.5	159.5	4.92	0.028
RS	1	2921.9	2921.9	2921.9	90.06	0.000
RT	1	4971.5	4971.5	4971.5	153.24	0.000
RDT	1	6996.3	6996.3	6996.3	215.65	0.000
MWBF	1	764.0	764.0	764.0	23.55	0.000
tenure	1	10.5	10.5	10.5	0.33	0.569
C/I	1	7.9	7.9	7.9	0.24	0.622
Error	176	5709.9	5709.9	32.4		
Total	191	62604.6				

Analysis of Variance for ATS WT

Source	DF	Seq SS	Adj SS	Adj MS	F	P
Rot/day	1	3.1894E+11	3.1894E+11	3.1894E+11	112.25	0.000
numBase	1	3.6354E+10	3.6354E+10	3.6354E+10	12.79	0.000
TBF	1	1637413378	1637413378	1637413378	0.58	0.449
TBR	1	1153045	1153045	1153045	0.00	0.984
numDIS	1	4.3850E+12	4.3850E+12	4.3850E+12	1543.32	0.000
PCF	1	24918493	24918493	24918493	0.01	0.925
ISGS	1	412687798	412687798	412687798	0.15	0.704
CP	1	1.6620E+10	1.6620E+10	1.6620E+10	5.85	0.017
MDIBN	1	6201801101	6201801101	6201801101	2.18	0.141
RS	1	4.9041E+10	4.9041E+10	4.9041E+10	17.26	0.000
RT	1	4.2557E+10	4.2557E+10	4.2557E+10	14.98	0.000
RDT	1	3.3708E+10	3.3708E+10	3.3708E+10	11.86	0.001
MWBF	1	1.7412E+10	1.7412E+10	1.7412E+10	6.13	0.014
tenure	1	81019931	81019931	81019931	0.03	0.866
C/I	1	3784878001	3784878001	3784878001	1.33	0.250
Error	176	5.0006E+11	5.0006E+11	2841273781		
Total	191	5.4118E+12				

Analysis of Variance for ATS Near feasible Crews

Source	DF	Seq SS	Adj SS	Adj MS	F	P
Rot/day	1	19180.0	19180.0	19180.0	624.75	0.000
numBase	1	1349.4	1349.4	1349.4	43.95	0.000
TBF	1	12.5	12.5	12.5	0.41	0.524
TBR	1	1.9	1.9	1.9	0.06	0.805

numDIS	1	16856.3	16856.3	16856.3	549.06	0.000
PCF	1	1.9	1.9	1.9	0.06	0.805
ISGS	1	0.0	0.0	0.0	0.00	0.990
CP	1	9.6	9.6	9.6	0.31	0.576
MDIBN	1	231.9	231.9	231.9	7.55	0.007
RS	1	2501.3	2501.3	2501.3	81.48	0.000
RT	1	5450.7	5450.7	5450.7	177.55	0.000
RDT	1	6521.7	6521.7	6521.7	212.43	0.000
MWBF	1	1135.9	1135.9	1135.9	37.00	0.000
tenure	1	10.5	10.5	10.5	0.34	0.559
C/I	1	86.7	86.7	86.7	2.82	0.095
Error	176	5403.2	5403.2	30.7		
Total	191	58753.4				

Analysis of Variance for ATS Near feasible Wait Time

Source	DF	Seq SS	Adj SS	Adj MS	F	P
Rot/day	1	2.9877E+11	2.9877E+11	2.9877E+11	106.96	0.000
numBase	1	3.0056E+10	3.0056E+10	3.0056E+10	10.76	0.001
TBF	1	1398686576	1398686576	1398686576	0.50	0.480
TBR	1	106943596	106943596	106943596	0.04	0.845
numDIS	1	3.9280E+12	3.9280E+12	3.9280E+12	1406.29	0.000
PCF	1	52310664	52310664	52310664	0.02	0.891
ISGS	1	555846020	555846020	555846020	0.20	0.656
CP	1	1.4012E+10	1.4012E+10	1.4012E+10	5.02	0.026
MDIBN	1	8723447252	8723447252	8723447252	3.12	0.079
RS	1	4.0127E+10	4.0127E+10	4.0127E+10	14.37	0.000
RT	1	4.8433E+10	4.8433E+10	4.8433E+10	17.34	0.000
RDT	1	3.2941E+10	3.2941E+10	3.2941E+10	11.79	0.001
MWBF	1	2.6836E+10	2.6836E+10	2.6836E+10	9.61	0.002
tenure	1	103858484	103858484	103858484	0.04	0.847
C/I	1	1.1601E+10	1.1601E+10	1.1601E+10	4.15	0.043
Error	176	4.9160E+11	4.9160E+11	2793168536		
Total	191	4.9333E+12				

Analysis of Variance for Iterations

Source	DF	Seq SS	Adj SS	Adj MS	F	P
Rot/day	1	233866967	233866967	233866967	12.37	0.001
numBase	1	47314	47314	47314	0.00	0.960
TBF	1	1922001	1922001	1922001	0.10	0.750
TBR	1	2581	2581	2581	0.00	0.991
numDIS	1	709748555	709748555	709748555	37.53	0.000
PCF	1	24795438	24795438	24795438	1.31	0.254
ISGS	1	664555717	664555717	664555717	35.14	0.000
CP	1	10187183	10187183	10187183	0.54	0.464
MDIBN	1	1841225	1841225	1841225	0.10	0.755
RS	1	71109311	71109311	71109311	3.76	0.054
RT	1	15638550	15638550	15638550	0.83	0.364
RDT	1	188159401	188159401	188159401	9.95	0.002
MWBF	1	6483435	6483435	6483435	0.34	0.559
tenure	1	12696833	12696833	12696833	0.67	0.414
C/I	1	3434709279	3434709279	3434709279	181.64	0.000
Error	176	3328118071	3328118071	18909762		
Total	191	8703881857				

Analysis of Variance for Total Solution Time (TST)

Source	DF	Seq SS	Adj SS	Adj MS	F	P
Rot/day	1	385188847	385188847	385188847	43.72	0.000
numBase	1	2109456	2109456	2109456	0.24	0.625
TBF	1	4285569	4285569	4285569	0.49	0.486
TBR	1	3473597	3473597	3473597	0.39	0.531
numDIS	1	808360779	808360779	808360779	91.75	0.000
PCF	1	820718	820718	820718	0.09	0.761
ISGS	1	51911600	51911600	51911600	5.89	0.016
CP	1	32514261	32514261	32514261	3.69	0.056
MDIBN	1	52041	52041	52041	0.01	0.939
RS	1	21614923	21614923	21614923	2.45	0.119
RT	1	21085391	21085391	21085391	2.39	0.124
RDT	1	81009538	81009538	81009538	9.20	0.003
MWBF	1	13052	13052	13052	0.00	0.969
tenure	1	14812408	14812408	14812408	1.68	0.196
C/I	1	136692563	136692563	136692563	15.52	0.000
Error	176	1550561940	1550561940	8810011		
Total	191	3114506682				

Analysis of Variance for Number of Conjugacy Classes Visited

Source	DF	Seq SS	Adj SS	Adj MS	F	P
Rot/day	1	5264888	5264888	5264888	3.35	0.069
numBase	1	188376	188376	188376	0.12	0.730
TBF	1	562034	562034	562034	0.36	0.550
TBR	1	181425	181425	181425	0.12	0.734
numDIS	1	145812408	145812408	145812408	92.83	0.000
PCF	1	2006963	2006963	2006963	1.28	0.260
ISGS	1	1549445	1549445	1549445	0.99	0.322
CP	1	14210369	14210369	14210369	9.05	0.003
MDIBN	1	1010360	1010360	1010360	0.64	0.424
RS	1	7524792	7524792	7524792	4.79	0.030
RT	1	10617305	10617305	10617305	6.76	0.010
RDT	1	23888230	23888230	23888230	15.21	0.000
MWBF	1	1531888	1531888	1531888	0.98	0.325
tenure	1	2104219	2104219	2104219	1.34	0.249
C/I	1	19797999	19797999	19797999	12.60	0.000
Error	176	276448966	276448966	1570733		
Total	191	512699666				

Analysis of Variance for Average Neighborhood Size

Source	DF	Seq SS	Adj SS	Adj MS	F	P
Rot/day	1	171015050	171015050	171015050	211.27	0.000
numBase	1	9284002	9284002	9284002	11.47	0.001
TBF	1	166852	166852	166852	0.21	0.650
TBR	1	27792	27792	27792	0.03	0.853
numDIS	1	335386133	335386133	335386133	414.33	0.000
PCF	1	183521	183521	183521	0.23	0.635
ISGS	1	1022292	1022292	1022292	1.26	0.263
CP	1	1249365	1249365	1249365	1.54	0.216
MDIBN	1	660352	660352	660352	0.82	0.368

RS	1	20378	20378	20378	0.03	0.874
RT	1	120501	120501	120501	0.15	0.700
RDT	1	1075205	1075205	1075205	1.33	0.251
MWBF	1	2121002	2121002	2121002	2.62	0.107
tenure	1	560520	560520	560520	0.69	0.406
C/I	1	869678	869678	869678	1.07	0.301
Error	176	142465887	142465887	809465		
Total	191	666228531				

Analysis of Variance for Average Tenure

Source	DF	Seq SS	Adj SS	Adj MS	F	P
Rot/day	1	51046875	51046875	51046875	12.28	0.001
numBase	1	250274	250274	250274	0.06	0.806
TBF	1	5852	5852	5852	0.00	0.970
TBR	1	244816	244816	244816	0.06	0.809
numDIS	1	86028075	86028075	86028075	20.70	0.000
PCF	1	2916588	2916588	2916588	0.70	0.403
ISGS	1	104270761	104270761	104270761	25.09	0.000
CP	1	19120	19120	19120	0.00	0.946
MDIBN	1	664581	664581	664581	0.16	0.690
RS	1	13005213	13005213	13005213	3.13	0.079
RT	1	1426920	1426920	1426920	0.34	0.559
RDT	1	27700485	27700485	27700485	6.66	0.011
MWBF	1	778771	778771	778771	0.19	0.666
tenure	1	26082431	26082431	26082431	6.28	0.013
C/I	1	813231049	813231049	813231049	195.66	0.000
Error	176	731527053	731527053	4156404		
Total	191	1859198864				

Estimated Effects and Coefficients for ATS CREWS(coded units)

Term	Effect	Coef	SE Coef	T	P
Constant		40.151	0.1739	230.88	0.000
Rot/day	21.302	10.651	0.1739	61.25	0.000
num_Base	5.781	2.891	0.1739	16.62	0.000
TBF	0.448	0.224	0.1739	1.29	0.200
TBR	-0.115	-0.057	0.1739	-0.33	0.742
num_DIS	19.177	9.589	0.1739	55.14	0.000
PCF	0.094	0.047	0.1739	0.27	0.788
ISGS	-0.240	-0.120	0.1739	-0.69	0.492
CP	0.490	0.245	0.1739	1.41	0.162
MDIBN	1.823	0.911	0.1739	5.24	0.000
RS	7.802	3.901	0.1739	22.43	0.000
RT	10.177	5.089	0.1739	29.26	0.000
RDT	12.073	6.036	0.1739	34.71	0.000
MWBF	3.990	1.995	0.1739	11.47	0.000
tenure	0.469	0.234	0.1739	1.35	0.180
C/I	-0.406	-0.203	0.1739	-1.17	0.245
Rot/day*num_Base	0.531	0.266	0.1739	1.53	0.129
Rot/day*TBF	-0.177	-0.089	0.1739	-0.51	0.611
Rot/day*TBR	0.010	0.005	0.1739	0.03	0.976
Rot/day*num_DIS	3.510	1.755	0.1739	10.09	0.000
Rot/day*PCF	0.260	0.130	0.1739	0.75	0.455
Rot/day*ISGS	2.385	1.193	0.1739	6.86	0.000

Rot/day*CP	0.531	0.266	0.1739	1.53	0.129
Rot/day*MDIBN	1.240	0.620	0.1739	3.56	0.001
Rot/day*RS	1.802	0.901	0.1739	5.18	0.000
Rot/day*RT	3.052	1.526	0.1739	8.78	0.000
Rot/day*RDT	4.781	2.391	0.1739	13.75	0.000
Rot/day*MWBF	2.156	1.078	0.1739	6.20	0.000
Rot/day*tenure	2.302	1.151	0.1739	6.62	0.000
Rot/day*C/I	-0.073	-0.036	0.1739	-0.21	0.834
num_Base*TBF	0.052	0.026	0.1739	0.15	0.881
num_Base*TBR	-2.177	-1.089	0.1739	-6.26	0.000
num_Base*num_DIS	3.948	1.974	0.1739	11.35	0.000
num_Base*ISGS	-1.010	-0.505	0.1739	-2.91	0.004
num_Base*CP	-0.281	-0.141	0.1739	-0.81	0.420
num_Base*MDIBN	0.219	0.109	0.1739	0.63	0.530
num_Base*RS	0.365	0.182	0.1739	1.05	0.296
num_Base*RT	-0.552	-0.276	0.1739	-1.59	0.115
num_Base*RDT	-0.740	-0.370	0.1739	-2.13	0.035
num_Base*tenure	0.656	0.328	0.1739	1.89	0.061
num_Base*C/I	-0.344	-0.172	0.1739	-0.99	0.325
TBF*TBR	-0.677	-0.339	0.1739	-1.95	0.054
TBF*num_DIS	0.490	0.245	0.1739	1.41	0.162
TBF*ISGS	0.656	0.328	0.1739	1.89	0.061
TBF*RS	0.073	0.036	0.1739	0.21	0.834
TBF*RT	0.281	0.141	0.1739	0.81	0.420
TBF*tenure	-1.135	-0.568	0.1739	-3.26	0.001
TBF*C/I	-1.635	-0.818	0.1739	-4.70	0.000
TBR*num_DIS	-0.406	-0.203	0.1739	-1.17	0.245
TBR*RS	-0.198	-0.099	0.1739	-0.57	0.570
TBR*tenure	0.094	0.047	0.1739	0.27	0.788
TBR*C/I	1.427	0.714	0.1739	4.10	0.000
num_DIS*C/I	-1.740	-0.870	0.1739	-5.00	0.000
ISGS*RS	-0.615	-0.307	0.1739	-1.77	0.080
ISGS*RDT	0.448	0.224	0.1739	1.29	0.200
ISGS*MWBF	-0.302	-0.151	0.1739	-0.87	0.387
CP*RS	-0.510	-0.255	0.1739	-1.47	0.145
CP*MWBF	0.010	0.005	0.1739	0.03	0.976
MDIBN*RS	1.698	0.849	0.1739	4.88	0.000

Analysis of Variance for ATS (coded units)

Source	DF	Seq SS	Adj SS	Adj MS	F	P
Main Effects	15	56894.7	56894.7	3792.98	653.22	0.000
2-Way Interactions	43	4937.6	4937.6	114.83	19.78	0.000
Residual Error	133	772.3	772.3	5.81		
Lack of Fit	5	24.3	24.3	4.86	0.83	0.530
Pure Error	128	748.0	748.0	5.84		
Total	191	62604.6				

Unusual Observations for ATS _ cr

Obs	ATS _ cr	Fit	SE Fit	Residual	St Resid
62	22.0000	26.4531	1.3358	-4.4531	-2.22R
63	31.0000	26.4531	1.3358	4.5469	2.27R
78	28.0000	23.2656	1.3358	4.7344	2.36R
80	38.0000	42.5156	1.3358	-4.5156	-2.25R
137	63.0000	56.5990	1.3358	6.4010	3.19R

151	91.0000	85.2656	1.3358	5.7344	2.86R
152	81.0000	85.2656	1.3358	-4.2656	-2.13R
169	39.0000	44.1823	1.3358	-5.1823	-2.58R
170	49.0000	44.1823	1.3358	4.8177	2.40R
178	75.0000	70.9323	1.3358	4.0677	2.03R

R denotes an observation with a large standardized residual

Estimated Effects and Coefficients for ATS Wait Time(coded units)

Term	Effect	Coef	SE Coef	T	P
Constant		165491	991.1	166.97	0.000
Rot/day	81514	40757	991.1	41.12	0.000
num_Base	27520	13760	991.1	13.88	0.000
TBF	5841	2920	991.1	2.95	0.004
TBR	-155	-77	991.1	-0.08	0.938
num_DIS	302248	151124	991.1	152.48	0.000
PCF	721	360	991.1	0.36	0.717
ISGS	2932	1466	991.1	1.48	0.141
CP	18608	9304	991.1	9.39	0.000
MDIBN	11367	5683	991.1	5.73	0.000
RS	31964	15982	991.1	16.12	0.000
RT	29776	14888	991.1	15.02	0.000
RDT	26500	13250	991.1	13.37	0.000
MWBF	19046	9523	991.1	9.61	0.000
tenure	1299	650	991.1	0.66	0.513
C/I	-8880	-4440	991.1	-4.48	0.000
Rot/day*num_Base	3839	1919	991.1	1.94	0.055
Rot/day*TBF	607	304	991.1	0.31	0.760
Rot/day*TBR	-1732	-866	991.1	-0.87	0.384
Rot/day*num_DIS	72225	36113	991.1	36.44	0.000
Rot/day*PCF	4	2	991.1	0.00	0.998
Rot/day*ISGS	26319	13160	991.1	13.28	0.000
Rot/day*CP	38562	19281	991.1	19.45	0.000
Rot/day*MDIBN	17950	8975	991.1	9.06	0.000
Rot/day*RS	3027	1514	991.1	1.53	0.129
Rot/day*RT	4240	2120	991.1	2.14	0.034
Rot/day*RDT	14928	7464	991.1	7.53	0.000
Rot/day*MWBF	10840	5420	991.1	5.47	0.000
Rot/day*tenure	25443	12722	991.1	12.84	0.000
Rot/day*C/I	-2053	-1026	991.1	-1.04	0.302
num_Base*TBF	120	60	991.1	0.06	0.952
num_Base*TBR	-6197	-3099	991.1	-3.13	0.002
num_Base*num_DIS	25592	12796	991.1	12.91	0.000
num_Base*ISGS	-3173	-1586	991.1	-1.60	0.112
num_Base*CP	-3281	-1640	991.1	-1.66	0.100
num_Base*MDIBN	748	374	991.1	0.38	0.707
num_Base*RS	455	227	991.1	0.23	0.819
num_Base*RT	-8361	-4180	991.1	-4.22	0.000
num_Base*RDT	-52	-26	991.1	-0.03	0.979
num_Base*tenure	1431	715	991.1	0.72	0.472
num_Base*C/I	-1006	-503	991.1	-0.51	0.613
TBF*TBR	-1548	-774	991.1	-0.78	0.436
TBF*num_DIS	4550	2275	991.1	2.30	0.023

TBF*ISGS	4556	2278	991.1	2.30	0.023
TBF*RS	-4354	-2177	991.1	-2.20	0.030
TBF*RT	-569	-285	991.1	-0.29	0.774
TBF*tenure	-4775	-2388	991.1	-2.41	0.017
TBF*C/I	-10133	-5067	991.1	-5.11	0.000
TBR*num_DIS	-160	-80	991.1	-0.08	0.936
TBR*RS	1059	530	991.1	0.53	0.594
TBR*tenure	161	80	991.1	0.08	0.936
TBR*C/I	2583	1292	991.1	1.30	0.195
num_DIS*C/I	-8853	-4426	991.1	-4.47	0.000
ISGS*RS	-3709	-1854	991.1	-1.87	0.064
ISGS*RDT	2193	1096	991.1	1.11	0.271
ISGS*MWBF	-4108	-2054	991.1	-2.07	0.040
CP*RS	-2787	-1394	991.1	-1.41	0.162
CP*MWBF	634	317	991.1	0.32	0.750
MDIBN*RS	5785	2892	991.1	2.92	0.004

Analysis of Variance for ATS (coded units)

Source	DF	Seq SS	Adj SS	Adj MS	F	P
Main Effects	15	4.91176E+12	4.9118E+12	3.2745E+11	2E+03	0.000
2-Way Interactions	43	4.74979E+11	4.7498E+11	1.1046E+10	58.57	0.000
Residual Error	133	25085081634	2.5085E+10	188609636		
Lack of Fit	5	948762311	948762311	189752462	1.01	0.417
Pure Error	128	24136319323	2.4136E+10	188564995		
Total	191	5.41182E+12				

Unusual Observations for ATS WT

Obs	ATS WT	Fit	SE Fit	Residual	St Resid
20	274595	250568	7613	24027	2.10R
23	208104	231133	7613	-23029	-2.01R
31	249123	217430	7613	31693	2.77R
33	191600	217430	7613	-25830	-2.26R
60	298381	329460	7613	-31079	-2.72R
96	236945	261941	7613	-24996	-2.19R
115	480921	449599	7613	31322	2.74R
120	316411	347984	7613	-31573	-2.76R
127	452913	425901	7613	27012	2.36R
129	394082	425901	7613	-31819	-2.78R
130	384401	354955	7613	29446	2.58R
151	538437	499995	7613	38442	3.36R
190	576533	541142	7613	35391	3.10R

R denotes an observation with a large standardized residual

Estimated Effects and Coefficients for ATS Near feasible Crews

Term	Effect	Coef	SE Coef	T	P
Constant		37.557	0.1468	255.76	0.000
Rot/day	19.990	9.995	0.1468	68.06	0.000
num_Base	5.302	2.651	0.1468	18.05	0.000
TBF	0.510	0.255	0.1468	1.74	0.085
TBR	-0.198	-0.099	0.1468	-0.67	0.502
num_DIS	18.740	9.370	0.1468	63.81	0.000

PCF	-0.198	-0.099	0.1468	-0.67	0.502
ISGS	-0.010	-0.005	0.1468	-0.04	0.972
CP	0.448	0.224	0.1468	1.53	0.130
MDIBN	2.198	1.099	0.1468	7.48	0.000
RS	7.219	3.609	0.1468	24.58	0.000
RT	10.656	5.328	0.1468	36.28	0.000
RDT	11.656	5.828	0.1468	39.69	0.000
MWBF	4.865	2.432	0.1468	16.56	0.000
tenure	0.469	0.234	0.1468	1.60	0.113
C/I	-1.344	-0.672	0.1468	-4.58	0.000
Rot/day*num_Base	0.552	0.276	0.1468	1.88	0.062
Rot/day*TBF	0.010	0.005	0.1468	0.04	0.972
Rot/day*TBR	-0.031	-0.016	0.1468	-0.11	0.915
Rot/day*num_DIS	3.781	1.891	0.1468	12.87	0.000
Rot/day*PCF	-0.198	-0.099	0.1468	-0.67	0.502
Rot/day*ISGS	2.698	1.349	0.1468	9.19	0.000
Rot/day*CP	0.323	0.161	0.1468	1.10	0.274
Rot/day*MDIBN	1.573	0.786	0.1468	5.36	0.000
Rot/day*RS	1.719	0.859	0.1468	5.85	0.000
Rot/day*RT	3.281	1.641	0.1468	11.17	0.000
Rot/day*RDT	4.115	2.057	0.1468	14.01	0.000
Rot/day*MWBF	2.073	1.036	0.1468	7.06	0.000
Rot/day*tenure	2.969	1.484	0.1468	10.11	0.000
Rot/day*C/I	-0.635	-0.318	0.1468	-2.16	0.032
num_Base*TBF	0.865	0.432	0.1468	2.94	0.004
num_Base*TBR	-2.052	-1.026	0.1468	-6.99	0.000
num_Base*num_DIS	3.260	1.630	0.1468	11.10	0.000
num_Base*ISGS	-0.615	-0.307	0.1468	-2.09	0.038
num_Base*CP	-0.615	-0.307	0.1468	-2.09	0.038
num_Base*MDIBN	0.094	0.047	0.1468	0.32	0.750
num_Base*RS	0.573	0.286	0.1468	1.95	0.053
num_Base*RT	-0.740	-0.370	0.1468	-2.52	0.013
num_Base*RDT	-0.365	-0.182	0.1468	-1.24	0.217
num_Base*tenure	0.948	0.474	0.1468	3.23	0.002
num_Base*C/I	-0.531	-0.266	0.1468	-1.81	0.073
TBF*TBR	0.573	0.286	0.1468	1.95	0.053
TBF*num_DIS	0.427	0.214	0.1468	1.45	0.148
TBF*ISGS	0.219	0.109	0.1468	0.74	0.458
TBF*RS	0.073	0.036	0.1468	0.25	0.804
TBF*RT	0.052	0.026	0.1468	0.18	0.860
TBF*tenure	-1.094	-0.547	0.1468	-3.72	0.000
TBF*C/I	-1.865	-0.932	0.1468	-6.35	0.000
TBR*num_DIS	-0.573	-0.286	0.1468	-1.95	0.053
TBR*RS	0.198	0.099	0.1468	0.67	0.502
TBR*tenure	0.573	0.286	0.1468	1.95	0.053
TBR*C/I	1.219	0.609	0.1468	4.15	0.000
num_DIS*C/I	-2.010	-1.005	0.1468	-6.85	0.000
ISGS*RS	-0.365	-0.182	0.1468	-1.24	0.217
ISGS*RDT	0.448	0.224	0.1468	1.53	0.130
ISGS*MWBF	-0.385	-0.193	0.1468	-1.31	0.192
CP*RS	-0.156	-0.078	0.1468	-0.53	0.596
CP*MWBF	-0.010	-0.005	0.1468	-0.04	0.972
MDIBN*RS	1.385	0.693	0.1468	4.72	0.000

Analysis of Variance for ATS_GI_C (coded units)

Source	DF	Seq SS	Adj SS	Adj MS	F	P
Main Effects	15	53350.2	53350.2	3556.68	859.05	0.000
2-Way Interactions	43	4852.6	4852.6	112.85	27.26	0.000
Residual Error	133	550.7	550.7	4.14		
Lack of Fit	5	15.3	15.3	3.06	0.73	0.600
Pure Error	128	535.3	535.3	4.18		
Total	191	58753.4				

Unusual Observations for ATS_GI_C

Obs	ATS_GI_C	Fit	SE Fit	Residual	St Resid
32	27.0000	30.8802	1.1279	-3.8802	-2.29R
62	20.0000	24.4427	1.1279	-4.4427	-2.62R
63	29.0000	24.4427	1.1279	4.5573	2.69R
74	22.0000	26.1094	1.1279	-4.1094	-2.43R
75	30.0000	26.1094	1.1279	3.8906	2.30R
80	37.0000	40.4427	1.1279	-3.4427	-2.03R
125	27.0000	30.4427	1.1279	-3.4427	-2.03R
136	47.0000	51.0677	1.1279	-4.0677	-2.40R
137	57.0000	51.0677	1.1279	5.9323	3.50R
151	87.0000	82.7344	1.1279	4.2656	2.52R

R denotes an observation with a large standardized residual

Estimated Effects and Coefficients for ATS Near feasible Wait Time

Term	Effect	Coef	SE Coef	T	P
Constant		156037	861.1	181.20	0.000
Rot/day	78895	39447	861.1	45.81	0.000
num_Base	25023	12512	861.1	14.53	0.000
TBF	5398	2699	861.1	3.13	0.002
TBR	-1493	-746	861.1	-0.87	0.388
num_DIS	286065	143033	861.1	166.10	0.000
PCF	-1044	-522	861.1	-0.61	0.545
ISGS	3403	1701	861.1	1.98	0.050
CP	17086	8543	861.1	9.92	0.000
MDIBN	13481	6741	861.1	7.83	0.000
RS	28913	14457	861.1	16.79	0.000
RT	31765	15883	861.1	18.44	0.000
RDT	26197	13098	861.1	15.21	0.000
MWBF	23645	11822	861.1	13.73	0.000
tenure	1471	735	861.1	0.85	0.395
C/I	-15546	-7773	861.1	-9.03	0.000
Rot/day*num_Base	2156	1078	861.1	1.25	0.213
Rot/day*TBF	1258	629	861.1	0.73	0.466
Rot/day*TBR	-1223	-611	861.1	-0.71	0.479
Rot/day*num_DIS	70556	35278	861.1	40.97	0.000
Rot/day*PCF	-2349	-1175	861.1	-1.36	0.175
Rot/day*ISGS	28634	14317	861.1	16.63	0.000
Rot/day*CP	36904	18452	861.1	21.43	0.000
Rot/day*MDIBN	22271	11135	861.1	12.93	0.000
Rot/day*RS	2845	1423	861.1	1.65	0.101
Rot/day*RT	4731	2365	861.1	2.75	0.007
Rot/day*RDT	13631	6815	861.1	7.91	0.000

Rot/day*MWBF	12712	6356	861.1	7.38	0.000
Rot/day*tenure	23410	11705	861.1	13.59	0.000
Rot/day*C/I	-4992	-2496	861.1	-2.90	0.004
num_Base*TBF	2915	1458	861.1	1.69	0.093
num_Base*TBR	-6361	-3180	861.1	-3.69	0.000
num_Base*num_DIS	23125	11562	861.1	13.43	0.000
num_Base*ISGS	-2101	-1050	861.1	-1.22	0.225
num_Base*CP	-3265	-1632	861.1	-1.90	0.060
num_Base*MDIBN	-705	-352	861.1	-0.41	0.683
num_Base*RS	4273	2137	861.1	2.48	0.014
num_Base*RT	-9178	-4589	861.1	-5.33	0.000
num_Base*RDT	-284	-142	861.1	-0.17	0.869
num_Base*tenure	2157	1079	861.1	1.25	0.213
num_Base*C/I	-2409	-1204	861.1	-1.40	0.164
TBF*TBR	2511	1256	861.1	1.46	0.147
TBF*num_DIS	3877	1939	861.1	2.25	0.026
TBF*ISGS	2449	1224	861.1	1.42	0.157
TBF*RS	-4314	-2157	861.1	-2.51	0.013
TBF*RT	-2122	-1061	861.1	-1.23	0.220
TBF*tenure	-5901	-2951	861.1	-3.43	0.001
TBF*C/I	-10654	-5327	861.1	-6.19	0.000
TBR*num_DIS	-1609	-805	861.1	-0.93	0.352
TBR*RS	3807	1904	861.1	2.21	0.029
TBR*tenure	1079	540	861.1	0.63	0.532
TBR*C/I	2023	1012	861.1	1.17	0.242
num_DIS*C/I	-15199	-7600	861.1	-8.83	0.000
ISGS*RS	-3545	-1772	861.1	-2.06	0.042
ISGS*RDT	2935	1468	861.1	1.70	0.091
ISGS*MWBF	-4823	-2411	861.1	-2.80	0.006
CP*RS	-1735	-868	861.1	-1.01	0.316
CP*MWBF	1183	592	861.1	0.69	0.493
MDIBN*RS	3715	1857	861.1	2.16	0.033

Analysis of Variance for ATS_GI_W (coded units)

Source	DF	Seq SS	Adj SS	Adj MS	F	P
Main Effects	15	4.44172E+12	4.4417E+12	2.9611E+11	2E+03	0.000
2-Way Interactions	43	4.72662E+11	4.7266E+11	1.0992E+10	77.21	0.000
Residual Error	133	18935361545	1.8935E+10	142371139		
Lack of Fit	5	1380457410	1380457410	276091482	2.01	0.081
Pure Error	128	17554904135	1.7555E+10	137147689		
Total	191	4.93332E+12				

Unusual Observations for ATS_GI_W

Obs	ATS_GI_W	Fit	SE Fit	Residual	St Resid
12	246233	226057	6614	20176	2.03R
23	193651	217242	6614	-23591	-2.38R
31	214141	187345	6614	26796	2.70R
44	201729	222423	6614	-20694	-2.08R
60	288308	314131	6614	-25823	-2.60R
68	218406	240790	6614	-22384	-2.25R
96	222518	247577	6614	-25059	-2.52R
115	472558	438920	6614	33638	3.39R
117	416681	438920	6614	-22239	-2.24R
127	444345	416706	6614	27639	2.78R

129	388780	416706	6614	-27926	-2.81R
151	522027	486161	6614	35866	3.61R
168	350548	371185	6614	-20637	-2.08R
190	542598	513862	6614	28736	2.89R

R denotes an observation with a large standardized residual

Estimated Effects and Coefficients for Iterations

Term	Effect	Coef	SE Coef	T	P
Constant		6089	277.4	21.95	0.000
Rot/day	2207	1104	277.4	3.98	0.000
num_Base	-31	-16	277.4	-0.06	0.955
TBF	-200	-100	277.4	-0.36	0.719
TBR	7	4	277.4	0.01	0.989
num_DIS	3845	1923	277.4	6.93	0.000
PCF	719	359	277.4	1.30	0.197
ISGS	3721	1860	277.4	6.71	0.000
CP	-461	-230	277.4	-0.83	0.408
MDIBN	-196	-98	277.4	-0.35	0.725
RS	1217	609	277.4	2.19	0.030
RT	-571	-285	277.4	-1.03	0.305
RDT	-1980	-990	277.4	-3.57	0.000
MWBF	-368	-184	277.4	-0.66	0.509
tenure	-514	-257	277.4	-0.93	0.356
C/I	-8459	-4230	277.4	-15.25	0.000
Rot/day*num_Base	159	79	277.4	0.29	0.776
Rot/day*TBF	-213	-107	277.4	-0.38	0.701
Rot/day*TBR	58	29	277.4	0.10	0.917
Rot/day*num_DIS	-159	-79	277.4	-0.29	0.775
Rot/day*PCF	-267	-134	277.4	-0.48	0.631
Rot/day*ISGS	1091	546	277.4	1.97	0.051
Rot/day*CP	-466	-233	277.4	-0.84	0.403
Rot/day*MDIBN	745	373	277.4	1.34	0.181
Rot/day*RS	-696	-348	277.4	-1.25	0.212
Rot/day*RT	849	425	277.4	1.53	0.128
Rot/day*RDT	-741	-371	277.4	-1.34	0.184
Rot/day*MWBF	-327	-164	277.4	-0.59	0.556
Rot/day*tenure	733	366	277.4	1.32	0.189
Rot/day*C/I	-1967	-984	277.4	-3.55	0.001
num_Base*TBF	-1453	-726	277.4	-2.62	0.010
num_Base*TBR	6	3	277.4	0.01	0.991
num_Base*num_DIS	478	239	277.4	0.86	0.391
num_Base*ISGS	6	3	277.4	0.01	0.992
num_Base*CP	14	7	277.4	0.03	0.979
num_Base*MDIBN	359	179	277.4	0.65	0.519
num_Base*RS	-177	-89	277.4	-0.32	0.750
num_Base*RT	273	136	277.4	0.49	0.624
num_Base*RDT	-656	-328	277.4	-1.18	0.239
num_Base*tenure	37	18	277.4	0.07	0.947
num_Base*C/I	25	12	277.4	0.04	0.964
TBF*TBR	-1126	-563	277.4	-2.03	0.044
TBF*num_DIS	12	6	277.4	0.02	0.983
TBF*ISGS	214	107	277.4	0.39	0.701

TBF*RS	1400	700	277.4	2.52	0.013
TBF*RT	-158	-79	277.4	-0.29	0.776
TBF*tenure	315	158	277.4	0.57	0.571
TBF*C/I	500	250	277.4	0.90	0.369
TBR*num_DIS	396	198	277.4	0.71	0.477
TBR*RS	-112	-56	277.4	-0.20	0.840
TBR*tenure	-2816	-1408	277.4	-5.08	0.000
TBR*C/I	-437	-219	277.4	-0.79	0.432
num_DIS*C/I	-1912	-956	277.4	-3.45	0.001
ISGS*RS	324	162	277.4	0.58	0.560
ISGS*RTD	214	107	277.4	0.39	0.701
ISGS*MWBF	609	304	277.4	1.10	0.274
CP*RS	-635	-317	277.4	-1.14	0.254
CP*MWBF	-526	-263	277.4	-0.95	0.345
MDIBN*RS	450	225	277.4	0.81	0.418

Analysis of Variance for iteratio (coded units)

Source	DF	Seq SS	Adj SS	Adj MS	F	P
Main Effects	15	5375763787	5375763787	358384252	24.26	0.000
2-Way Interactions	43	1363363167	1363363167	31706120	2.15	0.001
Residual Error	133	1964754904	1964754904	14772593		
Lack of Fit	5	20007766	20007766	4001553	0.26	0.932
Pure Error	128	1944747138	1944747138	15193337		
Total	191	8703881857				

Unusual Observations for iteratio

Obs	iteratio	Fit	SE Fit	Residual	St Resid
22	27815.0	17752.3	2130.6	10062.7	3.15R
23	10576.0	17752.3	2130.6	-7176.3	-2.24R
96	23455.0	16732.7	2130.6	6722.3	2.10R
113	16782.0	9020.9	2130.6	7761.1	2.43R
124	5539.0	12649.1	2130.6	-7110.1	-2.22R
125	20668.0	12649.1	2130.6	8018.9	2.51R
127	35488.0	22693.6	2130.6	12794.4	4.00R
128	10949.0	22693.6	2130.6	-11744.6	-3.67R
134	5602.0	13731.2	2130.6	-8129.2	-2.54R
135	22786.0	13731.2	2130.6	9054.8	2.83R
142	10656.0	17094.1	2130.6	-6438.1	-2.01R
144	25770.0	17094.1	2130.6	8675.9	2.71R
149	28832.0	14758.3	2130.6	14073.7	4.40R
150	5675.0	14758.3	2130.6	-9083.3	-2.84R
151	25891.0	16427.1	2130.6	9463.9	2.96R

R denotes an observation with a large standardized residual

Estimated Effects and Coefficients for Total Solution Time (TST)

Term	Effect	Coef	SE Coef	T	P
Constant		2149.1	148.6	14.46	0.000
Rot/day	2832.8	1416.4	148.6	9.53	0.000
num_Base	-209.6	-104.8	148.6	-0.71	0.482
TBF	298.8	149.4	148.6	1.01	0.317
TBR	-269.0	-134.5	148.6	-0.90	0.367

num_DIS	4103.8	2051.9	148.6	13.80	0.000
PCF	130.8	65.4	148.6	0.44	0.661
ISGS	1039.9	520.0	148.6	3.50	0.001
CP	-823.0	-411.5	148.6	-2.77	0.006
MDIBN	-32.9	-16.5	148.6	-0.11	0.912
RS	671.1	335.5	148.6	2.26	0.026
RT	662.8	331.4	148.6	2.23	0.027
RDT	-1299.1	-649.6	148.6	-4.37	0.000
MWBF	16.5	8.2	148.6	0.06	0.956
tenure	555.5	277.8	148.6	1.87	0.064
C/I	-1687.5	-843.8	148.6	-5.68	0.000
Rot/day*num_Base	-146.8	-73.4	148.6	-0.49	0.622
Rot/day*TBF	4.6	2.3	148.6	0.02	0.988
Rot/day*TBR	-278.7	-139.3	148.6	-0.94	0.350
Rot/day*num_DIS	2696.8	1348.4	148.6	9.07	0.000
Rot/day*PCF	-351.0	-175.5	148.6	-1.18	0.240
Rot/day*ISGS	726.3	363.2	148.6	2.44	0.016
Rot/day*CP	-1266.7	-633.3	148.6	-4.26	0.000
Rot/day*MDIBN	22.7	11.3	148.6	0.08	0.939
Rot/day*RS	578.0	289.0	148.6	1.94	0.054
Rot/day*RT	957.4	478.7	148.6	3.22	0.002
Rot/day*RDT	-843.8	-421.9	148.6	-2.84	0.005
Rot/day*MWBF	-29.0	-14.5	148.6	-0.10	0.922
Rot/day*tenure	635.1	317.5	148.6	2.14	0.034
Rot/day*C/I	-1383.1	-691.5	148.6	-4.65	0.000
num_Base*TBF	-820.0	-410.0	148.6	-2.76	0.007
num_Base*TBR	-117.3	-58.7	148.6	-0.39	0.694
num_Base*num_DIS	-203.6	-101.8	148.6	-0.68	0.495
num_Base*ISGS	-295.6	-147.8	148.6	-0.99	0.322
num_Base*CP	38.3	19.2	148.6	0.13	0.898
num_Base*MDIBN	147.6	73.8	148.6	0.50	0.620
num_Base*RS	-459.3	-229.7	148.6	-1.55	0.125
num_Base*RT	121.3	60.6	148.6	0.41	0.684
num_Base*RDT	-6.6	-3.3	148.6	-0.02	0.982
num_Base*tenure	-354.3	-177.2	148.6	-1.19	0.235
num_Base*C/I	238.9	119.5	148.6	0.80	0.423
TBF*TBR	-467.0	-233.5	148.6	-1.57	0.119
TBF*num_DIS	304.6	152.3	148.6	1.02	0.307
TBF*ISGS	360.6	180.3	148.6	1.21	0.227
TBF*RS	-79.7	-39.9	148.6	-0.27	0.789
TBF*RT	238.6	119.3	148.6	0.80	0.424
TBF*tenure	170.3	85.2	148.6	0.57	0.568
TBF*C/I	123.8	61.9	148.6	0.42	0.678
TBR*num_DIS	-265.4	-132.7	148.6	-0.89	0.374
TBR*RS	-765.6	-382.8	148.6	-2.58	0.011
TBR*tenure	-892.8	-446.4	148.6	-3.00	0.003
TBR*C/I	-5.8	-2.9	148.6	-0.02	0.984
num_DIS*C/I	-1524.3	-762.2	148.6	-5.13	0.000
ISGS*RS	49.7	24.8	148.6	0.17	0.867
ISGS*RDT	-355.0	-177.5	148.6	-1.19	0.235
ISGS*MWBF	195.0	97.5	148.6	0.66	0.513
CP*RS	-304.7	-152.4	148.6	-1.03	0.307
CP*MWBF	-822.0	-411.0	148.6	-2.77	0.007
MDIBN*RS	366.0	183.0	148.6	1.23	0.220

Analysis of Variance for TST (coded units)

Source	DF	Seq SS	Adj SS	Adj MS	F	P
Main Effects	15	1563944742	1563944742	104262983	24.58	0.000
2-Way Interactions	43	986337955	986337955	22938092	5.41	0.000
Residual Error	133	564223985	564223985	4242286		
Lack of Fit	5	87228849	87228849	17445770	4.68	0.001
Pure Error	128	476995136	476995136	3726525		
Total	191	3114506682				

Unusual Observations for TST

Obs	TST	Fit	SE Fit	Residual	St Resid
106	11506.0	6902.5	1141.8	4603.5	2.69R
120	3956.0	7939.1	1141.8	-3983.1	-2.32R
127	30999.0	18677.7	1141.8	12321.3	7.19R
128	9028.0	18677.7	1141.8	-9649.7	-5.63R
142	5564.0	9263.1	1141.8	-3699.1	-2.16R
144	14274.0	9263.1	1141.8	5010.9	2.92R
151	18194.0	9936.4	1141.8	8257.6	4.82R
189	11705.0	7725.1	1141.8	3979.9	2.32R

R denotes an observation with a large standardized residual

Estimated Effects and Coefficients for Number of Conjugacy Classes Visited

Term	Effect	Coef	SE Coef	T	P
Constant		895.6	71.17	12.58	0.000
Rot/day	331.2	165.6	71.17	2.33	0.021
num_Base	-62.6	-31.3	71.17	-0.44	0.661
TBF	-108.2	-54.1	71.17	-0.76	0.449
TBR	-61.5	-30.7	71.17	-0.43	0.667
num_DIS	1742.9	871.5	71.17	12.24	0.000
PCF	204.5	102.2	71.17	1.44	0.153
ISGS	179.7	89.8	71.17	1.26	0.209
CP	-544.1	-272.1	71.17	-3.82	0.000
MDIBN	-145.1	-72.5	71.17	-1.02	0.310
RS	395.9	198.0	71.17	2.78	0.006
RT	-470.3	-235.2	71.17	-3.30	0.001
RDT	-705.5	-352.7	71.17	-4.96	0.000
MWBF	-178.6	-89.3	71.17	-1.25	0.212
tenure	-209.4	-104.7	71.17	-1.47	0.144
C/I	-642.2	-321.1	71.17	-4.51	0.000
Rot/day*num_Base	28.4	14.2	71.17	0.20	0.842
Rot/day*TBF	-25.0	-12.5	71.17	-0.18	0.861
Rot/day*TBR	-264.0	-132.0	71.17	-1.85	0.066
Rot/day*num_DIS	320.0	160.0	71.17	2.25	0.026
Rot/day*PCF	-75.0	-37.5	71.17	-0.53	0.599
Rot/day*ISGS	-440.5	-220.2	71.17	-3.09	0.002
Rot/day*CP	-677.2	-338.6	71.17	-4.76	0.000
Rot/day*MDIBN	-168.2	-84.1	71.17	-1.18	0.239
Rot/day*RS	-204.0	-102.0	71.17	-1.43	0.154
Rot/day*RT	171.0	85.5	71.17	1.20	0.232
Rot/day*RDT	-545.2	-272.6	71.17	-3.83	0.000

Rot/day*MWBF	-148.2	-74.1	71.17	-1.04	0.300
Rot/day*tenure	379.3	189.7	71.17	2.66	0.009
Rot/day*C/I	-159.6	-79.8	71.17	-1.12	0.264
num_Base*TBF	217.8	108.9	71.17	1.53	0.128
num_Base*TBR	367.7	183.8	71.17	2.58	0.011
num_Base*num_DIS	-56.6	-28.3	71.17	-0.40	0.691
num_Base*ISGS	-69.6	-34.8	71.17	-0.49	0.626
num_Base*CP	258.6	129.3	71.17	1.82	0.072
num_Base*MDIBN	204.8	102.4	71.17	1.44	0.153
num_Base*RS	-10.8	-5.4	71.17	-0.08	0.940
num_Base*RT	256.1	128.1	71.17	1.80	0.074
num_Base*RDT	-135.8	-67.9	71.17	-0.95	0.342
num_Base*tenure	42.9	21.5	71.17	0.30	0.764
num_Base*C/I	103.3	51.6	71.17	0.73	0.469
TBF*TBR	11.0	5.5	71.17	0.08	0.939
TBF*num_DIS	-98.9	-49.5	71.17	-0.70	0.488
TBF*ISGS	114.8	57.4	71.17	0.81	0.422
TBF*RS	359.7	179.8	71.17	2.53	0.013
TBF*RT	114.4	57.2	71.17	0.80	0.423
TBF*tenure	455.7	227.8	71.17	3.20	0.002
TBF*C/I	249.2	124.6	71.17	1.75	0.082
TBR*num_DIS	-55.0	-27.5	71.17	-0.39	0.700
TBR*RS	212.9	106.4	71.17	1.50	0.137
TBR*tenure	-129.2	-64.6	71.17	-0.91	0.366
TBR*C/I	-148.0	-74.0	71.17	-1.04	0.300
num_DIS*C/I	-645.0	-322.5	71.17	-4.53	0.000
ISGS*RS	261.2	130.6	71.17	1.83	0.069
ISGS*RDT	39.6	19.8	71.17	0.28	0.782
ISGS*MWBF	453.6	226.8	71.17	3.19	0.002
CP*RS	-69.4	-34.7	71.17	-0.49	0.627
CP*MWBF	-126.6	-63.3	71.17	-0.89	0.376
MDIBN*RS	118.9	59.4	71.17	0.84	0.405

Analysis of Variance for num_CC_V (coded units)

Source	DF	Seq SS	Adj SS	Adj MS	F	P
Main Effects	15	236250701	236250701	15750047	16.19	0.000
2-Way Interactions	43	147087307	147087307	3420635	3.52	0.000
Residual Error	133	129361659	129361659	972644		
Lack of Fit	5	4914271	4914271	982854	1.01	0.414
Pure Error	128	124447389	124447389	972245		
Total	191	512699666				

Unusual Observations for num_CC_V

Obs	num_CC_V	Fit	SE Fit	Residual	St Resid
22	10259.0	4728.9	546.7	5530.1	6.74R
23	2237.0	4728.9	546.7	-2491.9	-3.04R
24	1981.0	4728.9	546.7	-2747.9	-3.35R
95	1459.0	3853.4	546.7	-2394.4	-2.92R
96	7662.0	3853.4	546.7	3808.6	4.64R
106	8527.0	6464.0	546.7	2063.0	2.51R
107	4802.0	6464.0	546.7	-1662.0	-2.02R
127	8278.0	4435.3	546.7	3842.7	4.68R
128	631.0	4435.3	546.7	-3804.3	-4.63R
166	2198.0	3847.6	546.7	-1649.6	-2.01R

188 2856.0 4734.6 546.7 -1878.6 -2.29R

R denotes an observation with a large standardized residual

Estimated Effects and Coefficients for Average Neighborhood Size

Term	Effect	Coef	SE Coef	T	P
Constant		1822.3	28.72	63.45	0.000
Rot/day	1887.5	943.8	28.72	32.86	0.000
num_Base	-439.8	-219.9	28.72	-7.66	0.000
TBF	59.0	29.5	28.72	1.03	0.307
TBR	-24.1	-12.0	28.72	-0.42	0.676
num_DIS	2643.3	1321.7	28.72	46.02	0.000
PCF	-61.8	-30.9	28.72	-1.08	0.284
ISGS	-145.9	-73.0	28.72	-2.54	0.012
CP	-161.3	-80.7	28.72	-2.81	0.006
MDIBN	117.3	58.6	28.72	2.04	0.043
RS	20.6	10.3	28.72	0.36	0.720
RT	-50.1	-25.1	28.72	-0.87	0.385
RDT	-149.7	-74.8	28.72	-2.61	0.010
MWBF	210.2	105.1	28.72	3.66	0.000
tenure	-108.1	-54.0	28.72	-1.88	0.062
C/I	-134.6	-67.3	28.72	-2.34	0.021
Rot/day*num_Base	-344.0	-172.0	28.72	-5.99	0.000
Rot/day*TBF	-7.3	-3.7	28.72	-0.13	0.899
Rot/day*TBR	0.6	0.3	28.72	0.01	0.992
Rot/day*num_DIS	1351.7	675.8	28.72	23.53	0.000
Rot/day*PCF	-14.5	-7.3	28.72	-0.25	0.801
Rot/day*ISGS	-190.8	-95.4	28.72	-3.32	0.001
Rot/day*CP	-433.3	-216.7	28.72	-7.54	0.000
Rot/day*MDIBN	109.0	54.5	28.72	1.90	0.060
Rot/day*RS	-84.3	-42.1	28.72	-1.47	0.145
Rot/day*RT	-59.7	-29.9	28.72	-1.04	0.300
Rot/day*RDT	-25.1	-12.5	28.72	-0.44	0.663
Rot/day*MWBF	167.4	83.7	28.72	2.91	0.004
Rot/day*tenure	-66.0	-33.0	28.72	-1.15	0.252
Rot/day*C/I	-126.0	-63.0	28.72	-2.19	0.030
num_Base*TBF	37.7	18.9	28.72	0.66	0.513
num_Base*TBR	-122.2	-61.1	28.72	-2.13	0.035
num_Base*num_DIS	-380.3	-190.1	28.72	-6.62	0.000
num_Base*ISGS	-92.8	-46.4	28.72	-1.62	0.109
num_Base*CP	-93.1	-46.6	28.72	-1.62	0.107
num_Base*MDIBN	-29.7	-14.8	28.72	-0.52	0.606
num_Base*RS	-107.1	-53.6	28.72	-1.86	0.064
num_Base*RT	126.8	63.4	28.72	2.21	0.029
num_Base*RDT	-3.7	-1.8	28.72	-0.06	0.949
num_Base*tenure	2.4	1.2	28.72	0.04	0.967
num_Base*C/I	27.4	13.7	28.72	0.48	0.634
TBF*TBR	-25.1	-12.6	28.72	-0.44	0.663
TBF*num_DIS	76.6	38.3	28.72	1.33	0.185
TBF*ISGS	54.9	27.4	28.72	0.95	0.341
TBF*RS	-41.7	-20.8	28.72	-0.73	0.469
TBF*RT	42.1	21.1	28.72	0.73	0.464
TBF*tenure	-70.8	-35.4	28.72	-1.23	0.220

TBF*C/I	30.7	15.4	28.72	0.53	0.594
TBR*num_DIS	-39.7	-19.9	28.72	-0.69	0.490
TBR*RS	-42.5	-21.2	28.72	-0.74	0.461
TBR*tenure	56.0	28.0	28.72	0.97	0.331
TBR*C/I	34.0	17.0	28.72	0.59	0.555
num_DIS*C/I	-188.9	-94.5	28.72	-3.29	0.001
ISGS*RS	-90.0	-45.0	28.72	-1.57	0.120
ISGS*RDT	-49.0	-24.5	28.72	-0.85	0.395
ISGS*MWBF	-26.8	-13.4	28.72	-0.47	0.642
CP*RS	-6.4	-3.2	28.72	-0.11	0.912
CP*MWBF	17.7	8.9	28.72	0.31	0.758
MDIBN*RS	80.6	40.3	28.72	1.40	0.163

Analysis of Variance for Ave_NS (coded units)

Source	DF	Seq SS	Adj SS	Adj MS	F	P
Main Effects	15	523762644	523762644	34917510	220.44	0.000
2-Way Interactions	43	121399161	121399161	2823236	17.82	0.000
Residual Error	133	21066726	21066726	158396		
Lack of Fit	5	5582136	5582136	1116427	9.23	0.000
Pure Error	128	15484590	15484590	120973		
Total	191	666228531				

Unusual Observations for Ave_NS

Obs	Ave_NS	Fit	SE Fit	Residual	St Resid
57	1991.00	1255.08	220.62	735.92	2.22R
107	6731.00	5779.40	220.62	951.60	2.87R
108	5072.00	5779.40	220.62	-707.40	-2.14R
115	7004.00	6012.17	220.62	991.83	2.99R
119	5574.00	4759.31	220.62	814.69	2.46R
130	5768.00	4508.54	220.62	1259.46	3.80R
139	6786.00	6092.31	220.62	693.69	2.09R
143	5586.00	4915.42	220.62	670.58	2.02R
154	3567.00	4818.88	220.62	-1251.88	-3.78R
155	5921.00	4818.88	220.62	1102.12	3.33R
187	3493.00	4438.08	220.62	-945.08	-2.85R
189	5171.00	4438.08	220.62	732.92	2.21R

R denotes an observation with a large standardized residual

Estimated Effects and Coefficients for Average Tenure

Term	Effect	Coef	SE Coef	T	P
Constant		2541	134.3	18.92	0.000
Rot/day	1031	516	134.3	3.84	0.000
num_Base	-72	-36	134.3	-0.27	0.788
TBF	-11	-6	134.3	-0.04	0.967
TBR	-71	-36	134.3	-0.27	0.791
num_DIS	1339	669	134.3	4.98	0.000
PCF	247	123	134.3	0.92	0.360
ISGS	1474	737	134.3	5.49	0.000
CP	-20	-10	134.3	-0.07	0.941
MDIBN	-118	-59	134.3	-0.44	0.662
RS	521	260	134.3	1.94	0.055

RT	-172	-86	134.3	-0.64	0.522
RDT	-760	-380	134.3	-2.83	0.005
MWBF	-127	-64	134.3	-0.47	0.636
tenure	737	369	134.3	2.74	0.007
C/I	-4116	-2058	134.3	-15.32	0.000
Rot/day*num_Base	-109	-54	134.3	-0.40	0.686
Rot/day*TBF	13	7	134.3	0.05	0.961
Rot/day*TBR	-53	-26	134.3	-0.20	0.845
Rot/day*num_DIS	7	4	134.3	0.03	0.978
Rot/day*PCF	-299	-150	134.3	-1.11	0.267
Rot/day*ISGS	579	289	134.3	2.15	0.033
Rot/day*CP	-50	-25	134.3	-0.19	0.852
Rot/day*MDIBN	355	178	134.3	1.32	0.188
Rot/day*RS	232	116	134.3	0.86	0.390
Rot/day*RT	214	107	134.3	0.80	0.427
Rot/day*RDT	-203	-102	134.3	-0.76	0.451
Rot/day*MWBF	-146	-73	134.3	-0.54	0.588
Rot/day*tenure	436	218	134.3	1.62	0.107
Rot/day*C/I	-814	-407	134.3	-3.03	0.003
num_Base*TBF	-644	-322	134.3	-2.40	0.018
num_Base*TBR	-117	-58	134.3	-0.43	0.665
num_Base*num_DIS	139	69	134.3	0.52	0.606
num_Base*ISGS	-179	-89	134.3	-0.67	0.507
num_Base*CP	-26	-13	134.3	-0.10	0.923
num_Base*MDIBN	76	38	134.3	0.28	0.777
num_Base*RS	58	29	134.3	0.21	0.831
num_Base*RT	-31	-15	134.3	-0.11	0.909
num_Base*RDT	-116	-58	134.3	-0.43	0.666
num_Base*tenure	75	37	134.3	0.28	0.782
num_Base*C/I	32	16	134.3	0.12	0.904
TBF*TBR	-374	-187	134.3	-1.39	0.167
TBF*num_DIS	70	35	134.3	0.26	0.794
TBF*ISGS	123	62	134.3	0.46	0.647
TBF*RS	617	309	134.3	2.30	0.023
TBF*RT	-95	-47	134.3	-0.35	0.725
TBF*tenure	69	34	134.3	0.26	0.798
TBF*C/I	39	20	134.3	0.15	0.884
TBR*num_DIS	130	65	134.3	0.48	0.630
TBR*RS	34	17	134.3	0.13	0.900
TBR*tenure	-1333	-666	134.3	-4.96	0.000
TBR*C/I	169	84	134.3	0.63	0.531
num_DIS*C/I	-841	-421	134.3	-3.13	0.002
ISGS*RS	50	25	134.3	0.19	0.853
ISGS*RDT	205	102	134.3	0.76	0.447
ISGS*MWBF	239	120	134.3	0.89	0.374
CP*RS	-544	-272	134.3	-2.03	0.045
CP*MWBF	-195	-97	134.3	-0.73	0.469
MDIBN*RS	169	85	134.3	0.63	0.530

Analysis of Variance for Ave_Tenu (coded units)

Source	DF	Seq SS	Adj SS	Adj MS	F	P
Main Effects	15	1127671812	1127671812	75178121	21.71	0.000
2-Way Interactions	43	270872092	270872092	6299351	1.82	0.005
Residual Error	133	460654961	460654961	3463571		
Lack of Fit	5	14645386	14645386	2929077	0.84	0.523

Pure Error	128	446009575	446009575	3484450
Total	191	1859198864		

Unusual Observations for Ave_Tenu

Obs	Ave_Tenu	Fit	SE Fit	Residual	St Resid
113	8361.0	4315.6	1031.7	4045.4	2.61R
124	2765.0	6304.7	1031.7	-3539.7	-2.29R
125	10314.0	6304.7	1031.7	4009.3	2.59R
127	17714.0	11168.1	1031.7	6545.9	4.23R
128	5465.0	11168.1	1031.7	-5703.1	-3.68R
134	1969.0	6274.9	1031.7	-4305.9	-2.78R
135	10812.0	6274.9	1031.7	4537.1	2.93R
142	2885.0	7353.4	1031.7	-4468.4	-2.88R
144	12522.0	7353.4	1031.7	5168.6	3.34R
149	14391.0	7131.3	1031.7	7259.7	4.69R
150	2833.0	7131.3	1031.7	-4298.3	-2.77R
151	12921.0	8266.4	1031.7	4654.6	3.01R

R denotes an observation with a large standardized residual

APPENDIX H: Optimality Results on Smaller TCSPs

Design Point	% Distance ATS Crews	% Distance ATS Wait Time	Optimality Status
1	7.69	1.25	Optimal
2	9.09	7.77	Optimal
3	13.33	15.77	Optimal
13	7.69	6.55	Optimal
14	20.00	24.08	Optimal
15	0	0.47	Optimal
29	5.56	6.01	Optimal
40	0	0.43	Optimal
41	0	7.46	Optimal
42	0	5.69	Optimal
50	6.67	4.91	Optimal
51	0	4.36	Optimal
62	4.76	3.91	Optimal
66	4.35	5.13	Optimal
76	4.35	3.01	Optimal
77	11.11	9.23	Optimal
89	7.69	5.11	Optimal
90	0	6.12	Optimal
100	3.85	8.60	Optimal
101	18.18	21.50	Sub-optimal
102	4.17	5.33	Sub-optimal
113	3.57	7.59	Optimal
114	10.71	6.39	Optimal
121	0	8.23	Sub-optimal
122	3.23	2.91	Optimal
123	3.03	2.95	Optimal
133	3.85	5.35	Optimal
134	15.38	17.48	Sub-optimal
135	3.45	0.36	Optimal
148	4.00	7.11	Optimal
149	8.33	2.28	Optimal
157	0	1.46	Optimal
158	2.38	1.81	Optimal
159	0	0.06	Optimal
160	2.44	0.97	Optimal
161	0	1.44	Optimal
169	2.63	2.06	Optimal

171	2.38	0.54	Optimal
173	0	0.48	Optimal
174	0	1.08	Optimal
181	0	2.96	Optimal
182	4.76	2.70	Optimal
183	10.53	7.33	Optimal

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