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A FORMAL SPECIFICATION AND PROOF OF SYSTEM SAFETY USING THE SCHEMATIC PROTECTION MODEL

THESIS

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AFIT/GCS/ENG/08-21

A FORMAL SPECIFICATION AND PROOF OF SYSTEM SAFETY USING THE SCHEMATIC PROTECTION MODEL

THESIS

Presented to the Faculty

Department of Electrical and Computer Engineering

Graduate School of Engineering and Management

Air Force Institute of Technology

Air University

Air Education and Training Command

In Partial Fulfillment of the Requirements for the

Degree of Master of Science in Computer Science

Raymond S. Way, BS

Captain, USAF

March 2008

APPROVED FOR PUBLIC RELEASE; DISTRIBUTION UNLIMITED.

AFIT/GCS/ENG/08-21

A FORMAL SPECIFICATION AND PROOF OF SYSTEM SAFETY

USING THE SCHEMATIC PROTECTION MODEL

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Abstract

This research formally specifies the Schematic Protection Model (SPM) and provides a sound, flexible tool for reasoning formally about systems that implement a security model like SPM, to prove its ability to provide security services such as confidentiality and integrity. The theory described by the resultant model was logically proved in the Prototype Verification System (PVS), an automated prover. Each component of SPM was tested, as were several anomalous conditions, and each test produced results consistent with the model.

The model is internally modular, and therefore easily extensible, yet cohesive since the theory to be proved encompasses the entire specification. This approach ensures the specification is flexible enough to incorporate any extensions that can be expressed algorithmically, such as the deontic logic properties of obligation, permission, possibility and necessity. Furthermore, the modularity enhances the robustness of the model to ensure that previously-proved fundamental properties are not lost in the process of adding functionality.

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A FORMAL SPECIFICATION AND PROOF OF SYSTEM SAFETY USING THE SCHEMATIC PROTECTION MODEL

I. Introduction

Background

Cyber technology has seen great advances in last 20 years. The ability to create complex systems, and to combine the capabilities of individual systems into massively interconnected distributed systems has far outpaced the ability to model cyber systems and reason formally about their security properties. Formal modeling and analysis has established the security properties of small-scale subsystems such as cryptographic and authentication protocols, and modeled the safety properties of some highly reliable systems [Bal07]. Techniques in these specialized areas have kept pace with technological progress, and they are used successfully today. But the formal modeling and analysis of security properties of systems in cyberspace, such as computers, networks, or complex distributed systems has not advanced at the same pace. Two system security models, the Take-Grant model and the Schematic Protection Model, were developed in 1977 and 1988, respectively [Bis03]. These models have changed little since their introduction, and as a result, are rarely used in practice to analyze real-world systems.

Even so, the Schematic Protection Model still provides a sound and wellunderstood theoretical model, which can be formally specified to model contemporary cyber systems.

The demonstrated usefulness of formal modeling and analysis in the security and safety of protocols and the corresponding lack of progress in the establishing analogous properties in the cyber arena indicate a new approach may be warranted [Bal07].

Research Objective

The objective of this research is to develop a formal specification that implements the Schematic Protection Model, and can verify whether a given protection scheme correctly implements a specified security policy.

Overview

Introduction.

This chapter introduces the research problem and explains how this research advances the state of the art using an automated tool for formally reasoning about the safety of systems specified in the Schematic Protection Model (SPM). The developed Prototype Verification System specification supports future research by incorporating additional *virtual processor* modules. These modules support additional functionality that can be described in an algorithm and translated into the PVS language through a sequential coding paradigm.

Literature Review.

Chapter II introduces logic systems, focusing primarily on propositional and predicate logic systems as a means of describing the underlying higher-order sequent calculus engine of the PVS prover. The chapter discusses modal logics, specifically deontic logic, in response to limitations of the aforementioned classical logic systems. Extending SPM with deontic logic is recommended for future research.

SPM provides the means to describe an abstract system, including entities that comprise the system and the rules by which they interact. These rules describe the conditions under which the system can transition from one state to another, and consequently, allow it to be determined whether a particular state is reachable. It is this characteristic that enables a proof that a system in a known initial state cannot end up in an unsecure state.

The PVS specification language, its integrated support tools and theorem prover are described. This tool was selected largely due to the empirical examination of various automated verification systems done by Sonali Ubhayakar in 2003 [Ubh03].

The sequential programming paradigm, contrasted with the now more familiar object-oriented mindset, is used to formulate linear algorithms to be translated into assembly-like pseudocode that describes the desired behavior of the model. This pseudocode is translated into a PVS specification that implements the state machine presented by this research.

Specification of the Schematic Protection Model.

Chapter III presents a Prototype Verification System specification of the Schematic Protection Model followed by an annotated version of the specification itself.

The specification is considered in three parts, the first being initialization. The initialization process declares datatypes and the variables that use them. It includes system state initialization and setup functions common to any autonomous state machine being considered in the model. The second and third parts each represent autonomous state machines that implement rights transfer and entity creation, respectively, in SPM.

The description is followed by the specification itself, including the PVS statements with annotations. The results are presented using PVS-prover output, followed by an analysis that includes an overview of the proof sequence.

Schematic Protection Model Validation Scenarios.

Chapter IV presents a series of exceptional conditions within the SPM and their respective formal specifications in PVS to demonstrate that the safety of the system is preserved. These conditions test the model's ability to prevent an unsecure state transition.

Conclusion.

This research produces a formal specification that correctly implements SPM. This specification was designed to be robust, yet flexible as it will accept modular, autonomous additions in support of additional SPM modeling capabilities.

SPM specifications are a promising area for future research; they offer an established foundation from which to proceed. The use of deontic logic to reason about system properties is proposed for future research. Deontic logic provides the foundation for reasoning about obligation, permission, possibility and necessity, and is therefore expected to satisfy certain requirements that SPM itself cannot.

II. Literature Review

Logic Systems

Propositional Logic.

Propositional logic is a system of formulating and combining propositions using atomic variables, logical operators, axioms, and rules of inference. Atomic variables are declarative statements (i.e., *propositions*) such that, when their relationships are resolved in accordance with the system's axioms and inference rules, a determination of TRUTH or FALSITY can be made about the compound statement. Logical operators are considered in a prescribed order of precedence to ensure that no ambiguity exists. The axioms/rules must be both *sound* (all compound statements that resolve to TRUE *are*, in fact, true) and *complete* (any compound statement that is true can be determined to be TRUE by applying some combination of these axioms/rules.)

For example, using the atomic statements p and q, logical operators can be used to derive the familiar truth tables in Figure 1.

р	q	$\mathbf{p} \wedge \mathbf{q}$
Т	Т	Т
Т	F	F
F	Т	F
F	F	F

р	q	$\mathbf{p} \lor \mathbf{q}$
Т	Т	Т
Т	F	Т
F	Т	Т
F	F	F

р	¬p
Т	F
F	Т

Т
Т

р	q	$\mathbf{p} \rightarrow \mathbf{d}$
Т	Т	Т
Т	F	F
F	Т	Т
F	F	Т



Figure 1. Propositional Truth Tables

Predicate Logic.

Although propositional logic can represent simple relationships like *and*, *or*, *not*, and *if*... *then*, it cannot represent more complex notions such as *for all* x (\forall x), *there exists* x (\exists x), or concepts like *only*, and *at least* over a range of values. Predicate logic uses variables, functions, and constants to represent these more complex ideas. Variables represent atomic ideas, or propositions, as they do in propositional logic. Functions are used to express relationships between the variables. For example, **Taller**(x, y) might be used to mean x *is taller than* y, and would resolve to TRUE in a compound statement where that, in fact, held. Constants can be thought of as functions with no arguments, simply returning their default value when invoked.

Modal Logics.

The propositional and predicate (aka classical) logics are the foundation for most formal models, where the truth about some aspect of the system is reduced to TRUE, FALSE, or perhaps UNDECIDABLE. That is, a property holds (is TRUE), does not hold (is FALSE), or cannot be determined whether it holds (is UNDECIDABLE). Classical logic cannot effectively support reasoning about systems where, for example; a property *should* hold, where some agent is obliged to *see to it that* something occurs, or where a property is possible or, conversely, is necessary. Furthermore, classical logic does not support temporal reasoning. Rather, it reasons about a snapshot of the system at some point in time. That is, if a property is TRUE under given conditions, it is always TRUE for those conditions [Bal07]. Additionally, technical deficiencies in classical logic when reasoning about security have been identified [ChM06], including the well-known semantic paradox of material implication, the most troublesome example of which is that a false antecedent implies any consequent that follows. Imagine trying to reason about

the security of a critical system in which Authenticated=FALSE implies Authorized=TRUE. The system using this logic would allow any action to be accomplished by any entity, as long as they had *not* been properly authenticated first.

Reasoning about trust among distributed systems that must each perform certain actions to achieve a goal (but in fact may not) can be modeled using notions of obligation, permission, possibility, and necessity from deontic logic. Extending the SPM with deontic logic is a promising area for further research.

The fundamental task of this research is to create a sound formal specification that captures the semantics of the Schematic Protection Model, which will ultimately enable formal modeling, analysis, and reasoning about various aspects of cyberspace security.

The Schematic Protection Model

Introduction.

To determine the protection state of a system, rules that allow or prevent transitions from one state to another must be described. With this structured framework, or *schema*, it can be proven whether an unsecure state can be reached from a given initial state. The Schematic Protection Model (SPM) introduces one such framework for modeling an abstract system's security-related interrelationships.

In SPM, entities within the system are anything that can act or be acted upon, such as a user, a file, or a printer. These entities are classified and labeled according to their *protection type* upon creation, which does not change for the life of that entity. The entity also has associated with it zero or more *tickets* that collectively constrain the ways in which the entity can act to trigger events within the system. Each ticket identifies a single right and the target-entity to which that right applies. For example, if an entity possesses

the ticket Y/z, then the entity has z rights over the entity Y, or stated another way; the ability to do z to Y. The set of all tickets that an entity has is in its possession is the *domain* of that entity. Rights belong to one of two broad categories: inert rights or control rights. Inert rights are those that, when exercised, have no effect on the security state of the system (e.g., an authorized *read* or *write* operation). Control rights are those that, when exercised, can affect the security state of the system (e.g., creating a new entity). Rights are of interest as they describe the events that are *allowed* within the system, and thus describe whether a violation of security policy is possible in a given state. If the domains were static, this would conclude the analysis, but one of the allowable events is the transfer of a ticket, which alters the reachable states, making further safety analysis necessary.

Rights can be transferred between entities if-and-only-if three conditions hold: the initiating entity has in its domain a copyable version of the ticket, there is a *link* between the entities, and there is an associated system policy, or *filter function*, which explicitly allows the transfer. SPM differentiates between nontransferable and transferable rights with the *copy flag*. That is, the transferable right **r** over file **F** would be designated by the ticket **F**/**rc** as opposed to the noncopyable **F**/**r**.

Domains.

Every entity in the system has associated with it a set of tickets that collectively describe how it can interact with other entities. A ticket is a tuple of the target entity and the associated right, as described above. Each right r has an associated copyable right rc [Bis03, pg. 66]. An entity need only possess the ticket X/r to exercise the right r over X,

but to copy the ticket to another entity, the initiator must possess the associated ticket X/rc in its own domain.

Links.

A link predicate defines a relationship between two subjects in the context of the tickets in their respective domains, and determines whether there is a link between the two. A link predicate is a conjunction or disjunction (but not a negation) of the following terms for any control right z [Bis03, pg. 67]

$$X/z \in \operatorname{dom}(X) \tag{1}$$

$$X/z \in \operatorname{dom}(Y) \tag{2}$$

$$Y/z \in \operatorname{dom}(X) \tag{3}$$

$$Y/z \in \operatorname{dom}(Y) \tag{4}$$

$$TRUE (5)$$

where dom(X) is the set of tickets that X possesses.

For example, the following link predicate establishes a link from X to Y, iff the ticket X/z is in Y's domain

$$link(X, Y) = X/z \in dom(Y).$$
(6)

The predicate link(X, Y) = TRUE is a universal link and establishes a link from X to Y unconditionally. The existence of a valid link satisfies one of the three conditions that must hold for a ticket transfer to take place. The action must also be allowed by a *filter function* associated with the type of link, determined by the *protection types* of the associated entities.

Filters.

The *filter function* specifies the rights that may be transferred across the associated link. The factors that determine whether to allow the operation are the entity's *protection types* (including that of the target entity, which may not be one of the two involved in the transfer) and the right to be transferred. For example, for *superuser* \mathbf{X} to transfer a copyable read permission (**rc**) over *file* \mathbf{F} to *user* \mathbf{Y} , the link established in the preceding paragraph between \mathbf{X} and \mathbf{Y} would have to have the following filter

$$f(superuser, user) = \{ file/\mathbf{rc} \}$$
(7)

where **rc** denotes a *read* right with an associated *copy flag*.

To preserve the principle of *attenuation of privilege*, "no entity may have more rights than its creator" [Bis03, pg. 71], an entity must possess a right itself before it can transfer that right to another. This prevents the proliferation of privileges that would occur with no such constraint. Accordingly, for **X** to copy the ticket **F/rc** to **Y**, it must be true that $\mathbf{F/rc} \in dom(\mathbf{X})$ in the first place.

Creates.

The means by which new entities are created has important implications for the integrity of the system. New entities and their respective privileges introduce combinatoric relationships among system entities that could make safety analysis intractable. In SPM, create-events are controlled by *can-create* relations between entity types, and associated *create-rules* that are invoked upon creation.

The set of entity-types T is partitioned into a *subject set* TS and an *object set* TO [Bis03, pg. 66]. An entity *a* can create another entity *b* iff the can-create relation cc(a,b) exists such that $cc \subseteq TS \times T$. For example, for subject **X** to create object **F** (where **X** is of

type *user* and **F** is of type *file*), the tuple (user, file) must be in the *can-create* relation cc(user, file). Furthermore, for any *can-create* relation, say, (a, b), neither entities of type *b* nor any descendent (if the *b-type* entity creates other entities) can create an entity of protection-type *a*. This acyclic-create restriction is a characteristic of SPM that makes analysis tractable.

A *create-rule* determines which tickets are assigned to the parent and the child entities after a create. For example, the *create-rule* $\mathbf{cr}(a, b)$ is comprised of two subrules: $\mathbf{cr}_{p}(a, b)$ and $\mathbf{cr}_{c}(a, b)$, which specify the tickets the parent and child get upon creation. To preserve *attenuation of privilege*, the child cannot be given any privileges the parent doesn't have. If necessary, the parent can be assigned new tickets at creation-time before, in turn, granting them to the child.

As an acyclic attenuating scheme, the Schematic Protection Model can determine the safety of certain classes of systems. Representing this scheme in an automated verification system such as the Prototype Verification System allows the constraints and capabilities represented therein to be explored.

The Prototype Verification System (PVS)

The requirements or high-level design of many systems (perhaps any system, at a high enough level of abstraction) can be modeled as a state machine. Doing so introduces an abstract representation of the dynamic system-state and a set of operations that can be used to manipulate it. These operations transition the system from one state to another in response to external inputs and their influence on internal logic.

The development of a state machine representation requires a robust and systemrelevant collection of type definitions to build the state description. Additional types,

constants, and functions are needed to support subsequent formalization of the operations that act on the state. These state operations, themselves, are functions that take the system from one state to another or, more generally, that operate as structured relationships between states. Many times an *invariant* to the system state is provided to formalize the notion of a *well-defined* system state. This invariant is shown to hold in the presence of arbitrary operations on the state, assuming it holds prior to the operation. Other properties may be expressed as predicates over the system state and operations, and can be proved as *putative theorems* that follow from the formalization [NAS93].

PVS is a verification system. That is, a specification language integrated with support tools and a theorem prover. It represents the state-of-the-art in mechanized formal methods and can be used for significantly complex applications [SRI07]. Indeed, it has been used in numerous high-complexity research efforts around the world, both in academia and practical application [SRI08].

This research uses PVS to create logic-based models to verify whether a given protection scheme correctly implements a given security policy. The choice to use PVS was based, in part, on [Ubh03].

Automated Tool Selection.

Sonali Ubhayakar developed a methodology and a set of evaluation criteria to determine the utility of automated verification systems for the Naval Postgraduate School [Ubh03]. The ability of PVS to capture the properties of software systems and to provide a mapping between hierarchical levels of system abstractions, a necessary feature for understanding how a systems meets security objectives, was evaluated. Fifteen verification tools were tested based on prominence or specific characteristics of interest, according to the following criteria:

1) Age is an indicator of maturity/completeness. Tools that have been in use over a longer period of time are more likely to have been used and assessed for suitability for different applications. There is simply more data available which can be used to evaluate the tool.

2) Purpose, with a focus on the ability to describe software systems. Tools that are tailored to a specific class of problems, e.g., a particular mathematical property, were not considered to be good candidates.

3) Implementation language, with a focus on portability.

4) Resource requirements, with a focus on commonly available platforms such as a Windows- or Unix-based workstation with no extraordinary specifications. The availability of a suitable platform contributes to the tool's usefulness by minimizing cost and time to implement.

5) User friendliness. This is a trade-off between ease of use and degree of automation. The more completely automated the tool, the more limited it is in what it can verify. This part of the evaluation focused on the ability to use the tool without in-depth training on the language or mechanics of the tool.
6) User Interface. Related to user-friendliness, a well-designed graphical

interface is favored over a command-line interface.

Important characteristics identified for further research include:

1) User Presentation Language. The tool's usefulness is considered to be enhanced if its interface language is one that the user is already comfortable with and competent in.

 Consistency of specifications. A tool being used to uncover errors and inconsistencies in the correctness of a system must first be free of these same flaws. To the extent that the tool's correctness is suspect, so should be the results that it produces.

3) Executable specifications. The ability to construct and execute a potential solution allows the user to demonstrate the modeled system's behavior and more readily identify changes that need to be made.

4) Multiple levels of abstraction. The tool should be able to prove that the formal top-level specification, and the security policies that support it, together satisfy the overall security model for the system.

5) Expressiveness, described as the flexibility with which a tool can be applied to more complex and difficult problems. The expressiveness of PVS is enhanced by its support for the introduction of axioms.

PVS was selected after applying the empirical criteria above, specifically due to the amount of available documentation, the number of satisfied evaluation criteria, and the researcher's familiarity. "PVS can be used to specify and validate system requirements, verify that an implementation meets the requirements and then help to refine the design in an effort to improve system performance" [Ubh03].

PVS has an editing environment and an interactive theorem prover, which facilitate the development and debugging of specifications that can be formally shown to hold to explicitly stated properties. The prover includes powerful atomic and aggregate commands that apply rules of inference in a sequent calculus based on a higher-order predicate logic which allows predicates to take other predicates as arguments.

The PVS prover includes many commands to apply the rules of inference interactively at different stages of the proof. The proof begins with an assertion of the theorem to be proved, and proceeds sequentially through the sequent invoking the reduction tactic specified by the user. Selected commands that can be used to prove the SPM schematic are described below.

Split

The Split command separates conjunctive terms for individual consideration. For example, applying Split to the statement *A AND B* branches the proof into two separate subgoals from that point, one for statement *A* and one for *B*.

Expand.

The Expand command is used to expand and simplify the definition of a function during the proof. For example, the statement f(a, b) becomes a + b for the function

f(int x, int y) = x + y

Skolem.

Where the current sequent contains an existential antecedent, e.g., $\exists x(y(x))$, or a universal consequent, e.g., $\forall x(y(x))$; the Skolem command introduces a particular but arbitrarily chosen constant to represent *x* in the function *y()*. For example, $\forall x(y(x))$ is reduced to *y*(c), for the arbitrarily chosen constant *c*.

Flatten.

The Flatten command performs disjunctive simplification on the current sequent, transforming each formula into a list of expressions that is free of disjuncts by applying these transformations, as appropriate [Sha01]:

1) An antecedent formula $\neg A$ into the consequent formula A.

2) An antecedent formula $A \wedge B$ into the two antecedent formulas A and B.

3) A consequent formula $\neg A$ into the antecedent formula A.

4) A consequent formula $A \rightarrow B$ into the antecedent formula A and the consequent formula B.

5) A consequent formula $A \lor B$ into the two consequent formulas A and B.

6) An antecedent formula $A \Leftrightarrow B$ into the two antecedent formulas $A \rightarrow B$ and $B \rightarrow A$.

SkoSimp.

SkoSimp is an aggregate command that applies Skolem, and then Flatten.

Induct.

The Induct command produces base and induction cases from the target formula based on the data type of the target which must be a natural number or a PVS-language abstract datatype with an internally-defined induction scheme.

Rewrite.

Rewrite automatically determines required substitutions by matching the

conclusion of a named lemma, axiom, assumption, or function definition against

expressions in the current sequent.

Install-Rewrites.

Install-Rewrites can be used to invoke theories whose declarations are meant to be used as rules for applying the Rewrite command.

Bddsimp.

Binary decision diagram simplification repeatedly applies the propositional rules of inference to all the formulas in the sequent, to be reintroduced as a list of zero or more subgoal sequents.

Assert.

Assert applies internal decision procedures to prove trivial theorems, and to simplify complex linear arithmetic and boolean expressions.

Replace.

Replace substitutes formulas in the current sequent using an equality formula from the antecedent. If there is an antecedent formula x = y, Replace will substitute y for occurrences of x in a given target formula.

Inst?.

When the current sequent contains an existential consequent, e.g., $\exists x(y / x - 2))$, or a universal antecedent, e.g., $\forall x(y / x - 2))$; the Inst? command reduces them by instantiating the quantified variables with any matching terms having the same number of bound variables.

Skolem-typepred.

Like Skolem, with the additional function of adding any discovered type constraints on the introduced constants as antecedent formulas.

Lift-if.

Lift-if is a propositional reduction that brings the leftmost-innermost conditional expression to the outermost level. (e.g., [Sha01]),

```
f(IF(A;B;IF(C;D;E)))
```

is converted to the formula

```
IF(A; f(B); IF(C; f(D); f(E)))
```

Bash.

Bash is an aggregate command that executes assert, bddsimp, inst?, skolemtypepred, flatten, and lift-if, in that order.

Reduce.

Reduce is an aggregate command that applies bash followed by replace*, repeating the two until it has no effect.

Grind.

Grind is an aggregate command that can often complete a proof branch automatically using a combination of the aforementioned commands. Grind executes install-rewrites to install any given theories, rewrite rules, or relevant definitions. It then applies bddsimp, assert, replace*, and finally reduce.

Sequential Programming

To replicate the behavior of an abstract system that implements the Schematic Protection Model, it is helpful to envision the system's desired behavior using a sequential programming paradigm. The term *sequential programming* contrasts with the more familiar paradigm of object oriented (OO) design. To effectively reason about the system, it was necessary to abandon such higher-order abstractions and deal explicitly with the flow of logic through a virtual processor. SPM was initially modeled as a collection of sequential algorithms in a pseudocode similar to the C programming language that behaved as prescribed by the SPM under explicit initial conditions and known subsequent transitions. For example, the ownership test and the link test are shown in their initial form below:

```
void main(){
```

```
enum Right_type = {r, w}
 Right_type Right1
                     = r
 Right_type Right2
                     = w
 8-----
 enum ProtT_type = {Subj, Obj}
ProtT_type PType1 = Subj
ProtT_type PType2 = Obj
 ୫_____
 Record_ptr Ticket_type = [#
                       actor: Actor_type,
                       right: Right_type
                        #1
 8------
                    _____
 Ticket_type Ticket_Xr = [X, r]
 &_____
 Record_ptr Domain_type = [#
                    actor: Actor_type,
                    domain: setof[Ticket_type]
                    #1
 Domain_type Domain_X
 Domain_type Domain_Y
 ୫-----
 Record_ptr Link_type = [#
                    actor1: Actor_type,
                    actor2: Actor_type,
                    #1
 Set_ptr Links = setof[Link_type]
 %______
      State_OK = TRUE
 bool
 8_____
 add_Ticket([X, r], X);
 transfer([X, r], X, Y);
 IF (contains([X, r], dom(Y))) THEN State_OK = FALSE;
} //end main
bool linktest(Actor type A, Actor type B) {
 bool response = FALSE
 IF (contains([A, B], Links)) THEN response = TRUE;
 return(response);
}
Domain_type dom(Actor_type A) {
 return(domain | actor = A);
}
void add_Ticket(Ticket_type T, Actor_type A) {
 Domains = Domains WITH [add(domain, T) | actor = A]
}
```

These algorithms were translated into an assembly-like syntax, breaking down the

original flow-control constructs into comparisons and conditional jump statements.

```
_____
// Pseudo-SPM in goto format:
void main() {
11
    (initialize as described above)
L1:
    Domain_X`domain = Domain_X`domain WITH
          [add(Ticket_Xr, Domain_X`domain)]
//transfer [X, r] from X to Y
T.2:
    //test source domain for ticket
    IF (!(contains(Ticket_Xr, Domain_X`domain)))
    THEN goto L5
L3:
    //test for link
    IF (!(contains([X, Y], Links)))
    THEN goto L5
L4:
    //add [X, r] to Y
    Domain Y`domain = Domain Y`domain WITH
          [add(Ticket_Xr, Domain_Y`domain)]
    goto END
L5:
    IF (contains(Ticket_Xr, Domain_Y`domain))
    THEN State_OK = FALSE;
END:
}
```

The resultant pseudo-assembly code was directly translatable into PVS

instructions [CK01]. The example above supplied the logic flow for what eventually

became these transition functions for the transfer test state machine in the current

specification:

```
trans(snapshot: State_template): State_template =
    CASES snapshot`PC OF
         % Each case applies WITH conditions before passing
         % snapshot to the specified operation, then
         % returns snapshot.
         % set up initial state and increment PC
         L1_1: Init(snapshot) WITH [PC := L2_1],
         % set up test conditions and increment PC
         L2_1: Setup(snapshot) WITH [PC := L3_1],
         % verify that source entity has copyable ticket
         % and adjust PC
         L3_1: snapshot
                            WITH [PC :=
               IF (member(myfile_rc, snapshot`Domain(Bob)))
                   AND
                   myfile_rc`copyable?
                                                  THEN L4_1
                                                  ELSE L7_1
              ENDIF],
         % verify that link exists between source and
         % target/adjust PC
         L4_1: snapshot
                               WITH [PC :=
               IF Link?(snapshot, Bob, Alice)
                                                  THEN L5_1
                                                  ELSE L7 1
              ENDIF],
         % verify that a filter function allows this
         % transfer/adjust PC
         L5_1: snapshot
                                WITH [PC :=
              IF Filter?(snapshot, Bob,
                         Alice, myfile_rc)
                                                 THEN L6 1
                                                 ELSE L7_1
               ENDIF],
         % Execute the transfer and increment PC
         L6_1: Exec_1(snapshot) WITH [PC := L7_1],
         % Test State_OK and move PC to end
         L7 1: Test 1(snapshot) WITH [PC := LEND 1],
         LEND_1: snapshot
         ELSE
                 snapshot
    ENDCASES
```

Summary

Propositional and predicate logic systems are the fundamental underpinnings of the higher-order sequent calculus engine of the PVS prover. Modal logics, specifically deontic logic, represent a promising potential extension of SPM to model modern, complex cyber systems.

SPM is used to describe an abstract system. The model offers clearly defined rules through which we can prove the abstract system cannot enter a state that would violate the system security policies.

PVS is an interactive, semi-automated prover that proves the safety of the abstract system. This tool was weighed empirically against various other automated verification systems. It was found that PVS is well-suited to prove the safety properties of an abstract system that implements the security constraints described by SPM.

A sequential programming paradigm is used to develop the desired model behavior algorithmically in a way that is easily transferable to a PVS specification.

III. Specification of the Schematic Protection Model

Introduction

The PVS specification implementing SPM includes an initialization section, followed by two autonomous state machines. The state machines each represent a virtual processor against which state transition functions are applied, implementing the ticket transfer and entity creation operations, respectively. It is here that the flexibility of this design is realized. Additional autonomous virtual processors can be added as modules to implement any functionality that can be described algorithmically, and integrated with a reference to the new module in the comprehensive theory *System_correct* at the end of the specification. Then, PVS can formally reason about the behavior of the new module in the same context as the original modules. Because a single system state is shared among modules, it may be necessary to add state variables to support additional operations.

Specification Subprocesses

Initialization.

Since the PVS specification is interpreted sequentially, it begins with an initialization section in which datatypes that represent components of the SPM model are described. This is followed by the instantiation of variables using the declared datatypes. These are the named variables manipulated during validation of the specification.

The next section includes state initialization and setup operations. Two state transition functions are outside the scope of the autonomous virtual processor. These ensure the autonomous state machines used in the *System_correct* theory are applied to the same system under the same conditions.

The Ticket Transfer Process.

Transferring a ticket is contingent upon the results of three tests that together ensure that the transfer is not a violation of system policy and that the proposed new state of the system will remain secure.

Consider the PVS ticket transfer process in Figure 2 where *Bob* transfers *myfile/r* to *Alice*. The first test ensures that *Bob* has a copyable version of the ticket, which ensures that attenuation of privilege is preserved. The specification checks *Bob*'s domain to verify that it contains the ticket *myfile/rc*, which is the copyable version of ticket *myfile/r*.

The second test ensures there is a link between *Bob* and *Alice*. This is done by checking for a link predicate associated with the ordered pair (*Bob*, *Alice*).

The third test ensures that a *filter function* associated with the link allows the transfer of the ticket between entities with the respective protection-types of the originating- and target-entities. The test checks the set *Filters* for the element (*file*, r) associated with the tuple (*administrator*, *user*), all associated with the link (*Bob*, *Alice*) which are represented by their respective IDs (0, 1). Explicitly,

(file, r) \in Filters(0, 1)(administrator, user)

which states that ticket {X, r}, where X is an entity with the protection-type *file*, may be transferred from an entity of protection-type *administrator* to another of type *user*. Note that the actual entity identified in the ticket (X/r) is not identified in the *filter function*. Rather, the system policy applies only to the right itself and the *protection type* of the entity to which the right applies.

These three tests ensure that ticket transfers are well defined and attenuating. A transfer can occur between any two entities, such as a user or a printer, that can initiate or

be affected by actions that change the security state of the system. The transfer process is described in Figure 2 by *Bob*'s attempt to transfer a ticket to *Alice*. In this example *Bob* initiates a potential change to the system state, i.e., adding a ticket to *Alice*'s domain. If successful, the system will transition from the *pre-transfer* state to that identified as *post-transfer*, which includes *myfile/r* in *Alice*'s domain.



Figure 2. The Ticket Transfer Process

The Create Process.

Creating a new entity in the PVS specification is contingent upon that creation not being a violation of system policy. In Figure 3, *Bob* initiates the creation of *LaserJet_1* of type *printer*. A system policy, in the form of a *can-create* relation, specifies whether an entity of protection-type *administrator* can create an entity of protection-type *printer*. This rule is simply an ordered pair representing the parent and child types, respectively. The specification checks the current state of the set *Can_Creates* to ensure that it contains the pair (*administrator, printer*). The Pre- and Post-Create State boxes contain the members of the set *Entities* and their respective domains. The system initially has only two entities (*Bob and Alice*). Also shown is the relevant member of the set *Can_Creates*, and the sets cr`p and cr`c, which will determine the outcome of the create. The associated create-rule sets cr`p and cr`c include two tickets to be added to the parent's domain (*myfile/rc* and *syslog/w*) and none for the child.



Figure 3. The Create Process

SPM Encoding

The PVS specification for SPM is presented below. This version of the model contains the theory named SPM, which includes the ability to transfer a ticket and create a new entity. Slightly modified versions are presented in the next chapter to demonstrate correct behavior under the specified exceptional conditions.
The code implements two separate state-machines, implementing the rules of ticket-transfer and the rules of entity creation, respectively. State transitions within each are controlled with a sequential logic that mimics an assembly-like program running on a virtual processor, referred to in the embedded comments as processor_1 and processor_2. The program-counter is a state variable used by the transition functions to navigate the flow of control, starting from a known initialized state.

Since the PVS statements are interpreted by the prover in the order they appear, these transition functions are preceded by datatype and function declarations, and followed by the single theory through which the state machines will be evaluated together. It is at this point that the illusion of linearity is abandoned and PVS considers the correctness of the state transitions from every possible initial state that ultimately results in a termination state. It is this all-possible-worlds analysis that supports the claim that the safety of the SPM is correctly demonstrated by the specification.

SPM Specification.

The PVS specification below is interpreted with minor formatting changes only. Comments (preceded by a "%" sign) are included throughout, followed by the pertinent PVS instruction. Major sections are delineated with a horizontal row of equal signs (====), minor sections with dashes (====):

% custom datatypes used by the SPM specification. <u>°</u>_____ % RECORD-TYPE DEFINITIONS PVS allows the use of a record datatype that acts as a % record with named fields. The record structure allows the individual fields to be 00 % examined by referencing the name. This SPM specification defines several datatypes that 00 % use this structure: Type_name: TYPE = (# 00 00 fieldname_1 := datatype, fieldname_2 := datatype, 00 00 ..., 00 fieldname_n := datatype % #) % Right_class is an enumerated type which lists all % possible classes of right Right_class: TYPE = {Control, Inert} % Right_priv is an enumerated type which lists all allowable % privileges in the system Right_priv: TYPE = {read, write, append, execute, take, grant, demand} % Right_type is a record type comprised of the privilege and % the class it belongs to Right_type: TYPE = [#privilege: Right_priv, class: Right_class #1 % Enumerate possible protection-types and entity classes Entity_class: TYPE = {Subject, Object} Protection_type: TYPE = {administrator, user, printer, file} % define the Entity_type as a record containing an % identifier for comparison with other entities during the % proof, and associated protection type ID_type: TYPE = $\{0, 1, 2, 3, 4\}$ Entity_type: TYPE = [# ID: ID_type, ptype: Protection_type #]

% Ticket type is a record datatype that contains three named % parts, an entity of type Entity_type and a right of type % Right_type (each described above), and a boolean copy flag Ticket_type: TYPE = [# entity: Entity_type, right: Right_type, copyable?: bool #1 % PTicket_type is a tuple datatype that contains two parts, % one to hold a valid protection-type and one a valid right, % as described in their respective datatype definitions % above. PTicket_type: TYPE = [Protection_type, Right_type] % Rule_type is a record that contains two sets of tickets to % be used in a create rule. % The set p is for the parent and c is for the child of a % create operation Rule_type:TYPE=[# p: setof[Ticket_type], c: setof[Ticket_type] #1 % Link type identifies the edge between two entities Link_type: TYPE = [ID_type, ID_type] % Filter type associates a pair of Protection_type with % a set of PTicket_type % e.g. [user, user] -> {(file, r), (printer, w)} Filter_type: TYPE = [[Protection_type, Protection_type] -> setof[PTicket_type]] % PCt is an enumerated datatype which lists possible values % of the virtual program counters (suffix _x indicates % processor). These values represent code labels, as appear % in assembly or BASIC programs, and are used to navigate % the logic of the state-machine. PCt: TYPE = {L1_1, L2_1, L3_1, L4_1, L5_1, L6_1, L7_1, LEND_1, L1_2, L2_2, L3_2, L4_2, L5_2, LEND 2} 8-----% State_template is a record datatype that comprehensively % represents the state of the system. The definition below

```
% identifies names for each of the system attributes that
% comprise the current state, each followed by their
% respective datatype. The datatypes are either inherent to
% PVS, such as boolean (bool), or defined above.
State_template: TYPE = [#
     % virtual program counter
    PC:
                    PCt,
     % The set of all protections types, by class
              [Entity_class -> setof[Protection_type]],
    Т:
     % The set of all privilege-bearing entities
                   setof[Entity_type],
    Entities:
    % set of Tickets in the provided Entity's domain
    Domain:
                    [Entity_type -> setof[Ticket_type]],
     % The set of can-create relationships
    Can_Creates: [Protection_type ->
                        setof[Protection_type]],
    % The set of all active create rules
    Create_rules: [Entity_class, Entity_class ->
                                       Rule type],
    % The set of all active transfer-filter policies
    Filters:
                    [Link_type -> Filter_type],
    % Do test conditions allow the transfer?
    tr Authorized?: bool,
     % Do test conditions allow the create?
    cc Authorized?: bool,
     % Flag used to record breach of secure state
    State OK:
                   bool
     #]
%======
              ______
% INSTANTIATIONS
% In this section, named entities are created to represent
% specific system components for PVS to manipulate, as
% instantiations of record-type definitions.
% These record-types are instantiated as follows:
00
         Name: datatype = (#
%
                           fieldname_1 := value_1,
%
                           fieldname 2 := value 2,
```

00 •••, 00 fieldname_n := value_n 00 #) 8----------% RIGHTS % Used to represent the different privileges that can be % exercised by one entity over another r: Right_type = (# privilege := read, class := Inert #) w: Right_type = (# privilege := write, class := Inert #) %_____ % ENTITIES % Instantiate named entities for the current system % ID's should be unique to avoid erroneous comparisons % e.g., "Bob = Alice" Bob: Entity_type = (# ID := 0, ptype := administrator #) Alice: Entity_type = (# ID := 1, ptype := user #) LaserJet_1: Entity_type = (# ID := 2, ptype := printer #) myfile: Entity_type = (# ID := 3, ptype := file #) syslog: Entity_type = (# ID := 4, ptype := file #) %_____ % TICKETS

% Create a copyable version of the ticket: myfile/rc % This ticket would allow read-access to myfile to be % exercised by any entity possessing this ticket in its % associated domain, representing the ticket myfile/rc. myfile_rc: Ticket_type = (# entity := myfile, right := r, copyable? := TRUE #) % Create a non-copyable version of the same ticket: i.e., % myfile/r. myfile_r: Ticket_type = (# entity := myfile, right := r, copyable? := FALSE #) % Create a ticket representing the copyable write privilege % (w) over the entity "LaserJet_1" representing the ticket % LaserJet 1/wc. LaserJet 1 wc: Ticket type = (# entity := LaserJet_1, right := w, copyable? := TRUE #) % Create a non-copyable version of the ticket syslog/w. syslog_w: Ticket_type = (# entity := syslog, right := w, copyable? := FALSE #) %_____ % INITIALIZE state and SETUP the desired conditions: % Below, the initial system state and its immediate % successor, the setup state, are described. The latter is % used to establish the preconditions for any test to be % conducted. %_____ _____ % Init can be thought of as a function, taking an argument % (snapshot) of type State_template. It returns to the % calling statement a State_template equal to snapshot

```
Init(snapshot: State_template): State_template =
     snapshot WITH [
     % Establish there are no protection types in TS or TO
     T := snapshot`T WITH [
                (Subject) := emptyset,
(Object) := emptyset],
     % Establish that there are no Entities in the current
     % system state
     Entities
                                           := emptyset,
     % Establish that the domains of each instantiated
     % Entity is initially empty
     Domain := snapshot`Domain WITH [
                (Bob)
                                          := emptyset,
                (Alice)
                                          := emptyset,
                (Alice,
(LaserJet_1)
                                          := emptyset,
                                          := emptyset],
     % Establish that there are no can-create relations
     Can_Creates := snapshot`Can_Creates WITH [
                (administrator) := emptyset,
                                          := emptyset,
                (user)
                (printer)
                                          := emptyset,
                (file)
                                           := emptyset],
     % Establish that there are no create rules
     Create_rules := snapshot`Create_rules WITH [
                (Subject, Subject)`p := emptyset,
(Subject, Subject)`c := emptyset,
(Subject, Object)`p := emptyset,
(Subject, Object)`c := emptyset],
     % Establish that there are no filters.
     % Filter_type = [(Protection_type,Protection_type) ->
                                          setof[PTicket type]]
     00
     % Filters = [Link_type -> Filter_type] (State_template)
     Filters := snapshot`Filters WITH [
                (Bob`ID, Alice`ID)
                (administrator, user) := emptyset,
                (Alice`ID, Bob`ID)
                (user, administrator) := emptyset],
```

% after the changes indicated in the WITH[] block have been

% sequentially applied.

```
% Set flag to indicate a secure initial state
    State OK
                                        := TRUE]
%_____
% Set up test pre-conditions
% The Setup function takes an argument (snapshot) of type
% State_template and returns it with the following
% sequentially-applied changes:
Setup(snapshot: State_template): State_template =
     snapshot WITH [
    % Add protection types to TS and TO
    T := snapshot`T WITH [
         (Subject) := add(administrator,
                        add(user,
                            snapshot`T(Subject))),
         (Object) := add(printer,
                        add(file,
                            snapshot`T(Object)))],
    % Add Bob and Alice to the system
    Entities := add(Bob,add(Alice, snapshot`Entities)),
    % Add myfile_rc to Bob's Domain
    Domain := snapshot`Domain WITH [
         (Bob) := add(myfile rc, snapshot`Domain(Bob))],
    % ESTABLISH SYSTEM POLICIES
    % (Link predicate policies are established in the Link?
    % function in processor_1)
    % _____
    % Add Can-Create relations
    Can_Creates := snapshot`Can_Creates WITH [
         % cc(Subject, Object)
         (administrator) :=
           add(user,
              add (printer,
                 add(file,
                 snapshot`Can_Creates(administrator))))],
    ° _____
    % Add Create rules
    Create_rules := snapshot`Create_rules WITH [
    % cr(Subject, Subject) =
    00
        cr`p(Subject, Subject) = {syslog_w, myfile_rc}
         cr`c(Subject, Subject) = {syslog_w, myfile_r}
    (Subject, Subject) `p :=
         add(syslog_w,
```

```
add(myfile rc,
                 snapshot`Create rules(
                     Subject, Subject)`p)),
    (Subject, Subject) `c :=
        add(syslog_w,
            add(myfile_r,
                 snapshot`Create_rules(
                     Subject, Subject)`c)),
    % cr(Subject, Object) =
        cr`p(Subject, Object) = {syslog_w, myfile_rc}
        cr`c(Subject, Object) = {}
    (Subject, Object) `p :=
        add(syslog_w,
            add(myfile_rc,
                 snapshot`Create_rules(
                     Subject, Object)`p))],
    ° _____
    % Add Filter
    % f(administrator, user) = {(file, r), (printer, w)}
    % to the link from Bob to Alice
    Filters := snapshot`Filters WITH [
        (Bob`ID, Alice`ID) (Bob`ptype, Alice`ptype) :=
           add((file,r),
             add((printer,w),
                snapshot`Filters(Bob`ID, Alice`ID)
                      (administrator, user)))],
    % Set the expected outcomes for an attempted transfer
    tr Authorized? := TRUE,
    % Set the expected outcomes for an attempted create
    cc Authorized? := TRUE]
%_____
%_____
% Fork into separate state machines
    At this point in our sequential analysis, the logic of
8
% the specification forks into two distinct and autonomous
% state machines. Their respective virtual program counters
% are differentiated by suffix (_1 and _2), and the virtual
% processors are correspondingly tagged processor_1 and
% processor_2 for clarity.
    The first, processor_1, verifies the correct behavior
00
% of an attempt to execute a ticket transfer.
```

```
% EXECUTE TRANSFERS (processor _1):
% Verify the correct behavior of an attempt to transfer a
% ticket.
<u>%</u>_____
% Test Link
% Link predicate system policies are entered in the inner
% nested-CASES statements to determine a link from source to
% target. The predicates themselves are resolved to a
% boolean value which is returned as the response from Link?
% e.g., the predicate: ticket Î dom(entity) is implemented
% with:
00
         member(ticket, snapshot`Domain(entity))
00
% In this case, the following link predicates are
% implemented:
%
00
    myfile/rc Î dom(Bob), for the edge: Bob to Alice,
00
                          for the edge: Bob to LaserJet 1,
    TRUE,
    TRUE,
00
                          for the edge: Alice to Bob.
Link?(snapshot: State_template,
     source:
              ID_type,
     target: ID_type): bool =
     % CASES used to facilitate additions
    CASES source OF
         % source = Bob's ID
         0: CASES target OF
              % target = Alice's ID
              1: member(myfile_rc, snapshot`Domain(Bob)),
              % target = LaserJet_1's ID
              2:
                   TRUE
              ELSE FALSE
            ENDCASES,
         % source = Alice's ID
         1: CASES target OF
              % target = Bob's ID
              0: TRUE
              ELSE FALSE
            ENDCASES
         ELSE FALSE
    ENDCASES
```

```
°_____
% Test Filter
% Determine whether a filter function exists in
% snapshot`Filters, associated with the link predicate
% for (source and target), that allows tickets that match
% the tuple (protection-type, right) in the given ticket, to
% be transferred from the source to the target, as
% determined by their respective ptypes,
% implementing the filter function:
00
% (ticket`entity`ptype, ticket`right) 
% f(source`ptype, target`ptype)
0/2
% In this test case, (1): ticket
                                       = myfile_rc
                       myfile_rc`entity = myfile
00
%
                       myfile`ptype = file
%
                       myfile rc`right = r
00
% and,
                  (2): source
                                      = Bob
                                     = administrator
= Alice
                       Bob`ptype
%
00
                       target
%
                       Alice`ptype = user
%
% It follows that,
00
    (ticket`entity`ptype, ticket`right)=(file, r) (1)
% and,
00
    (source`ptype, target`ptype)=(administrator, user) (2)
00
% and since the filter
00
    (administrator, user) = { (file, r), (printer, w) }
%
% we know that
00
    (file,r) in (administrator, user) = TRUE
%
% and that the filter is associated with the link
% (Bob, Alice) in the State_template set, then
%
%
         Filters(0, 1)(administrator, user) =
00
         {(file, r), (printer, w)}
Filter?(snapshot: State_template,
       source: Entity_type,
       target: Entity_type,
       ticket: Ticket_type): bool =
         member((ticket`entity`ptype, ticket`right),
              snapshot`Filters(source`ID, target`ID)
                       (source`ptype, target`ptype))
%_____
% Establish event of interest indicator
```

% For processor_1, the event that will imply a successful % transfer is the presence of myfile_r in Alice's domain, as % indicated by the boolean value of Event_1? Event_1?(snapshot: State_template): boolean = member(myfile_r, snapshot`Domain(Alice)) ٥٥_____ % Execute transfer % The Exec 1 function is where the actual transfer takes % place. It takes an argument (snapshot) of type % State_template and returns it after applying the changes % in the WITH block. In this case the ticket myfile_r is % added to the Alice's domain. Exec_1(snapshot: State_template): State_template = snapshot WITH [Domain := snapshot`Domain WITH [(Alice) := add(myfile r, snapshot`Domain(Alice))]] %_____ % Test system state The Test_1 function takes a State_template and returns 00 % a State_template with an updated State_OK. If the test condition (Event_1?) returns TRUE, 00 % indicating that it did happen, then tr_Authorized? % determines the value of State OK (if it was not % authorized, then State_OK is FALSE). If the test condition returns FALSE, indicating that it 00 % did not happen, then we don't care whether it was % authorized, and State_OK remains TRUE. Note that this test does not prove that if the 00 % operation is authorized that it will happen, only that if % it did happen, it was authorized. % i.e.: % Event 1?(snapshot) snapshot`tr Authorized? State OK 1 1 1 00 00 1 0 0 0 1 1 00 0 00 0 1 Test_1(snapshot: State_template): State_template = snapshot WITH [State_OK := IF Event_1?(snapshot) THEN snapshot`tr_Authorized? ELSE TRUE ENDIF] 8-----

% TRANSITION FUNCTIONS for program counter (PC) within the

% context of processor 1. trans(snapshot: State_template): State_template = CASES snapshot `PC OF % Each case applies WITH conditions before passing % snapshot to the specified operation, then % returns snapshot. % set up initial state and increment PC L1_1: Init(snapshot) WITH [PC := L2_1], % set up test conditions and increment PC L2_1: Setup(snapshot) WITH [PC := L3_1], % verify that source entity has copyable ticket % and adjust PC L3_1: snapshot WITH [PC := IF (member(myfile_rc, snapshot`Domain(Bob))) AND myfile_rc`copyable? THEN L4 1 ELSE L7_1 ENDIF], % verify that link exists between source and % target/adjust PC WITH [PC := L4_1: snapshot IF Link?(snapshot, Bob`ID, Alice`ID) THEN L5 1 ELSE L7_1 ENDIF], % verify that a filter function allows this % transfer/adjust PC L5_1: snapshot WITH [PC := IF Filter?(snapshot, Bob, Alice, myfile_rc) THEN L6_1 ELSE L7_1 ENDIF], % Execute the transfer and increment PC L6_1: Exec_1(snapshot) WITH [PC := L7_1], % Test State OK and move PC to end L7_1: Test_1(snapshot) WITH [PC := LEND_1], LEND_1: snapshot ELSE snapshot ENDCASES

% Prove safety Show that State_OK will still be TRUE after an attempt 00 % to transfer a right from any given initial state, using % any given natural counter T. % 00 The tr_find_zero() function will recurse through the % ELSE statement, decrementing T until it is finally called % with T=0, at which point it returns the State_template % initial with the virtual program counter (PC) set to L1_1, % to be subsequently passed to the trans() function. 00 The state returned from trans() will have accrued % changes from the trans() state machine, including an % updated PC. The returned state is then repeatedly passed back to 00 % trans(), and returned with changes and updated PC as the % logic backs out of the recursion. 0 The effect is that, given a nonnegative number T and a 00 % State_template initial, the state-transition functions % within trans() will be applied against initial, starting % with the first (L1_1) and proceeding according to the % manipulation of the program counter PC. tr_find_zero(T: nat, initial: State_template): RECURSIVE State_template = IF T = 0 THEN initial WITH [PC := L1 1] ELSE trans(tr find zero(T-1, initial)) ENDIF MEASURE T ٥٤_____ % Test all possible initial states % Assign a boolean result to the following nested assertion % that only authorized transfers can occur: Given any possible initial state, as described by the 8 % State template record type: Given any possible nonnegative number T, such that 8 % the function tr_find_zero(T, initial) returns a State_template with the virtual program counter % % at LEND_1 (indicating termination): % the returned State_template will also % indicate that State OK = TRUE. transfer_correct: bool = FORALL (initial: State_template): FORALL (T: nat | tr_find_zero(T, initial)`PC = LEND_1): tr_find_zero(T, initial)`State_OK = TRUE %_____ % CREATES (processor _2): Verify correct behavior of

%____

```
% attempts to create a new entity.
<u>%_____</u>
% Can-create test
% Test for appropriate cancreate relation; in this case:
8
00
         cc(administrator, printer)
00
% The test determines whether child is in the set
% CanCreates(parent)
    where child = printer
00
    and parent = administrator
00
CC?(snapshot: State_template,
             parent: Protection_type,
             child: Protection_type): boolean =
                   (member(child,
                    snapshot`Can_Creates(parent)))
٥٥------
% Establish event of interest indicator
% For processor_2, the event that will imply a successful
% create is the presence of LaserJet_1 in the system, and
% the appropriate updates to both the parent and child
% domains, as indicated by the boolean Event_2?
Event_2?(snapshot: State_template): boolean =
     (member(LaserJet_1, snapshot`Entities))
95_____
% Execute create
% The Exec_2 function is where the actual create takes
% place. It takes an argument (snapshot) of type
% State_template and returns it after adding LaserJet_1 to
% the set Entities.
0
00
    The two entities' Domains are updated at create-time to
% reflect the create rule
0
00
          cr(Subject, Object)
%
% which is comprised of these system policies, established
% in the Setup function:
         cr`p(Subject, Object) = {syslog_w, myfile_rc}
00
         cr`c(Subject, Object) = {}
00
Exec_2(snapshot: State_template,
      parent: Entity_type,
      child: Entity_type): State_template = snapshot WITH[
   % Create entity
   Entities := add(child, snapshot`Entities),
```

```
% Invoke associated create-rules
    Domain
            :=
        IF member(child`ptype, snapshot`T(Subject)) THEN
          snapshot`Domain WITH [
               (parent) :=
                   union(snapshot`Create_rules(
                          Subject, Subject) `p,
                             snapshot`Domain(parent)),
               (child)
                        :=
                   union(snapshot`Create_rules(
                          Subject, Subject)`c,
                             snapshot`Domain(child))]
        ELSIF member(child`ptype, snapshot`T(Object)) THEN
         snapshot`Domain WITH [
                (parent) :=
                   union(snapshot`Create rules(
                          Subject, Object) `p,
                             snapshot`Domain(parent)),
                (child)
                        :=
                   union(snapshot`Create_rules(
                          Subject, Object)`c,
                             snapshot`Domain(child))]
        ELSE snapshot`Domain
       ENDIF]
                   -----
§_____
% Test system state
    The Test_2 function takes a State_template and returns
00
% a State_template with an updated State_OK.
     If the test condition (Event_2?) returns TRUE,
00
% indicating that it did happen, then cc_Authorized?
% determines the value of State_OK (if it was not
% authorized, then State_OK is FALSE).
     If the test condition returns FALSE, indicating that it
9
% did not happen, then we don't care whether it was
% authorized, and State_OK remains TRUE.
    Note that this test does not prove that if the
00
% operation is authorized that it will happen, only that if
% it did happen, it was authorized.
% i.e.:
% Event_1?(snapshot)
                      snapshot`tr_Authorized? State_OK
00
                   1
    1
                                1
                                0
00
    1
                   0
00
    0
                   1
                                1
00
    0
                   0
                                 1
Test_2(snapshot: State_template): State_template =
     snapshot WITH [
```

State OK := IF Event 2?(snapshot) THEN snapshot`cc_Authorized? ELSE TRUE ENDIF] g_____ % TRANSITION FUNCTIONS for program counter (PC) within the % context of processor_2. create(snapshot: State_template): State_template = CASES snapshot PC OF % Each case applies WITH conditions before passing % snapshot to the specified operation, then % returns snapshot. % initialize system state L1_2: Init(snapshot) WITH [PC := L2_2], % establish setup conditions $L2_2$: Setup(snapshot) WITH [PC := $L3_2$], % verify that a cancreate relation will allow the % create L3_2: snapshot WITH [PC := IF CC?(snapshot, Bob`ptype, LaserJet_1`ptype) THEN L4_2 ELSE L5_2 ENDIF], % execute the create L4_2: Exec_2(snapshot, Bob, LaserJet_1) WITH [PC := L5 2], % test State_OK and move PC to end L5 2: Test 2(snapshot) WITH [PC := LEND 2], LEND_2: snapshot ELSE snapshot ENDCASES 95_____ % Prove safety Show that State_OK will always be TRUE after a create 9 % attempt. The function cc_find_zero will decrement T down to 0 00 % recursively, and pass the State_template initial to the % create state-machine with program counter (PC) set to % L1_2, and then step through the state-machine in the same % way that tr_find_zero did above.

```
cc_find_zero(T: nat, initial: State_template): RECURSIVE
State_template =
    IF T = 0 THEN initial WITH [PC := L1 2]
           ELSE create(cc_find_zero(T-1, initial))
    ENDIF MEASURE T
<u>%</u>_____
% Test all possible initial states
% Assign a boolean result to the following nested assertion
% that only authorized creates can occur:
    Given any possible initial state, as described by the
8
00
    State_template record type:
        Given any possible nonnegative number T, such that
00
        the function cc_find_zero(T, initial) returns a
%
%
        State_template with the virtual program counter
00
        at LEND_2 (indicating termination):
00
            the returned State_template will also
%
            indicate that State OK = TRUE.
cancreate correct: bool =
 FORALL (initial: State_template):
   FORALL (T: nat | cc_find_zero(T, initial) PC = LEND_2):
     cc_find_zero(T, initial)`State_OK = TRUE
%______
% SPM Safety Theorem
% System correct is the single theorem to be proved by PVS.
% It asserts that the boolean statements transfer correct
% and cancreate_correct resolve to TRUE
System_correct: Theorem transfer_correct
             AND
             cancreate correct
END SPM
∞_____
```

Specification Description.

The System_correct theorem asserts that transfer_correct and cancreate_correct

are both TRUE expressions.

The statement *transfer_correct* asserts that for any possible initial state and any

possible starting point submitted to the recursive function *tr_find_zero*, which

successfully terminates, the boolean state variable *State_OK* will be TRUE. *State_OK* is a flag set when the model operates correctly.

The tr_find_zero function takes the natural number T and the current system state as input. It recursively decrements T, until T = 0, at which point it introduces the current state into the sequential state-transition function *trans*. The returned state is repeatedly passed back to the *trans* function, with accrued changes, as tr_find_zero backs out of the recursion. *Transfer_correct* initiates this process for all possible values of T, and all possible initial states.

The *trans* function behaves as a virtual processor, applying the state transition function indicated by the program counter (*PC*) and updating it as appropriate. The internal state transition operations represent the PVS-language interpretation of assembly-like pseudocode derived from a sequential algorithm, using the process described in Chapter II to implement the correct behavior of the ticket transfer component of SPM.

A positive outcome of the proof indicates the applied rules behave as expected for all possible valid inputs, and the boolean indicator *State_OK* was not changed.

Just like *tranfer_correct*, the statement *cancreate_correct* asserts that for any possible initial state and any possible starting point submitted to the recursive function *cc_find_zero*, which successfully terminates, the boolean state variable *State_OK* will be TRUE.

The *cc_find_zero* function takes the natural number *T* and the current system state as input. It recursively decrements *T*, until T = 0, at which point it introduces the current state into the sequential state-transition function *create*.

45

The *create* function behaves as a second virtual processor, applying the state transition function indicated by the program counter (*PC*), and updating it accordingly.

A positive outcome of the proof indicates the applied rules behave as expected for all possible valid inputs, and the boolean indicator State_OK was not changed.

SPM Proof

The *System_correct* theorem at the end of the SPM specification is the single statement that resolves to TRUE if and only if the specification correctly implements SPM. The theorem consists of the boolean statement

transfer_correct AND cancreate_correct

which, when the two state machines correctly implement their respective transfer and create processes, resolves to the formula

TRUE AND TRUE

Before the specification is tested by the prover, the PVS parser checks datatypes and logic flow structures for consistency and completeness. In some cases, the correctness of the proof depends upon the properties of datatypes, so these must also be proved for the results to be complete. These alerts are presented by PVS as Type Correctness Conditions.

Type Correctness Conditions.

Type Correctness Conditions (TCC), such as those identified in Figure 4 as tr_find_zero_TCC1 and tr_find_zero_TCC2, describe assumed conditions that must hold to ensure well-formed values for the variable indicated in the TCC description.

In the SPM specification, two such conditions were discovered: the nonnegative property of the *nat* datatype, and the inevitability of reaching the termination condition in

the recursive function tr_find_zero. The TCCs proofs were accomplished separately from the System_correct proof, and are described below.

TCC1.

The condition entitled tr_find_zero_TCC1 is a response to this line from the recursive function tr_find_zero, which makes a references to *T-1*:

ELSE trans(tr_find_zero(T-1, initial))

Since the function tr_find_zero is expecting to be passed a natural (nonnegative)

number, it must be shown that *T*-1 will, in fact, be natural. More formally:

FORALL (**T**: **nat**): **NOT T** = **0 IMPLIES T** - **1** >= **0**

This expression was proved as a stand-alone theory using the automated prover.

The proof was accomplished by invoking the prover to execute the aggregate command

SUBTYPE-TCC, which applied repeated skolemization, instantiation, and if-lifting,

resulting in the following proof:

tr_find_zero_TCC1 :
 |-----{1} FORALL (T: nat): NOT T = 0 IMPLIES T - 1 >= 0
Rerunning step: (SUBTYPE-TCC)
Trying repeated skolemization, instantiation, and if-lifting,
Q.E.D.

TCC2.

The condition entitled tr_find_zero_TCC2 is a termination warning in reference to

the inner part of the same statement

tr_find_zero(T - 1, initial)

Since this function is recursively decrementing to zero, it must be shown that T-1

is, in fact, less than T, and progresses toward zero. More formally

FORALL (T: nat): NOT T = 0 IMPLIES T - 1 < T

This expression was also proved as an autonomous theory using PVS. It was accomplished by invoking the automated prover to execute the aggregate command TERMINATION-TCC, which applied repeated skolemization, instantiation, and iflifting, resulting in the following proof:

tr_find_zero_TCC2 :
 |-----{1} FORALL (T: nat): NOT T = 0 IMPLIES T - 1 < T
Rerunning step: (TERMINATION-TCC)
Trying repeated skolemization, instantiation, and if-lifting,
Q.E.D.</pre>

The System_correct Theorem.

The System_correct theorem asserts the correct behavior of the model as an

implementation of SPM with the statement

transfer_correct AND cancreate_correct

The PVS split command was used to consider the two statements separately.

Each individual statement then represents a subgoal of the original theorem. The prover presented each subgoal as a sequent, and satisfied (aka, dismissed) them according to the sequence of commands shown in Figure 4.

For example, in node 1 of Figure 4, the command expand "transfer_correct"

replaces the statement *transfer_correct* with its definition from within the specification,

resulting in the sequent

|-----{1} FORALL (initial: State_template):
FORALL (T: nat | tr_find_zero(T, initial)`PC = LEND_1):
tr_find_zero(T, initial)`State_OK

The **skosimp** command, applied to the above sequent, inserts the skolem constant *initial*?1 to represent an arbitrary variable with which to test the outer FORALL condition, resulting in the sequent

The command **induct** "T" runs a natural-number induction against the variable T,

resulting in three subgoals. The first two subgoals are dismissed with the grind

command, an aggregate of several prover commands,

```
Inducting on T on formula 1,
this yields 3 subgoals:
System_correct.1.1 :
 |-----
{1} tr_find_zero(T!1, initial!1) PC = LEND_1
{2} tr_find_zero(T!1, initial!1)`State_OK
Rerunning step: (GRIND)
Trying repeated skolemization, instantiation, and if-lifting,
This completes the proof of System_correct.1.1.
System_correct.1.2 :
  |-----
{1} tr_find_zero(0, initial!1) PC = LEND_1 IMPLIES
      tr_find_zero(0, initial!1)`State_OK
Rerunning step: (GRIND)
tr_find_zero rewrites tr_find_zero(0, initial!1)
 to initial!1 WITH [PC := L1_1]
Trying repeated skolemization, instantiation, and if-lifting,
This completes the proof of System_correct.1.2.
```

and the third subgoal of node 1 generates more subgoals by performing an induction on

the variable j in this sequent

The proof of the System_correct theorem progressed in this way until all subgoals

were dismissed as shown in Figure 4, using the combination of the PVS prover

commands described in Chapter II.



Figure 4. SPM Proof Tree

The proof-summary in Figure 5 was generated by PVS for the SPM theory. It

shows that the theory was proved, and that the necessary Type Correctness Conditions

(TCCs) discovered by PVS during the proof were each, themselves proved.

```
Proof summary for theory SPM

tr_find_zero_TCC1.....proved - complete [SHOSTAK](0.32 s)

tr_find_zero_TCC2....proved - complete [SHOSTAK](0.03 s)

System_correct...proved - complete [SHOSTAK](36.75 s)

Theory totals: 3 formulas, 3 attempted, 3 succeeded (37.10 s)
```

Figure 5. PVS proof summary for SPM

IV. Schematic Protection Model Validation Scenarios

Introduction

The Schematic Protection Model describes the conditions under which rights can be transferred from one entity to another, and new entities can be created in the system. These conditions test the model's ability to prevent transition to an unsecure state. Each of these conditions is tested in the following scenarios, followed by several tests of anomalous conditions.

Test Scenario 1 - No Ticket

Below is a test scenario modification to the Setup function. In this test, the entity *Bob* initiates a transfer of the ticket *myfile_r*, but does not possess the ticket in its domain, which is a necessary condition to allow the transfer.

Encoding.

In the original SPM specification, the ticket *myfile_rc* is added to *Bob*'s domain in the Setup function. To test this condition of the model, the statements below were commented out effectively removing them from *Bob*'s domain:

% Add myfile_rc to Bob's Domain %Domain := snapshot`Domain WITH [% (Bob) := add(myfile_rc, snapshot`Domain(Bob))],

When the transition function L3_1 is invoked by the *trans* function, the current state of the model, encapsulated in *snapshot*, does not include *myfile_rc* in *Bob*'s domain. Since this is a necessary condition to allow the transfer, the program counter *PC* is set to proceed to the transition function $L7_1$ for the next iteration, rather than step through the remaining sequence of tests.

% verify that source entity has copyable ticket % and adjust PC L3_1: snapshot WITH [PC := IF (member(myfile_rc, snapshot`Domain(Bob))) AND myfile_rc`copyable? THEN L4_1 ELSE L7_1 ENDIF],

Transition function $L7_1$ sets *PC* to the terminal value LEND_1, and passes snapshot to the *Test_1* function for a determination of whether the model has correctly implemented this condition of SPM.

> % Test State_OK and move PC to end L7_1: Test_1(snapshot) WITH [PC := LEND_1],

The *Test_1* function passes the state *snapshot* to *Event_1*? to determine whether

the event of interest in this case has occurred. *Event_1*? returns the boolean value of the

statement

which resolves to FALSE because *myfile_r* was never added to *Alice*'s domain. Since the

IF condition in *Test_1* is FALSE, the logic diverts to the ELSE statement, setting the

value of *State_OK* to TRUE, indicating that the unauthorized transfer did not take place.

Results.

The statement *transfer_correct* is an assertion that *State_OK* will be TRUE.

When the resultant state is eventually returned from the recursive tr_find_zero function with the program counter *PC* set to LEND_1, the value of *State_OK* is TRUE, and the boolean value of transfer correct becomes TRUE.

```
transfer_correct: bool =
  FORALL (initial: State_template):
    FORALL (T: nat | tr_find_zero(T, initial)`PC = LEND_1):
        tr_find_zero(T, initial)`State_OK = TRUE
```

The proof of the System_correct theorem with this test modification progressed as

shown in Figure 6 until all subgoals were dismissed, using a combination of the PVS

prover commands as described in Chapter II.



Figure 6. SPM_noticket Proof Tree

The PVS-generated proof summary in Figure 7 shows that this modification of the theory was proved, and that necessary Type Correctness Conditions implied by the theory were also proved:

```
Proof summary for theory SPM_noticket

tr_find_zero_TCC1.....proved - complete [SHOSTAK](0.68 s)

tr_find_zero_TCC2....proved - complete [SHOSTAK](0.27 s)

System_correct....proved - complete [SHOSTAK](40.54 s)

Theory totals: 3 formulas, 3 attempted, 3 succeeded (41.49 s)
```

Figure 7. PVS proof summary for SPM_noticket

Test Scenario 2 - Ticket Not Copyable

Below is a test scenario modification for the SPM in which the ticket to be transferred exists in the initiating entity's domain, but the ticket is not copyable, which is a necessary condition to allow the transfer.

Encoding.

The only modification required for this test was to instantiate the ticket with

copyable? = FALSE:

```
myfile_rc: Ticket_type = (#
    entity := myfile,
    right := r,
    copyable? := FALSE
    #)
```

In the $L3_1$ transition function, the test of the originator's domain is conducted as normal, failing the second conjunctive test in the IF condition: myfile_rc`copyable?. The logic diverts to the ELSE statement, and sets the program counter (*PC*) to $L7_1$, skipping the subsequent tests and the transfer operation itself.

In the next pass, the statement at $L7_1$ is invoked, setting the *PC* to LEND_1 and passing the state information contained in *snapshot* to *Test_1* for a determination of whether the model has correctly implemented this condition of SPM.

% Test State_OK and move PC to end L7_1: Test_1(snapshot) WITH [PC := LEND_1],

The *Test_1* function passes the state *snapshot* to *Event_1*? to determine whether

the event of interest in this case has occurred. *Event_1*? returns the boolean value of the

statement

```
member(myfile_r, snapshot`Domain(Alice))
```

which resolves to FALSE because *myfile_r* was never added to *Alice*'s domain. Since the

IF condition is FALSE, the logic diverts to the ELSE statement, setting the value of

State_OK to TRUE, indicating that the unauthorized transfer did not take place.

Results.

The proof of the *System_correct* theorem with this test modification progressed as shown in Figure 8 until all subgoals were dismissed, using a combination of the PVS prover commands as described in Chapter II.



Figure 8. SPM_nocopy Proof Tree

The PVS-generated proof summary for this modification in Figure 9 shows that

the theory was proved, and that necessary conditions implied by the theory were also

proved. Since the unauthorized transfer did not happen, the safety of the system holds.

```
Proof summary for theory SPM_nocopy

tr_find_zero_TCC1.....proved - complete [SHOSTAK](0.68 s)

tr_find_zero_TCC2....proved - complete [SHOSTAK](0.27 s)

System_correct....proved - complete [SHOSTAK](28.90 s)

Theory totals: 3 formulas, 3 attempted, 3 succeeded (29.85 s)
```

Figure 9. PVS proof summary for SPM_nocopy

Test Scenario 3 - No Link

Below is a test scenario modification for the SPM in which no link exists between the entity (*Bob*) initiating a transfer and the intended recipient (*Alice*); a necessary condition to allow the transfer.

Encoding.

In the original SPM specification, the link from Bob to Alice is determined by the

link predicate *myfile_rc* \in *dom*(*Bob*), and evaluated in the Link? function:

To test this condition of the model, the inner case statement was changed so that

the test for a link from *Bob* to *Alice* would fail:

```
% target = Alice's ID
1: FALSE,
```

When the transition function $L4_l$ is invoked by the trans function, the returned

value of the call to Link? is FALSE:

L4_1: snapshot	WITH [PC :=	
IF Link?(snapsho	ot, Bob, Alice)	THEN L5_1
		ELSE L7_1
ENDIF],		

Since this is a necessary condition to allow the transfer, the program counter PC is

set to the transition function $L7_l$ for the next iteration, rather than step through the

remaining sequence of tests. The transition function $L7_1$ sets *PC* to the terminal value LEND_1, and passes snapshot to the *Test_1* function for a determination of whether the model has correctly implemented this condition of SPM.

% Test State_OK and move PC to end L7_1: Test_1(snapshot) WITH [PC := LEND_1],

The *Test_1* function passes the state *snapshot* to *Event_1*? to determine whether

the event of interest in this case has occurred. *Event_1*? returns the boolean value of the

statement

member(myfile_r, snapshot`Domain(Alice))

which resolves to FALSE because *myfile_r* was never added to *Alice*'s domain. Since the

IF condition in *Test_1* is FALSE, the logic diverts to the ELSE statement, setting the

value of *State_OK* to TRUE, indicating that the unauthorized transfer did not take place.

Results.

The statement *transfer_correct* is an assertion that *State_OK* is TRUE. When the resultant state is eventually returned from the recursive *tr_find_zero* function with the program counter *PC* set to LEND_1, the value of *State_OK* is discovered to be TRUE, and the boolean value of *transfer_correct* becomes TRUE.

```
transfer_correct: bool =
  FORALL (initial: State_template):
    FORALL (T: nat | tr_find_zero(T, initial)`PC = LEND_1):
        tr_find_zero(T, initial)`State_OK = TRUE
```

The proof of the *System_correct* theorem with this test modification progressed as shown in Figure 10 until all subgoals were dismissed, using the indicated PVS prover commands.



Figure 10. SPM_nolink Proof Tree

The PVS-generated proof summary in Figure 11 shows that this modification of

the System_correct theory was proved, and that necessary conditions implied by the

theory were also proved:

```
Proof summary for theory SPM_nolink

tr_find_zero_TCC1.....proved - complete [SHOSTAK](0.68 s)

tr_find_zero_TCC2....proved - complete [SHOSTAK](0.27 s)

System_correct....proved - complete [SHOSTAK](27.42 s)

Theory totals: 3 formulas, 3 attempted, 3 succeeded (28.37 s)
```

Figure 11. PVS proof summary for SPM_nolink

Test Scenario 4 - No Filter

Below is a test scenario modification for the SPM in which the filter on the link

from *Bob* to *Alice* does not allow the transfer of ticket *myfile_r*.

To allow the transfer, it is necessary that this filter function

(file, r) \in f(administrator, user)

be associated with the link from Bob to Alice, where

- 1) *Bob*'s protection type = administrator
- 2) *Alice*'s protection type = user
- 3) *myfile*'s protection type = file
- 4) *myfile_rc*'s right = r

Encoding.

In the original SPM specification, the filter on the link from Bob to Alice is

established in the Setup function

```
Filters := snapshot`Filters WITH [
   (Bob`ID, Alice`ID) (Bob`ptype, Alice`ptype) :=
    add((file,r),
        add((printer,w),
            snapshot`Filters(Bob`ID, Alice`ID)
                (administrator, user)))],
```

and tested in the Filter? function

To test this condition of the model, the statement in the *Setup* function that

created the filter was commented out.

```
% Filters := snapshot`Filters WITH [
% (Bob`ID, Alice`ID)(Bob`ptype, Alice`ptype) :=
% add((file,r),
% add((printer,w),
% snapshot`Filters(Bob`ID, Alice`ID)
% (administrator, user)))],
```

When the transition function $L5_l$ is invoked by the *trans* function, the returned

value of the call to Filter? is FALSE. Since this is a necessary condition to allow the

transfer, the program counter *PC* is set to the transition function $L7_1$ for the next

iteration, rather than proceed to $L6_1$.

```
L5_1: snapshot WITH [PC :=
IF Filter?(snapshot,
Bob,
Alice,
myfile_rc) THEN L6_1
ELSE L7_1
ENDIF],
```

The transition function $L7_1$ sets *PC* to the terminal value LEND_1, and passes snapshot to the *Test_1* function for a determination of whether the model has correctly implemented this condition of SPM.

> % Test State_OK and move PC to end L7_1: Test_1(snapshot) WITH [PC := LEND_1],

The Test_1 function passes the state *snapshot* to Event_1? to determine whether the event of interest in this case has occurred. Event_1? returns the boolean value of the statement

member(myfile_r, snapshot`Domain(Alice))

which resolves to FALSE because *myfile_r* was never added to *Alice*'s domain. Since the

IF condition in Test_1 is FALSE, the logic diverts to the ELSE statement, setting the

value of *State_OK* to TRUE, indicating that the unauthorized transfer did not take place.

Results.

The statement *transfer_correct* is an assertion that *State_OK* will hold to be

TRUE. When the resultant state is eventually returned from the recursive *tr_find_zero*

function with the program counter *PC* set to LEND_1, the value of *State_OK* is

discovered to be TRUE, and the boolean value of *transfer_correct* becomes TRUE.

```
transfer_correct: bool =
  FORALL (initial: State_template):
    FORALL (T: nat | tr_find_zero(T, initial)`PC = LEND_1):
        tr_find_zero(T, initial)`State_OK = TRUE
```

The proof of the *System_correct* theorem with this test modification progressed as shown in Figure 12 until all subgoals were dismissed, using a combination of the PVS

prover commands as described in Chapter II.


Figure 12. SPM_nofilter Proof Tree

The PVS-generated proof summary in Figure 13 shows that this modification of

the System_correct theory was proved, and that necessary conditions implied by the

theory were also proved:

```
Proof summary for theory SPM_nofilter

tr_find_zero_TCC1.....proved - complete [SHOSTAK](0.69 s)

tr_find_zero_TCC2.....proved - complete [SHOSTAK](0.27 s)

System_correct....proved - complete [SHOSTAK](40.14 s)

Theory totals: 3 formulas, 3 attempted, 3 succeeded (41.10 s)
```

Figure 13. PVS proof summary for SPM_nofilter

Test Scenario 5 - No Can-Create Relation

Below is a test scenario modification for the SPM in which there is no system policy established as a can-create relation between *Bob's* protection-type (*administrator*) and that of *LaserJet_1* (*printer*), which is a necessary condition to allow the create.

Encoding.

In the original SPM model, the can-create relation is established in the *Setup* function by adding the target class to the set associated with the originator's class. For this modification, that operation was commented out.

```
% Can_Creates := snapshot`Can_Creates WITH [
% (administrator):=
% add(user,
% add(printer,
% add(file,
% snapshot`Can_Creates(administrator))))],
```

The test for a valid can-create relation is done by the *CC*? function. This function is passed the parent's and the proposed child's protection types, and looks for the child's type to be associated with the parent's in the set *Can_Creates*, in the context of the current state of the model encapsulated in *snapshot*.

```
CC?(snapshot: State_template,
    parent: Protection_type,
    child: Protection_type): boolean =
    (member(child,
        snapshot`Can_Creates(parent)))
```

When the transition function $L3_2$ is invoked by the create function, the returned value of the call to *CC*? is FALSE, because the setup operation to establish the can-create relation was bypassed. Since this is a necessary condition to allow the create, the program counter *PC* is set to proceed to the transition function $L5_2$ for the next iteration, rather than proceed to $L4_2$, where the create would have been executed.

The transition function $L5_2$ sets *PC* to the terminal value LEND_2, and passes snapshot to the *Test_2* function for a determination of whether the model has correctly implemented this condition of SPM.

L5_2: Test_2(snapshot) WITH [PC := LEND_2],

The *Test_2* function passes the state *snapshot* to *Event_2*? to determine whether

the event of interest in this case has occurred.

Event_2? returns the boolean value of the statement

(member(LaserJet_1, snapshot`Entities))

as FALSE because *LaserJet_1* was never added to *Entities*. Since the IF condition in

Test_2 is FALSE, the logic diverts to the ELSE statement, setting the value of *State_OK*

to TRUE, indicating that the unauthorized transfer did not take place.

Results.

The statement *cancreate_correct* asserts *State_OK* is TRUE. When the resultant state is eventually returned from the recursive cc_find_zero function with the program counter *PC* set to LEND_1, the value of *State_OK* is discovered to be TRUE, and the boolean value of cancreate_correct becomes TRUE.

```
cancreate_correct: bool =
  FORALL (initial: State_template):
    FORALL (T: nat | cc_find_zero(T, initial)`PC = LEND_2):
        cc_find_zero(T, initial)`State_OK = TRUE
```

The proof of the *System_correct* theorem with this test modification progressed as shown in Figure 14 until all subgoals were dismissed, using a combination of the PVS prover commands as described in Chapter II.



Figure 14. SPM_nocreate Proof Tree

The PVS-generated proof summary in Figure 15 shows that this modification of the System_correct theory was proved, and that necessary conditions implied by the

theory were also proved:

```
Proof summary for theory SPM_nocreate

tr_find_zero_TCC1.....proved - complete [SHOSTAK](0.69 s)

tr_find_zero_TCC2....proved - complete [SHOSTAK](0.28 s)

System_correct....proved - complete [SHOSTAK](39.11 s)

Theory totals: 3 formulas, 3 attempted, 3 succeeded (40.08 s)
```

Figure 15. PVS proof summary for SPM_nocreate

Test Scenario 6 - Unauthorized Transfer

Below is a test scenario modification for the SPM in which all of the conditions to enable a ticket transfer are valid, but the *tr_Authorized?* flag has inadvertently been set to FALSE. The expected result is PVS will be unable to prove the theorem, because the theorem relies on the flag to reflect whether the event in *Event_1?* should have happened under the established conditions.

Encoding.

The only modification necessary for this test was to set the tr_Authorized? flag to

FALSE in the Setup function, as shown here:

% Set the expected outcome for an attempted transfer tr_Authorized? := FALSE,

When the proof reaches the *Test_l* function, the function passes the state *snapshot*

to *Event_1*? to determine whether the event of interest in this case has occurred.

Event_1? returns the boolean value of the statement

```
member(myfile_r, snapshot`Domain(Alice))
```

which resolves to TRUE because myfile_r was added to Alice's domain under these valid

conditions. Since the IF condition is TRUE, the logic proceeds to the THEN statement,

setting the value of *State_OK* to the current value of *tr_Authorized*?, which in this case is FALSE.

Results.

The proof of the *System_correct* theorem with this test modification progressed as shown in Figure 16 until the sequent in Table 1 was encountered, and no further progress was possible. In this test, this was the expected result, which indicates that the model is working as desired. Otherwise, a different proof strategy could be entered interactively at this point, or this sequent could be used to isolate the flaw in the original design.

		100	iui	· · · · ·		
[-1]	j!1	>=	= ()		
{-2}	j!1	_	5	=	0	
		-				
[1]	j!1	_	4	=	0	
[2]	j!1	_	3	=	0	
[3]	j!1	_	2	=	0	
[4]	j!1	-	1	=	0	
[5]	j!1	=	0			

 Table 1. SPM_noauth_tr result

The sequent in Table 1 clearly cannot be proved. All antecedent lines, denoted with negative line numbers above the *turnstile* (I---) represent conjunctive assumptions that, if true, imply disjunctively one or more of the consequent propositions below the turnstile. That is,

([-1] AND {-2}) IMPLIES ([1] OR [2] OR [3] OR [4] OR [5])

It may not be apparent at first glance, that this sequent is invalid. But, if we replace j!1 with x for clarity, the PVS-prover sequent reads as follows:

This can be further reduced to the following assertion, which is clearly incorrect:

(x = 5) IMPLIES (x = 4 OR x = 3 OR x = 2 OR x = 1 OR x = 0)



Figure 16. SPM_noauth_tr Proof Tree

The PVS-generated proof summary for this modification in Figure 17 shows that,

although the necessary conditions implied by the theory were proved, the theory itself

remains unproved. This result is, again, the correct result for this test:

```
Proof summary for theory SPM_noauth_tr

tr_find_zero_TCC1.....proved - complete [SHOSTAK](0.67 s)

tr_find_zero_TCC2.....proved - complete [SHOSTAK](0.27 s)

System_correct....unfinished [SHOSTAK](35.90 s)

Theory totals: 3 formulas, 3 attempted, 2 succeeded (36.84 s)
```

Figure 17. PVS proof summary for SPM_noauth_tr

Scenario 7 - Unauthorized Create

Below is a test scenario modification for the SPM in which all of the conditions to enable a create operation are valid, but the *cc_Authorized?* flag has inadvertently been set to FALSE. The expected result is PVS will be unable to prove the theorem, because the theorem relies on the flag to reflect whether the event in *Event_2?* should have happened under the established conditions.

Encoding.

The only modification necessary for this test was to set the flag to FALSE in the

Setup function, as shown here:

% Set the expected outcome for an attempted create
cc_Authorized? := FALSE,

When the proof reaches the *Test_2* function, the function passes the state *snapshot*

to *Event_2*? to determine whether the event of interest in this case has occurred.

Event_2? returns the boolean value of the statement

Event_2?(snapshot: State_template): boolean =
 (member(LaserJet_1, snapshot`Entities))

which resolves to TRUE because LaserJet_1 was added to Entities under these valid

conditions. Since the IF condition is TRUE, the logic proceeds to the THEN statement,

setting the value of *State_OK* to the current value of *cc_Authorized*?, which in this case is

FALSE.

Results.

The proof of the *System_correct* theorem with this test modification progressed as shown in Figure 18 until the sequent in Table 2 was encountered, and no further progress was possible. In this test, this was the expected result, which indicates that the model is working as desired. Otherwise, a different proof strategy could be entered interactively at this point, or this sequent could be used to isolate the flaw in the original design.

Table 2. SPM_noauth_cc result

[-1] {-2}	j!1 >= 0 j!1 - 3 = 0
 [1]	j!1 - 2 = 0
[2]	j!1 - 1 = 0 j!1 = 0

The sequent in Table 2 cannot be proved. All antecedent lines, denoted with negative line numbers above the *turnstile* (I---) represent conjunctive assumptions that, if true, imply disjunctively one or more of the consequent propositions below the turnstile. That is,

([-1] AND {-2}) IMPLIES ([1] OR [2] OR [3]).

If we replace j!1 with x for clarity, the PVS-prover sequent reads

(x >= 0 AND x - 3 = 0) IMPLIES (x - 2 = 0 OR x - 1 = 0 OR x = 0). This can be further reduced to the following assertion, which is clearly incorrect



Figure 18. SPM_noauth_cc Proof Tree

The PVS-generated proof summary for this modification in Figure 19 shows that, although the necessary conditions implied by the theory were proved, the theory itself remains unproved. This result is, again, the correct result for this test:

```
Proof summary for theory SPM_noauth_cc

tr_find_zero_TCC1.....proved - complete [SHOSTAK](0.67 s)

tr_find_zero_TCC2.....proved - complete [SHOSTAK](0.27 s)

System_correct.....unfinished [SHOSTAK](35.90 s)

Theory totals: 3 formulas, 3 attempted, 2 succeeded (36.84 s)
```

Figure 19. PVS proof summary for SPM_noauth_cc

Test Scenario 8 - Introduced Error

Below is a test scenario modification for the SPM in which an inappropriate transfer is allowed to occur, to demonstrate how the PVS prover treats an unprovable theory. In this experiment, we temporarily violate the model by allowing a transfer to occur in spite of the failure of the first test, which ensures that the initiator of the transfer is in possession of the ticket which is being transferred. The PVS prover should *not* be able to prove that *State_OK* will hold TRUE in this invalid SPM model.

Encoding.

As in Test Scenario 1, the addition of the ticket *myfile_rc* to *Bob*'s domain is

prevented from happening by commenting out that section of the Setup function.

% Add myfile_rc to Bob's Domain %Domain := snapshot`Domain WITH [% (Bob) := add(myfile_rc, snapshot`Domain(Bob))],

Since *Bob*'s possession of the ticket is a necessary condition to allow the transfer, the ticket should not be appear in *Alice*'s domain. The test condition *tr_Authorized*? is set to FALSE in the *Setup* function to indicate that the transfer should not be allowed.

```
tr_Authorized? := FALSE,
```

However, the ELSE statement in transition function $L3_1$ has been changed for this test. Instead of jumping to $L7_1$ and skipping the ticket transfer, the program counter (*PC*) is set to $L6_1$ for the next iteration.

```
L3_1: snapshot WITH [PC :=

IF (member(myfile_rc, snapshot`Domain(Bob)))

AND

myfile_rc`copyable? THEN L4_1

ELSE L6_1

ENDIF],
```

The transition function $L6_1$ sets the PC to $L7_1$ and passes the current state,

encapsulated in *snapshot*, to the *Exec_1* function, where *myfile_r* is added to *Alice*'s domain.

% Execute the transfer and increment PC L6_1: Exec_1(snapshot) WITH [PC := L7_1],

The transition function $L7_1$ sets PC to the terminal value LEND_1, and passes

snapshot to the *Test_1* function for a determination of whether the model has correctly implemented this condition of SPM.

% Test State_OK and move PC to end L7_1: Test_1(snapshot) WITH [PC := LEND_1],

The *Test_1* function passes the state *snapshot* to *Event_1*? to determine whether the event of interest in this case has occurred. *Event_1*? returns the boolean value of the statement

```
member(myfile_r, snapshot`Domain(Alice))
```

which resolves to TRUE because *myfile_r* was added to *Alice*'s domain by *Exec_1*. Since the IF condition in *Test_1* is TRUE, *State_OK* is set to the value of *tr_Authorized*? within snapshot, which has been set to FALSE, indicating that the transfer was unauthorized.

Results.

The proof of the *System_correct* theorem with this invalidated SPM model progressed as shown in Figure 20 until the sequent in Table 3 was encountered, and no further progress was possible. In this test, this was the expected result of trying to prove the properties of SPM for an invalid model.

Та	able 3.	spm_	_broken resul	t
	[-1] {-2}	j!1 j!1	>= 0 - 3 = 0	
	 [1] [2] [3]	j!1 j!1 j!1	$ \begin{array}{rcrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	

The sequent in Table 3 can be further reduced to the following assertion, which is clearly incorrect



Figure 20. SPM_broken Proof Tree

Figure 21 is the PVS-generated proof summary for this modification. It shows

that the theory has yet to be proved, although the TCCs for the theory were proved.

Proof summary for theory SPM_broken	
<pre>tr_find_zero_TCC1proved - complete</pre>	[SHOSTAK](0.68 s)
<pre>tr_find_zero_TCC2proved - complete</pre>	[SHOSTAK](0.27 s)
System_correctunfinished	[SHOSTAK](35.90 s)
Theory totals: 3 formulas, 3 attempted, 2 succeeded (36.	85 s)

Figure 21. PVS proof summary for SPM_broken

Summary

The Schematic Protection Model describes the conditions under which rights can be transferred from one entity to another, and new entities can be created in the system. These conditions test the model's ability to prevent transition to an unsecure state. Each of these conditions was tested in the preceding scenarios.

Each test produced the expected results. The absence of a required precondition to process a ticket transfer: originator-possession of the copyable ticket, a valid link to the recipient, or the absence of an enabling filter function; resulted, in each case, in the prevention of the transfer. And the absence of a can-create rule was shown to prevent the unauthorized create operation.

The correct functionality of the *tr_Authorized*? and *cc_Authorized*? flags was also tested. The *Test_1* and *Test_2* functions rely on these flags for the correct interpretation of the other tests. Finally, a test was run against an altered specification that does not correctly model SPM, to demonstrate that an attempt to prove it correct fails, as expected.

V. Conclusion

Contribution

The formal specification of the Schematic Protection Model provides a tool for reasoning about systems that implement the SPM security model. It is designed to be easily modifiable to incorporate any logical extensions that can be expressed algorithmically, such as the deontic logic properties of obligation, permission, possibility, and necessity. The specification is robust; it accepts the modular addition of autonomous *virtual processors* that can each implement any set of operations that can be described algorithmically. As such, this specification is a solid, flexible tool for formally reasoning about any security model that can be expressed in this manner.

This tool can now be used as the basis for further use of SPM to meet the modeling challenges posed by contemporary cyber systems. Proposed modifications can be added systematically to the specification to formally demonstrate correctness of both the autonomous modification and the integrated model as a whole.

Reliability of Results

This research proved the safety properties of the Schematic Protection Model, using the Prototype Verification System automated prover. The results are, of course, only as reliable as the prover itself. However, the uncertainty of this is mitigated by the widespread use of PVS by researchers and scientists worldwide since 1993. PVS has been used extensively within the scientific and academic communities [SRI08] to formally express well-known mathematical theorems and algorithms, and has yielded proofs that are consistent with expected results. These include the Fundamental

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Theorems of both Arithmetic and Calculus, the Infinitude of Primes, and the Law of Cosines [NAS07]. It has also been used to formally verify complex, real-world systems, revealing inconsistencies that would have otherwise been practically undiscoverable, such as during the formal analysis of the AAMP5 microprocessor [NAS07].

Suggestions for Further Research

SPM Modernization.

It will be worthwhile to reassess SPM for its applicability to modern cyber systems. SPM was proposed in 1988 as a tool for modeling and reasoning about computer systems. While the complexity and interdependence of automated systems have advanced dramatically in both practice and theory keeping pace with enablingadvances in technology, no popularly accepted analytical techniques have emerged in kind. As a result, these models, including SPM, are rarely used to reason about actual systems. It would be useful to identify specific extensions or modifications to the original model, to reestablish the ability to formally reason about actual modern cyber systems.

Deontic Logic.

A broader range of practical applicability may be realized by extending the SPM with modal logic concepts such as obligation, permission, possibility, and necessity. Deontic logic provides the "right fundamental logic system to provide us with a logical validity criterion of normative reasoning as well as a formal representation and specification language" while Classical Mathematical Logic (CML) fails to describe the notion of relevance when accounting for the validity of a statement. In CML, "the notion of conditional, which is intrinsically intensional but not truth-functional, is represented by the notion of material implication, which is intrinsically an extensional truth-function"

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[ChM06]. It is through these implications that the idea of vacuous truth arises, where a statement is regarded as TRUE simply because the premise itself is FALSE. The more expressive relationships between actors and actions offered by deontic logic would expand the field of scenarios about which the system is capable of reasoning.

Safety Analysis.

This specification presented herein can be modified to perform safety analysis of an explicitly described system by adding a virtual processor module that recursively executes all allowable transfer- and create-operations until no more are possible. It is only the resultant *maximal* state that need be tested for adherence to stated policy to make a determination about the safety of the system design. It is important to note that in order to ensure a maximal state is reached, the create-operations must be both acyclic and attenuating. Acyclicity means simply that no descendent of entity-type x can create an entity of type x. This rule simplifies the safety analysis by ensuring that create-operations do not continue recursively ad infinitum [Bis03, pg. 70]. Attenuation is considered with respect to tickets that are given to the new entity spawned by a create operation. An entity may not give a ticket to another entity that it does not, itself, possess.

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- [Ubh03] Sonali Ubhayakar, Evaluation of Program Specification and Verification Systems, Thesis/Naval PostGraduate School, June 2003. (ADA417580)

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14. ABSTRACT This research formally specifies the Schematic Protection Model (SPM) to prove its ability to provide security services such as confidentiality and integrity. The theory described by the resultant model was logically proved in the Prototype Verification System (PVS). Each component of SPM was tested, as were several anomalous conditions, and each test produced results consistent with the model. The model is internally modular, and therefore easily extensible, yet cohesive since the theory to be proved encompasses the entire specification. This approach ensures the specification is flexible enough to incorporate any extensions, such as the deontic logic properties of obligation, permission, possibility and necessity. The culmination of this effort was the development of a sound, flexible tool for reasoning formally about systems that implement a security model like SPM. Recommendations to further extend the utility of the specification are discussed.								
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