Design of an Oxygen Turbopump for a Dual Expander Cycle Rocket Engine

William S. Strain

Follow this and additional works at: https://scholar.afit.edu/etd

Part of the Propulsion and Power Commons

Recommended Citation
DESIGN OF AN OXYGEN TURBOPUMP FOR A DUAL EXPANDER CYCLE ROCKET ENGINE

THESIS

William S. Strain, Captain, USAF

AFIT/GAE/ENY/08-M26

DEPARTMENT OF THE AIR FORCE
AIR UNIVERSITY
AIR FORCE INSTITUTE OF TECHNOLOGY
Wright-Patterson Air Force Base, Ohio

APPROVED FOR PUBLIC RELEASE; DISTRIBUTION UNLIMITED
The views expressed in this thesis are those of the author and do not reflect the official policy or position of the United States Air Force, Department of Defense, or the U.S. Government.
DESIGN OF AN OXYGEN TURBOPUMP FOR A DUAL EXPANDER CYCLE ROCKET ENGINE

THESIS

Presented to the Faculty
Department of Aeronautics and Astronautics
Graduate School of Engineering and Management
Air Force Institute of Technology
Air University
Air Education and Training Command
In Partial Fulfillment of the Requirements for the
Degree of Master of Science in Aeronautical Engineering

William S. Strain, BS
Captain, USAF

March 2008

APPROVED FOR PUBLIC RELEASE; DISTRIBUTION UNLIMITED
DESIGN OF AN OXYGEN TURBOPUMP FOR A DUAL EXPANDER CYCLE ROCKET ENGINE

William S. Strain, BS
Captain, USAF

Approved:

______________________________  ___________________________
Richard D. Brannam, Maj, USAF (Chairman)  Date

______________________________  ___________________________
Robert B. Greendyke (Member)  Date

______________________________  ___________________________
Paul I. King (Member)  Date
Acknowledgments

I would like to express my sincere appreciation to my faculty advisor, Maj Richard Branam, for his guidance and support throughout the course of this thesis effort. The insight, experience and help was greatly appreciated. I would also like to thank Capt Michael Arguello for his help with aesthetic issues and for serving as a sounding board during the design process.

I would also like to thank my grandfather for the love and support he gave me during his life, and the work ethic and persistence he instilled in me. My thanks also go to Dr. Elias C. Mattas whose design class taught me how to think through the design process, be it for a refinery or a rocket engine, and whose kind recommendation played no small role in my acceptance to OTS. My sincerest thanks and deep gratitude also to Dr. Perwaiz Meraj, M.D. whose support was vital during a very difficult time in my life and whose friendship has made me happier and healthier for over a decade.

William S. Strain
Table of Contents

Acknowledgments....................................................................................................v
Table of Contents................................................................................................... vi
List of Figures ...................................................................................................... viii
List of Tables ......................................................................................................... ix
Nomenclature.........................................................................................................x
Abstract................................................................................................................ xiv

1 Introduction......................................................................................................1
  1.1 Motivation ...............................................................................................1
  1.2 Problem Statement...................................................................................4
  1.3 Research Goals........................................................................................4
  1.4 Research Focus........................................................................................5

2 Literature Review.............................................................................................6
  2.1 Current Systems.......................................................................................6
    2.1.1 Pratt & Whitney RL10 .................................................................... 6
    2.1.2 LE-5B .............................................................................................. 8
    2.1.3 Vinci ................................................................................................ 9
    2.1.4 Aerojet Orbital Transfer Vehicle Engine ...................................... 10
  2.2 Technical Issues.....................................................................................14
    2.2.1 Materials ....................................................................................... 14
    2.2.2 Bearings ........................................................................................ 16
    2.2.3 Hydraulic Design and Throttleability ........................................... 17

3 Methodology ..................................................................................................19
  3.1 Initial Power Balance .............................................................................19
3.2 Pump Design ...........................................................................................................22
  3.2.1 Impeller Inlet ............................................................................................... 23
  3.2.2 Impeller Outlet ......................................................................................... 24
  3.2.3 Volute ........................................................................................................ 24
  3.2.4 Analysis Mode ......................................................................................... 27
3.3 Turbine Design .......................................................................................................33
  3.3.1 Preliminary Sizing .................................................................................... 33
  3.3.2 Final Design ............................................................................................. 35
4 Results .....................................................................................................................38
  4.1 Pump Results .................................................................................................. 38
  4.2 Turbine Results ............................................................................................. 44
  4.3 Sensitivity Analysis ...................................................................................... 49
  4.4 Shaft and Bearings ....................................................................................... 51
5 Conclusions and Recommendations .................................................................55
  5.1 Conclusions .................................................................................................. 55
  5.2 Recommendations for Future Research ..................................................... 57
Appendix A ............................................................................................................... 58
Bibliography ..............................................................................................................64
Vita .............................................................................................................................68
# List of Figures

<table>
<thead>
<tr>
<th>Figure</th>
<th>Description</th>
<th>Page</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Dual Expander Cycle Engine Schematic</td>
<td>3</td>
</tr>
<tr>
<td>2</td>
<td>RL-10 Schematic</td>
<td>8</td>
</tr>
<tr>
<td>3</td>
<td>Vinci flow schematic</td>
<td>10</td>
</tr>
<tr>
<td>4</td>
<td>Control and flow schematic of the Aerojet dual expander cycle</td>
<td>12</td>
</tr>
<tr>
<td>5</td>
<td>Schematic of friction rubbing test apparatus</td>
<td>15</td>
</tr>
<tr>
<td>6</td>
<td>Schematic of particle test apparatus</td>
<td>16</td>
</tr>
<tr>
<td>7</td>
<td>Design process block diagram</td>
<td>21</td>
</tr>
<tr>
<td>8</td>
<td>Blockage correction for Station 8 pressure recovery</td>
<td>26</td>
</tr>
<tr>
<td>9</td>
<td>Diffusion Ratio/Specific Speed Function used by Pumpal</td>
<td>30</td>
</tr>
<tr>
<td>10</td>
<td>Final impeller</td>
<td>39</td>
</tr>
<tr>
<td>11</td>
<td>Pump Overall Performance Map</td>
<td>40</td>
</tr>
<tr>
<td>12</td>
<td>Pump Power Curve</td>
<td>42</td>
</tr>
<tr>
<td>13</td>
<td>Pump Map with Surge Line</td>
<td>43</td>
</tr>
<tr>
<td>14</td>
<td>NPSH Curve</td>
<td>44</td>
</tr>
<tr>
<td>15</td>
<td>Turbine rotor</td>
<td>46</td>
</tr>
<tr>
<td>16</td>
<td>Variation of total efficiency with velocity ratio</td>
<td>47</td>
</tr>
<tr>
<td>17</td>
<td>Variation of corrected mass flow with expansion ratio</td>
<td>48</td>
</tr>
<tr>
<td>18</td>
<td>Total efficiency variation with specific speed</td>
<td>49</td>
</tr>
<tr>
<td>20</td>
<td>Bearing arrangement</td>
<td>53</td>
</tr>
<tr>
<td>21</td>
<td>Final integrated rotor</td>
<td>54</td>
</tr>
</tbody>
</table>
## List of Tables

<table>
<thead>
<tr>
<th>Table</th>
<th>Description</th>
<th>Page</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>IHPRPT Goals for Boost and Orbit Transfer</td>
<td>2</td>
</tr>
<tr>
<td>2</td>
<td>LE-5B Performance Characteristics</td>
<td>9</td>
</tr>
<tr>
<td>3</td>
<td>Aerojet LOX Pump Design Point</td>
<td>13</td>
</tr>
<tr>
<td>4</td>
<td>Aerojet LOX Pump Design Point Parameters</td>
<td>13</td>
</tr>
<tr>
<td>5</td>
<td>Summary Material Ignition Results</td>
<td>16</td>
</tr>
<tr>
<td>6</td>
<td>Preliminary Pump Characteristics</td>
<td>18</td>
</tr>
<tr>
<td>7</td>
<td>Turbopump Design Point</td>
<td>22</td>
</tr>
<tr>
<td>8</td>
<td>Pumpal Inputs</td>
<td>22</td>
</tr>
<tr>
<td>9</td>
<td>Initial Turbine Design Inputs</td>
<td>33</td>
</tr>
<tr>
<td>10</td>
<td>Pump Design and Performance Parameters</td>
<td>38</td>
</tr>
<tr>
<td>11</td>
<td>Turbine Design and Performance Parameters</td>
<td>45</td>
</tr>
<tr>
<td>12</td>
<td>Sensitivity Analysis</td>
<td>50</td>
</tr>
<tr>
<td>13</td>
<td>Axial Loads and Fatigue Limits</td>
<td>53</td>
</tr>
</tbody>
</table>
# Nomenclature

## Acronyms

<table>
<thead>
<tr>
<th>Acronym</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>DEAN</td>
<td>Dual Expander Aerospike Nozzle</td>
</tr>
<tr>
<td>EELV</td>
<td>Evolved Expendable Launch Vehicle</td>
</tr>
<tr>
<td>IHPRPT</td>
<td>Integrated High Payoff Rocket Propulsion Technology</td>
</tr>
<tr>
<td>I_sp</td>
<td>Specific Impulse (s)</td>
</tr>
<tr>
<td>JAXA</td>
<td>Japanese Aerospace Exploration Agency</td>
</tr>
<tr>
<td>LOX</td>
<td>Liquid Oxygen</td>
</tr>
<tr>
<td>NIST</td>
<td>National Institute of Standards and Technology</td>
</tr>
<tr>
<td>NPSH</td>
<td>Net Positive Suction Head</td>
</tr>
<tr>
<td>NPSS</td>
<td>Numerical Propulsion Simulation System</td>
</tr>
</tbody>
</table>

## Symbols

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>Area (ft² or m²)</td>
</tr>
<tr>
<td>AR</td>
<td>Area Ratio</td>
</tr>
<tr>
<td>B</td>
<td>Blockage</td>
</tr>
<tr>
<td>C</td>
<td>Absolute Flow Velocity (ft/s or m/s) or Blade Cord (Eq. 49) (in or cm)</td>
</tr>
<tr>
<td>c*</td>
<td>Characteristic Velocity (ft/s or m/s)</td>
</tr>
<tr>
<td>DR</td>
<td>Diffusion Ratio</td>
</tr>
<tr>
<td>g_o</td>
<td>acceleration due to gravity at sea level (ft/s² or m/s²)</td>
</tr>
</tbody>
</table>

x
<table>
<thead>
<tr>
<th>Symbol</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>h</td>
<td>Specific Enthalpy (ft²/s² or m²/s²)</td>
</tr>
<tr>
<td>H</td>
<td>Head (ft or m)</td>
</tr>
<tr>
<td>I</td>
<td>Incidence (degrees)</td>
</tr>
<tr>
<td>LC</td>
<td>Loss Coefficient</td>
</tr>
<tr>
<td>N</td>
<td>Rotational Speed (RPM)</td>
</tr>
<tr>
<td>P</td>
<td>Pressure (psi or Pa) or Power (hp or kW) (Chap.3)</td>
</tr>
<tr>
<td>Q</td>
<td>Volumetric Flow Rate (ft³/s or m³/s)</td>
</tr>
<tr>
<td>R</td>
<td>Radius (in or cm) or exhaust gas constant (eq. C)</td>
</tr>
<tr>
<td>s</td>
<td>Specific Entropy</td>
</tr>
<tr>
<td>U</td>
<td>Blade Tip Speed (ft/s or m/s)</td>
</tr>
<tr>
<td>W</td>
<td>Relative Velocity (ft/s or m/s)</td>
</tr>
<tr>
<td>Z</td>
<td>Blade Number</td>
</tr>
<tr>
<td>(m)</td>
<td>Mass Flow Rate (lbm/s or kg/s)</td>
</tr>
</tbody>
</table>
Greek Symbols

ε  Secondary Area Ratio; exit clearance; nozzle expansion ratio
χ  Secondary Mass Fraction
ρ  Density (lbm/ft³ or kg/ m³)
α  Flow Angle (degrees)
ψ  Loading Coefficient
φ  Flow Coefficient
β  Relative Flow Angle (degrees); Subscript b Denotes Blade Angle
σ  Slip Factor
ξ  Meridional Velocity Ratio
η  Efficiency
γ  Heat capacity ratio
λ  Nozzle efficiency; inlet swirl parameter

Station Numbering

Pump

0  Up Stream/ Stage Inlet
1  Impeller Inlet
2  Impeller Exit
5  Diffuser Exit
7  Volute Throat
8 Stage Exit

_Turbine_

4 Rotor Inlet
6 Rotor Exit

Subscripts

0 Denotes Total Conditions

c Combustion

e Exit

i Inlet

m Meridional

p pump

t Tangential

T Turbine
Abstract

The design of a pump intended for use with a dual expander cycle (LOX/H₂) engine is presented. This arrangement offers a number of advantages over hydrogen expander cycles; among these are the elimination of gearboxes and inter-propellant purges and seals, an extended throttling range, and higher engine operating pressures and performance. The target engine has been designed to meet the needs of Phase III of the Integrated High Payoff Rocket Propulsion Technology (IHPRPT) program; thus, this pump must meet the program’s reliability, maintainability, and service life goals. In addition, this pump will be driven by warm gaseous oxygen. In order to meet the needs of this engine, the pump will need to be capable of delivering 106 lbm/s (48.1 kg/s) at 4500 psi (31 MPa); this will necessitate a turbine capable of supplying at least 2215 hp (1652 kW). The pump and turbine were designed with the aid of an industry standard design program; the design methodology and justification for design choices are presented. Appropriate materials of construction and bearings for this pump are discussed.
CONCEPTUAL DESIGN OF AN OXYGEN PUMP FOR USE IN A DUAL-EXPANDER CYCLE ENGINE

1 Introduction

1.1 Motivation

The Integrated High-Payoff Rocket Propulsion Technology (IHPRPT) program was initiated in 1994 with the goal of doubling US rocket propulsion capabilities by 2010 (as measured against the 1993 baseline). The goals are summarized in Table 1, taken from Blair and DeGeorge. The main goals of interest are increased payload (which this effort will accomplish by increasing Isp of the upper stage), cost reduction and reliability improvement. Additionally, as this program envisions the use of a reusable launch vehicle, the ability to perform aircraft-like operations and thus reliability and maintainability is highly valued.

The Centaur upper stage used on both EELV variants (the Delta IV and Atlas V) is powered by the RL-10 engine, described in detail in section 2. The heavy variants of these launch systems are capable of boosting payloads of 21,890 kg to LEO and 6,280 kg to GEO. When compared to foreign counterparts, the US appears to be falling behind in its technological advantage. The H-IIA, operated by the Japanese Aerospace Exploration Agency (JAXA), utilizes an LE-5B upper stage engine. This vehicle has a LEO (300 km, circular 30° orbit) payload capability of 10,000 kg (22,000 lb). The Ariane 5 ESC-B upper stage powered by the Vinci engine has payload capacity of 12,000 kg (26,400 lb) to geostationary transfer orbit.
<table>
<thead>
<tr>
<th>Boost and Orbit Transfer Propulsion</th>
<th>Phase I</th>
<th>Phase II</th>
<th>Phase III</th>
</tr>
</thead>
<tbody>
<tr>
<td>Reduce Stage Failure Rate</td>
<td>25%</td>
<td>50%</td>
<td>75%</td>
</tr>
<tr>
<td>Improve Mass Fraction (Solids)</td>
<td>15%</td>
<td>25%</td>
<td>35%</td>
</tr>
<tr>
<td>Improve $I_{sp}$ (Solids)</td>
<td>2%</td>
<td>4%</td>
<td>8%</td>
</tr>
<tr>
<td>Improve $I_{sp}$ (sec) (Liquids)</td>
<td>14</td>
<td>21</td>
<td>26</td>
</tr>
<tr>
<td>Reduce Hardware Cost</td>
<td>15%</td>
<td>25%</td>
<td>35%</td>
</tr>
<tr>
<td>Reduce Support Costs</td>
<td>15%</td>
<td>25%</td>
<td>35%</td>
</tr>
<tr>
<td>Improve Thrust to Weight (Liquids)</td>
<td>30%</td>
<td>60%</td>
<td>100%</td>
</tr>
<tr>
<td>Mean Time Between Removal (Mission Life: Reusable)</td>
<td>20</td>
<td>40</td>
<td>100</td>
</tr>
</tbody>
</table>

In support of the IHPRPT goals, a study was performed at AFIT to examine the design of a dual expander cycle upper stage LOX/H₂ engine with an aerospike nozzle to accomplish IHPRPT Phase III goals. The LOX/H₂ combination was chosen because of its potential to achieve high $I_{sp}$ values relative to other liquid propellant systems such as LOX/RP. Maximizing $I_{sp}$ in an upper stage has a greater positive effect on payload capacity than doing likewise in a first stage. This engine, shown schematically in Figure 1, was designed with a target $I_{sp}$ of 464 s and a thrust goal of 50,000 lbf (222 kN). In the phase III concept engine, LOX will be used to cool the chamber wall while H₂ is used to cool the nozzle and aerospike. Each propellant is to have its own pump and turbine driven by heat pickup from the respective cooling circuits. This arrangement negates the need for a gearbox required for single-turbine engines such as the one employed on the current upper stage engine, the Pratt & Whitney RL-10. Avoiding the use of a gearbox will result in lower weight and greater operability for the dual expander concept. Additionally, this approach will eliminate the inter-propellant seal and purge fluid systems necessary in a hydrogen-only expander cycle. The elimination of this seal eliminates the critical failure possibility; however, it will also require hot oxygen tolerant
turbine materials.9

Further, a dual expander cycle is better suited to the high cycle life, mean time between removal, and throttleability targets since the heat pickup demands on the hydrogen circuit are less than for a comparable hydrogen expander cycle.10 The elimination of the inter-propellant seals and purges also facilitates the reliability goal when many restarts will be required. In comparison to other rocket cycles, an expander cycle engine is also inherently safer, as it avoids the use of multiple combustion chambers. Finally as mentioned by Buckmann, et al., this cycle delivers the propellants to the combustion chamber as superheated gases, resulting in an injector pressure drop which varies
approximately as mass flow instead of mass flow squared. This feature will help maintain stable chamber conditions when the engine is throttled.

1.2 Problem Statement

In order to continue to meet the nation’s space lift goals, the Air Force must improve its orbital transfer vehicle capabilities, which necessitates improvements in upper-stage engines; this need is the driving force behind the IHPRPT program. The Dual Expander Aerospike Nozzle (DEAN) engine has been designed to meet the 2010 goals set out in the Phase III IHPRPT program. This engine concept will require an oxygen pump capable of supporting the program’s reliability, maintainability, and service life goals while delivering the required flow at the required pressure. Additionally, this pump must be powered by (and thus be resistant to) hot oxygen and have the ability to operate stably over a range of flow rates.

1.3 Research Goals

This effort details the design of an oxygen turbopump required by a dual expander cycle upper stage engine intended to meet the Phase III IHPRPT requirements. The primary objectives of this effort are fourfold:

1. to deliver LOX flow at the operating conditions required by this engine
2. to include design features supporting reliability goals of the IHPRPT Phase III requirements
3. to analyze throttling capability over a range of flow rates
4. to ensure the pump concept can support aircraft-like operations, is maintainable and reusable with acceptable service life.

1.4 Research Focus

This work focuses on the design of the impeller and turbine necessary for this pump. Of most interest is the design of the components, especially the turbine rotor and pump impeller necessary for this pump to achieve the performance, maintainability, and reliability goals set out by the Phase III IHPRPT program. Further, the components must be capable of supporting throttled operation, thus off-design performance will be important. Finally, this work will explore the materials and bearings required for the pump to be successful.
2 Literature Review

This chapter starts with a survey of current and planned LOX/H₂ upper-stage engines and their LOX pumps. It concludes with an exploration of details of design features critical to pump success and the attainment of the objectives set out in Chapter 1.

2.1 Current Systems

Due to unique advantages of LOX/H₂ upper-stage engines, such as greater I\(_{sp}\), there are a number in use today. These include the RL-10 which powers the Centaur upper stage on both EELV variants, the LE-5 used by the Japanese Aerospace Exploration Agency (JAXA), and the Vinci used by the European Space Agency (ESA). This section will discuss these with special attention paid to their LOX pumps, and conclude with an Aerojet effort which developed a LOX pump intended for an upper stage application.

2.1.1 Pratt & Whitney RL10

The RL-10 is used on the Centaur and has a long track record as a reliable engine having been originally developed in the 1960s, and it was the first flight engine to have bearings lubricated and cooled by liquid hydrogen.\(^{11,12}\) As shown in Figure 2, it relies on a hydrogen expander cycle to power the turbine and a geared arrangement to drive both the LOX and H₂ pumps.\(^{13}\) The RL10-A4’s LOX pump delivers 17.78 kg/s (39.1 lb/s) at 5,725 kPa (830.6 psi) with a design speed of 14300 rpm. As noted by Brannam, et al\(^{14}\), the hydrogen expander cycle used by this engine is capable of only modest improvements over the baseline RL-10A-3-3A. This engine’s growth potential is limited due to power extraction requirements from the cooling circuit.
The hydrogen must be heated to temperatures near the design limit for alloys currently used in the chamber liner.

Other limits of this engine cycle that make it an unattractive candidate for this application include:

1. While the RL-10 is designed to have restart capability, it is designed for a relatively short life.

2. The RL-10 has a high parts count, a large gearbox vital to its operation, and requires many hours of touch labor, suggesting that it would be difficult to achieve the IHPRPT maintainability goal with this type of engine configuration.

3. A single expander cycle is capable of only a limited throttling range. When other IHPRPT goals such as mean time between removal, the ability to have multiple starts, and throttleability are considered, the limitations of this cycle make it a less than ideal candidate for this application.
2.1.2 LE-5B

The LE-5 is used on the upper stage of the Japanese H-II rocket.\textsuperscript{15} It uses a single expander cycle to power both LOX and H\textsubscript{2} pumps with H\textsubscript{2} as the drive gas for both turbines, and is designed to deliver 137 kN (30,800 lb) of thrust with a specific impulse of 448 s. Its attributes are summarized in Table 2. Its LOX pump delivers 19.4 kg/s (42.7 lb/s) at a design speed of 17,000 rpm. Throttling and the ability to have multiple burns with long coast phases were two design priorities during the development of this engine. It is expensive compared to other similar engines.\textsuperscript{15} Like the Vinci engine (below), it requires an inter-propellant seal and purge system for the oxygen turbopump.
### Table 2: LE-5B Performance Characteristics

<table>
<thead>
<tr>
<th></th>
<th>LE-5B</th>
<th>LE-5A</th>
</tr>
</thead>
<tbody>
<tr>
<td>Thrust (in Vacuum) [kN]</td>
<td>137</td>
<td>122</td>
</tr>
<tr>
<td>Isp (in vacuum) [sec]</td>
<td>450</td>
<td>453</td>
</tr>
<tr>
<td>Engine Mixture Ratio</td>
<td>5</td>
<td>5</td>
</tr>
<tr>
<td>Chamber Pressure [MPa]</td>
<td>3.6</td>
<td>4.0</td>
</tr>
<tr>
<td>FTP Rotational Speed [rpm]</td>
<td>50200</td>
<td>50500</td>
</tr>
<tr>
<td>LTP Rotational Speed [rpm]</td>
<td>17100</td>
<td>17400</td>
</tr>
<tr>
<td>Turbine Inlet Temperature [K]</td>
<td>380</td>
<td>600</td>
</tr>
</tbody>
</table>

#### 2.1.3 Vinci

The Vinci is the upper stage of the Ariane 5. It has a design thrust of 180 kN (40,000 lb), a design Isp of 464 s and uses an expander cycle, as shown in Figure 3. Similar to the LE-5B, H₂ is the drive gas for both turbines. It is intended to be capable of five restarts. While the dual-turbine design eliminates the need for a gearbox (as in the RL-10), it requires an inter-propellant seal and associated purge system for the oxygen turbopump, which will add weight and negatively impact reliability and maintainability. Thus, this engine cycle is not the ideal candidate for IHPRPT Phase III application.
2.1.4 Aerojet Orbital Transfer Vehicle Engine

Beginning in July of 1983, Aerojet designed and built an oxygen turbopump intended for use in a dual expander cycle engine on an orbital transfer vehicle. This engine is shown schematically in Figure 4 and, unlike the target engine considered in this work, this engine does not use an aerospike nozzle. Additionally, this engine will require an H2/O2 heat exchanger that the DEAN will not. As a result, this engine does not offer the potential weight savings of the DEAN. This engine design produces 3,750 lb\textsubscript{f} of thrust; design parameters for the oxygen pump are shown in Tables 3 and 4. This pump was designed with a two-stage impeller and a single...
stage, full admission turbine. A boost pump was required, driven by a hydraulic turbine supplied by a tap-off from the inducer discharge. The rolling element bearings have reliability issues and life limitations due to the high operating speed (75,000 rpm).\textsuperscript{7} To avoid these problems, LOX-lubricated hydrostatic bearings were deemed necessary to meet the service life goals (500 starts/20 hours between overhauls and 100 starts/4 hours with no service necessary\textsuperscript{17}). This pump was tested at speeds up to 69,800 rpm (93% of design speed) for a total run time of 37 minutes while driven by nitrogen. The pump achieved 88\% of its design discharge pressure when driven with ambient temperature oxygen. The bearings operated successfully, with no abnormal wear. However, hot oxygen testing was not performed\textsuperscript{17}. 
Figure 4: Control and flow schematic of the Aerojet dual expander cycle\textsuperscript{10}
**Table 3: Aerojet LOX pump design point**

<table>
<thead>
<tr>
<th></th>
<th>Boost Pump</th>
<th>High Pressure Pump</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of Stages</td>
<td>1</td>
<td>2</td>
</tr>
<tr>
<td>Weight Flow, lb/sec</td>
<td>5.5</td>
<td>5.5</td>
</tr>
<tr>
<td>Volume Flowrate- Inducer, gpm</td>
<td>-</td>
<td>51.4</td>
</tr>
<tr>
<td>Volume Flowrate- Impellers, gpm</td>
<td>34.7</td>
<td>34.7</td>
</tr>
<tr>
<td>Suction Pressure- psia</td>
<td>15.0</td>
<td>54.6</td>
</tr>
<tr>
<td>Discharge Pressure- psia</td>
<td>54.6</td>
<td>4654.6</td>
</tr>
<tr>
<td>Inducer Head Rise- ft</td>
<td>-</td>
<td>525</td>
</tr>
<tr>
<td>Head Rise per Stage- ft</td>
<td>80</td>
<td>4575</td>
</tr>
<tr>
<td>Speed, rpm</td>
<td>12,700</td>
<td>75,000</td>
</tr>
<tr>
<td>Stage Specific Speed, US units</td>
<td>2,722</td>
<td>787</td>
</tr>
<tr>
<td>Impeller Discharge Diameter- in</td>
<td>1.41</td>
<td>1.62</td>
</tr>
<tr>
<td>Impeller Discharge Port Width- in</td>
<td>0.097</td>
<td>.0812</td>
</tr>
<tr>
<td>Efficiency, %</td>
<td>65.0</td>
<td>59.0</td>
</tr>
<tr>
<td>Net Positive Suction Head, ft</td>
<td>0 (TSH = 4.3 ft)</td>
<td>80</td>
</tr>
<tr>
<td>Suction Specific Speed,</td>
<td>24,800</td>
<td>20,100</td>
</tr>
<tr>
<td>*TSH- Thermodynamic Suppression Head</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

**Table 4: Aerojet LOX pump design point parameters**

<table>
<thead>
<tr>
<th>Pump</th>
<th>LOX</th>
</tr>
</thead>
<tbody>
<tr>
<td>Weight Flow- lb/sec</td>
<td>5.5</td>
</tr>
<tr>
<td>Volume Flow- gpm</td>
<td>34.7</td>
</tr>
<tr>
<td>Pressure Rise- psi</td>
<td>4600</td>
</tr>
<tr>
<td>Speed- rpm</td>
<td>75000</td>
</tr>
<tr>
<td>Efficiency- %</td>
<td>59</td>
</tr>
<tr>
<td>Specific Speed, rpm, gpm ,ft</td>
<td>790</td>
</tr>
<tr>
<td>Turbine</td>
<td>GOX</td>
</tr>
<tr>
<td>Weight Flow- lb/sec</td>
<td>5.1</td>
</tr>
<tr>
<td>Inlet Temperature, °R</td>
<td>860</td>
</tr>
<tr>
<td>Inlet Total Pressure- psia</td>
<td>4315</td>
</tr>
<tr>
<td>Outlet Static Pressure- psia</td>
<td>2236</td>
</tr>
<tr>
<td>Efficiency (total-to static)- %</td>
<td>67</td>
</tr>
<tr>
<td>Horsepower- shp</td>
<td>156</td>
</tr>
</tbody>
</table>
2.2 Technical Issues

In order for a LOX pump to successfully fulfill the goals laid out in Chapter 1, a number of technical hurdles must be addressed. First, materials must be found that can tolerate both LOX (inducer and impeller) and hot oxygen (turbine). Bearings must be selected satisfying the reliability and service life goals. The impeller and diffuser must be designed in such a way as to maximize throttleability. Finally, sound design methods must be used to complete the hydraulic design of the inducer, impeller, and turbine.

2.2.1 Materials

Past LOX pumps intended for use on expendable platforms have successfully used impellers and casings fashioned from such materials as cast aluminum, stainless steel, Inconel 718, and K Monel.\textsuperscript{18,19,20} The use of the first two materials poses a fire risk due to a lack of ignition resistance in the event of a material rub. The casing on the LOX turbopump used in the Vulcain engine was changed from aluminum to Inconel after such a fire in the early 1990s.\textsuperscript{21} Turbine materials for such applications (which used LOX/RP-1 or LOX/H\textsubscript{2} combustion products as the drive gas) included Stellite 21, Hastelloy B and C, and Inconel 718.\textsuperscript{22} In contrast, this pump will use high-pressure, high velocity oxygen as the turbine drive fluid. It is thus very important from both a safety and reliability standpoint to ensure the turbine is fabricated from a material tolerant to this expected environment without experiencing damage and meeting service life goals.
Likewise, the impeller material must be resistant to the potential hazards of rubbing friction and foreign particle damage in a liquid oxygen environment.\textsuperscript{23} The ignition potential from a particle strike or metal rub in pure oxygen was identified by Brannam et al. as the main technology issue in the development of the Aerojet pump.\textsuperscript{14}

To assess the suitability of candidate materials for this type of service, Schoenman\textsuperscript{24} performed friction rubbing tests and particle impact tests in a high temperature gaseous oxygen environment. Apparatus for these tests are shown schematically in Figures 5 and 6, respectively. A summary of the results of both test results are shown in Table 5. Guided by similar data and the need to have acceptable mechanical properties (qualities lacking in the top three materials in Table 6), Buckmann et al. chose to construct their pump from Monel.\textsuperscript{9}

![Figure 5: Schematic of friction rubbing test apparatus\textsuperscript{24}](image)
Table 5: Summary material ignition results

<table>
<thead>
<tr>
<th>Material</th>
<th>Burn Factor</th>
<th>Observations</th>
</tr>
</thead>
<tbody>
<tr>
<td>Zirconium Copper</td>
<td>35</td>
<td>No ignition in any tests (790/1800°F)</td>
</tr>
<tr>
<td>Nickel 200</td>
<td>550</td>
<td>Ignition above 2200°F in FRT only (825/2200°F)</td>
</tr>
<tr>
<td>Silicon Carbide</td>
<td>1145</td>
<td>No ignition limited testing (850/-3°F)</td>
</tr>
<tr>
<td>Monel 400</td>
<td>1390</td>
<td>Ignition above 1200°F in FRT only (800/1200°F)</td>
</tr>
<tr>
<td>K-Monel 500</td>
<td>2090</td>
<td>Ignition above 1500°F in FRT (750/1500°F)</td>
</tr>
<tr>
<td>Inconel 600</td>
<td>3226</td>
<td>Ignition above 1100°F in FRT only (-1000°F)</td>
</tr>
<tr>
<td>316 Stainless Steel</td>
<td>4515</td>
<td>Ignition in all tests (450/800°F)</td>
</tr>
<tr>
<td>Invar-36</td>
<td>5444</td>
<td>Ignition in all tests (675/340°F)</td>
</tr>
<tr>
<td>Hastelloy-X</td>
<td>7160</td>
<td>Ignition in all tests (725/750°F)</td>
</tr>
</tbody>
</table>

2.2.2 Bearings

Bearing inspection and replacement is a time-consuming procedure representing a significant portion of the maintenance cost of a reusable propulsion system. Ball bearing wear has been a recurring life-limiting factor during testing of the Space Shuttle Main Engine and it is believed unlikely their performance will be
battered by an operational system in the near term. Although Urke suggests an expendable system would not require hydrostatic bearings below a design speed of 40,000 rpm, it is likely a pump whose duty cycle reflects that envisioned by the IHPRPT Phase III requirements will need hydrostatic bearings. Scharrer, Tellier, and Hibbs mentioned several applications where this bearing design choice benefits the overall engine performance, specifically in thrust to weight. By increasing pump speed, the overall weight of the pump can be reduced. An additional benefit of the use of hydrostatic bearings is a reduction in parts count with salutary implications for reliability and maintainability.

2.2.3 Hydraulic Design and Throttleability

The initial performance requirements of the LOX pump considered in this work was obtained by performing a cycle power balance at the design point and using the resulting parameters as inputs into the pump sizing routine suggested in Humble, Henry, and Larson; the resulting pump characteristics are shown in Table 6. There is a wealth of historical practices that apply to the problem of designing an inducer/impeller system to accomplish this task and to the design of a turbine required to drive it. Many of these are based on empirical correlations such as the specific speed/ efficiency chart presented in Urke or the blade number envelope presented in NASA SP-8109.

Oyama and Liou identified the exit blade angle, entrance and exit blade numbers, and blade thickness as design parameters having the most impact on successful impeller design. Veres presents a method for predicting the off-design performance of a centrifugal pump. Off-design performance is of great importance for a pump, as most
pumps are required to operate below design flow for a significant fraction of their service lives.

Veres also presents suggestions for ensuring a pump is capable of a wide throttling range; among these are to specify nearly tangential blade angles, the use of vaneless diffusers, and the use of a higher number of impeller blades.³⁴

Based on the need to have a compact, efficient turbopump, a radial inflow turbine design was chosen.³⁵ Other advantages of this approach as compared to an axial turbine include durability, greater manufacturability, and a higher per-stage work output.³⁶

<table>
<thead>
<tr>
<th>Table 6: Preliminary pump characteristics</th>
</tr>
</thead>
<tbody>
<tr>
<td>Shaft Speed</td>
</tr>
<tr>
<td>Rotation/Minute (RPM)</td>
</tr>
<tr>
<td>Head Rise</td>
</tr>
<tr>
<td>Feet (ft.)</td>
</tr>
<tr>
<td>Power Required</td>
</tr>
<tr>
<td>Brake Horsepower (BHP)</td>
</tr>
<tr>
<td>Flow</td>
</tr>
<tr>
<td>Gallons/Minute (GPM)</td>
</tr>
<tr>
<td>Mass Flow</td>
</tr>
<tr>
<td>Pounds Mass/Second (lbm/s)</td>
</tr>
</tbody>
</table>
3 Methodology

This chapter discusses the design methodology used in this work. It begins with the initial power balance and NPSS results, and proceeds to the impeller and turbine design.

3.1 Initial Power Balance

In order to define the performance parameters required of the pump, an initial power balance was performed using equations below presented in Humble, Henry, and Larson. The master power balance equation is:

\[
P_{\text{req}} = \frac{g_0 m H}{\eta_p} = \eta_i m c_p T_i \left[ 1 - \left( \frac{1}{P_{\text{rat}}} \right)^{\gamma-1} \right]
\]  

(1)

Where \( P_{\text{req}} \) represents the required pressure, the quantity to the left of the second equals sign represents the power required by the pump, and the quantity on the right is the power supplied by the turbine; NIST data was used to find the heat capacity and \( \gamma \) at the desired inlet temperature. The turbine expansion ratio, \( P_{\text{rat}} \), is simply the ratio of the inlet to outlet turbine pressures, and the outlet turbine pressure is constrained by the combustion chamber pressure. With the goal \( I_{sp} \) known, this may be found by using equations (2) through (5) below:

\[
I_{sp} = \lambda \left\{ \frac{c^* \gamma}{g_o} \sqrt{\left( \frac{2}{\gamma - 1} \right) \left( \frac{2}{\lambda + 1} \right) \gamma^{\gamma+1}} \left[ 1 - \left( \frac{p_e}{P_c} \right)^{\gamma-1} \right] + \frac{c^* e}{g_o P_c} (P_e - P_a) \right\}
\]

(2)
The exit Mach number ($M_e$) may be determined implicitly from the nozzle expansion ratio (set by the nozzle design) via equation (5). With the combustion chamber pressure set, the mass flow required may be determined from the thrust goal, the target $I_{sp}$ and the relation $I_{sp} = F/W$.\textsuperscript{7} The pump head required may be determined from the sum of the pressure drops through the cooling system, the injector, and the turbine; the last of these may be found if the turbine pressure ratio is known. Thus equation (1) was solved iteratively for the turbine pressure ratio with the seven following assumptions:

1. Oxygen behaves ideally at all operating conditions experienced by the pump
2. the pump has a total efficiency of 85%
3. the turbine has an efficiency of 90%
4. combustion chamber pressure of 1,740 psi (12 MPa) calculated based on goal $I_{sp}$
5. total pressure drop of 20% in the cooling jacket and 300 psi (2.07 Mpa) between the turbine exhaust and combustion chamber (includes injector pressure loss)
6. a thrust requirement of 50,000 lb_f (222 kN)

7. target $I_{sp}$ specified in Phase III IHPRPT goals.

Combined with results from NASA’s Numerical Propulsion Simulation System (NPSS)\textsuperscript{37}, this analysis yielded the design point values for pump and turbine characteristics listed in Table 7. The design process is illustrated in Figure 7.

Figure 7: Design process block diagram
Table 7: Turbopump design point

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Pump inlet pressure, psi (Mpa)</td>
<td>45 (.31)</td>
</tr>
<tr>
<td>Pump output pressure, psi (Mpa)</td>
<td>4500 (31)</td>
</tr>
<tr>
<td>Mass flow, lbm/s (kg/s)</td>
<td>106 (48.1)</td>
</tr>
<tr>
<td>Turbine inlet total pressure, psi</td>
<td>3663 (25.26)</td>
</tr>
<tr>
<td>Turbine total pressure ratio</td>
<td>1.8</td>
</tr>
<tr>
<td>Turbine inlet total temperature, R (K)</td>
<td>600 (333)</td>
</tr>
<tr>
<td>Shaft speed, rpm</td>
<td>32000</td>
</tr>
</tbody>
</table>

### 3.2 Pump Design

To aid in the detailed design of the impeller, the Concepts NERC software package Pumpal\textsuperscript{38} was used. This package uses a mean line (mass averaged one-dimensional analysis along a streamline) code to size and predict the pump performance. This software may be operated in two modes of interest for this work: design (which is used to create impellers and determine performance at the design point) and analysis (which is used to determine off-design characteristics and draw the pump maps shown in chapter 4). Inputs to the program are shown in Table 8 below.

Table 8: Pumpal inputs

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Inlet total pressure, psi (MPa)</td>
<td>45 (0.31)</td>
</tr>
<tr>
<td>Inlet total temperature, °R (K)</td>
<td>150 (83.3)</td>
</tr>
<tr>
<td>Inlet mass flow, lbm/s (kg/s)</td>
<td>106 (48.08)</td>
</tr>
<tr>
<td>Speed, rpm</td>
<td>32000</td>
</tr>
<tr>
<td>Total Dynamic Head, psi (MPa)</td>
<td>4500 (31.03)</td>
</tr>
<tr>
<td>Impeller inlet incidence angle (hub)</td>
<td>2°</td>
</tr>
<tr>
<td>Impeller inlet incidence angle (mean)</td>
<td>2°</td>
</tr>
<tr>
<td>Impeller inlet incidence angle (tip)</td>
<td>2°</td>
</tr>
<tr>
<td>Impeller inlet blade number</td>
<td>7</td>
</tr>
<tr>
<td>Leading edge blade thickness, in (mm)</td>
<td>.0625 (1.588)</td>
</tr>
<tr>
<td>Inclination angle at impeller exit</td>
<td>90°</td>
</tr>
<tr>
<td>Impeller exit blade number</td>
<td>14</td>
</tr>
</tbody>
</table>
The impeller inlet and exit blade numbers were chosen based on the guidance in Oyama and Liou\textsuperscript{32} so as to maximize the total head produced by the pump and minimize power required. The incidence values were chosen to be small in accordance with the guidance in Japikse, Marscher, and Furst\textsuperscript{39} to prevent flow separation and stalling at the inlet and to help ensure a wide throttling range.

### 3.2.1 Impeller Inlet

In order to determine optimum impeller dimensions, Pumpal was run in design mode, which first sets the impeller inlet tip radius (the optimum value of which corresponds to minimum tip relative speed) via the following equation\textsuperscript{40}:

\[
R_{1t} = \left( \frac{30Q\sqrt{2}}{\pi^2 N (1 - (R_{1h}/R_{1t})^2)} \right)^{1/2}
\]

where \( N \) is the pump’s rotational speed, \( Q \) is the volumetric flow rate, \( R_{1h} \) is the inlet hub radius, and \( R_{1t} \) is the inlet tip radius. This equation assumes no inlet swirl, and the inlet hub-to-tip ratio is fixed. In order to determine this, the impeller eye is sized to obtain the minimum Net Positive Suction Head Required (NPSH):

\[
NPSH = \frac{1}{2} \rho C_{1t}^2 (1 + \sigma_b) + \frac{1}{2} \sigma_b U_{1t}^2
\]

where \( \rho \) is the inlet density, \( C_{1t} \) is the absolute flow velocity at the tip inlet, \( U_{1t} \) is the blade tip speed at the inlet, and \( \sigma_b \) is the slip factor, which is assumed constant. By minimizing the NPSH requirement, the designer allows himself a greater range of cavitation-free flow and thus a larger potential operating range for the pump.

Minimum NPSH then occurs when:
\[ R^2_{t_t} = R^2_{t_h} + \left[ \frac{30}{\pi N} \right]^2 \frac{2Q^2}{\pi^2} \frac{1 + \sigma_b}{\sigma_b} \right]^{\frac{1}{3}} \]  

(8)

The blade angle is then set by:

\[ \beta_{t_h} = \beta_{t_t} + I_{t_{t, \text{opt}}} \]  

(9)

\[ \beta_{m_b} = \beta_{m_m} + I_{m_{m, \text{opt}}} \]  

(10)

\[ \beta_{h_h} = \beta_{h_h} + I_{h_{h, \text{opt}}} \]  

(11)

The subscripts t, m, and h correspond to the tip, mean, and hub respectively, \( \beta_h \) is the blade angle, \( \beta \) is the flow angle, and I is the incidence specified in Table 8.

3.2.2 Impeller Outlet

The impeller outlet calculation scheme selected optimizes the impeller outlet radius and impeller exit width. The outlet radius is adjusted to match the desired head rise, while the exit width is based on the value of the exit swirl parameter (defined as the ratio of the tangential to meridional velocities).

3.2.3 Volute

To begin the volute calculation scheme, a loss coefficient \( (LC_{57}) \) is determined, where \( LC_{57} \) is the sum of a meridional \( (LC_m) \) and tangential loss coefficient \( (LC_r) \), total loss of the meridional component of the entering kinetic energy is assumed, and:

\[ LC_m = \frac{1}{1 + \lambda^2} \]  

(12)

\[ LC_r = \left( \frac{r_5}{r_6} \right)^2 \frac{(\lambda - 1/AR)^2}{1 + \lambda^2} \]  

(13)
Here $\lambda$, the inlet swirl parameter, is defined as the ratio of the tangential and meridional velocities at the volute inlet (station 5), $AR$ is the ratio of the volute throat area to the volute inlet area, and $LC_t$ is the average of the inlet and throat radii; if the core flow accelerates ($C_{ts} < C_7$) as happens in the design case, there is no loss in the tangential velocity component and so $LC_t$ becomes zero. After $LC57$ is determined, other properties at the volute throat (station 7) may be determined as follows:

\[ P_{07} = P_{05} - LC57*(P_{05} - P5) \]  
(14)

\[ T_{07} = f(P_{07}, H_{05}) \]  
(15)

\[ s = f(P_{07}, T_{07}) \]  
(16)

Static properties at the volute throat (station 7) are then calculated in an iteration loop using equations (17)-(21):

\[ C_t = \frac{M}{A_t \cdot \rho_t} \]  
(17)

\[ H_t = H_{05} - \frac{C_t^2}{2} \]  
(18)

\[ P_t = f(H_t, s) \]  
(19)

\[ T_t = f(H_t, P_t) \]  
(20)

\[ \rho_t = f(T_t, P_t) \]  
(21)
The pressure recovery coefficient at the volute exit (station 8) is determined by a blockage correlation model, illustrated in Figure 8, which assumes a blockage of 12% at the volute throat. Once this coefficient (CP78) is determined, other properties may be determined in an iterative process as done for station 7:

\[ P_8 = P_7 + CP78 \times (P_{07} - P_7) \]  \hspace{1cm} (22)

\[ H_{08} = H_{07} \]  \hspace{1cm} (23)

Figure 8: Blockage correction for Station 8 pressure recovery\textsuperscript{40}
3.2.4 Analysis Mode

In order to determine off-design performance and draw the pump maps presented in Chapter 4, Pumpal must be run in analysis mode. In this mode, the total pressure and temperature at the impeller inlet are fixed from the upstream conditions and the velocity triangles and static conditions are solved via an iterative process using equations (24) to (29):

\[ P_{01} = \left( P_x + LC1 \cdot P_1 \right) / (1 + LC1) \]  
\[ h_{01} = h(T_x, P_x) \]  
\[ s_1 = s(h_{01}, P_{01}) \]  
\[ C_{m1} = \frac{m}{\rho A_1 (1 - B1)} \]  
\[ C_1 = C_{m1} / \cos(\alpha_1) \]  
\[ h_1 = h_{01} - \frac{1}{2} C_1^2 \]  
\[ \rho_1 = \rho(h_1, s_1) \]

LC1 is the upstream loss coefficient, B1 is the upstream blockage, \( \alpha_1 \) is the inlet flow angle, \( A_1 \) is the impeller inlet area, \( m \) is the mass flow, \( C_1 \) is the impeller inlet absolute velocity, \( C_{m1} \) is the impeller inlet meridional velocity (both at the RMS position), and \( \rho, h, \text{ and } s \) symbolize density, enthalpy, and entropy, respectively, which are calculated based on NIST data.
A two-zone model is used to determine the conditions at the impeller exit. This model divides the outlet flow into two zones (primary and secondary), and employs these basic assumptions:

1. The primary zone flow is assumed to be isentropic; all losses inside the impeller passage occur in the secondary zone.
2. At the impeller exit, the primary zone and secondary zone have the same static pressure.

The first step in this process is to calculate the relative velocity in the primary zone:

\[ W_{2p} = W_{1t} \times DR2 \]  \hspace{1cm} (31)

\( W_{2p} \) is the primary zone relative velocity at the impeller exit, \( W_{1t} \) is the relative inlet velocity at the impeller tip, and \( DR2 \) is the diffusion ratio, defined by:

\[ DR2 = \frac{W_{1t}}{W_{2p}} \]  \hspace{1cm} (31)

The value of \( DR2 \) is determined by a specific speed function, illustrated in Figure 9 (with the specific speed given in the figure in English units) which has been derived from past pumps. With \( W_{2p} \) known, the assumption of rothalpy conservation is applied, as explained below.
If the flow through a thin annular passage bounded by two stream surfaces is analyzed, the torque ($\tau$) acting on the fluid between two meridional locations is given by the conservation of angular momentum\textsuperscript{42}:

$$\tau = m \left( r_2 C_{\theta 2} - r_1 C_{\theta 1} \right) \quad (32A)$$

With $r$ being the radius at each station, and $C_{\theta}$ being the absolute tangential flow velocity. The power imparted to the fluid is then the product of this torque and the angular velocity $\Omega$\textsuperscript{41}:

$$\tau \ \Omega = m \left( U_2 C_{\theta 2} - U_1 C_{\theta 1} \right) \quad (32B)$$

The work done on the fluid per unit mass (specific work) is the power divided by the mass flow rate, or $U_2 C_{\theta 2} - U_1 C_{\theta 1}$.

Since the specific work done on the fluid is equal to the change in total enthalpy for steady, adiabatic, and irreversible flow,

$$h_{02} - h_{01} = U_2 C_{\theta 2} - U_1 C_{\theta 1} \quad (32C)$$

With total enthalpy defined as $h_0 = h + 0.5C_1^2$ equation (32C) may be rearranged to give\textsuperscript{41}:

$$h_1 + 0.5C_1^2 - U_1 C_{\theta 1} = h_2 + 0.5C_2^2 - U_2 C_{\theta 2} = I$$

Where $I$ is defined as the rothalpy (rotational stagnation enthalpy), a quantity that is unchanged between impeller entrance and exit.

Applied here, the assumption of constant rothalpy gives:

$$h_{2,p} + \frac{W_{2,p}^2}{2} = \frac{U_2^2}{2} = h_1 + \frac{W_{1}^2}{2} = \frac{U_1^2}{2} \quad (33)$$

This may be rearranged to find the static enthalpy:
\[
h_{2p} = \left( h_1 + \frac{W_1^2}{2} - \frac{U_1^2}{2} \right) - \frac{W_{2p}^2}{2} + \frac{U_{2p}^2}{2}
\]  \hspace{1cm} (34)

Since the flow in the primary zone is assumed to be isentropic,

\[
s_{2p} = s_i
\]  \hspace{1cm} (35)

With \( s_{2p} \) and \( h_{2p} \) known, other thermodynamic properties such as \( P_{2p} \), \( T_{2p} \), and \( \rho_{2p} \) may be determined. The primary flow angle \( (\beta_{2p}) \) may then be found from the impeller exit blade angle \( (\beta_{2b}) \) and the deviation angle \( (\delta_{2s}) \) from equation (36):

\[
\beta_{2p} = \beta_{2b} + \delta_{2s}
\]  \hspace{1cm} (36)

Figure 9: Diffusion Ratio/Specific Speed Function used by Pumpal\(^{40}\)
The velocity triangle is completely defined with $\beta_{p}$ and $W_{2p}$. After the primary zone has been completely defined, the mass fraction in the primary zone may be calculated:

$$1 - \chi = \frac{\rho_{2p} (1 - \varepsilon) A_{2} W_{2p} \cos(\beta_{2p})}{m}$$  \hspace{1cm} (37)

where the secondary flow mass fraction ($\chi$, which is determined by the program as a function of specific speed) is defined as:

$$\chi = \frac{m_s}{m_{tot}}$$  \hspace{1cm} (38)

where the subscripts s and tot refer to the secondary and total flows, respectively, and the secondary area fraction ($\varepsilon$) is defined as:

$$\varepsilon = \frac{A_{2s}}{A_{2}}$$  \hspace{1cm} (39)

The secondary area fraction may be found from:

$$\varepsilon = 1 - \frac{(1 - \chi) m}{\rho_{2p} A_{2} W_{2p} \cos(\beta_{2p})}$$  \hspace{1cm} (40)

Also, since

$$\chi = \frac{\rho_{2s} (\varepsilon A_{2}) W_{2s} \cos(\beta_{2s})}{m}$$  \hspace{1cm} (41)

the secondary zone relative velocity ($W_{2s}$) may be found from:
\[
W_{2s} = \frac{\dot{m}}{\epsilon \rho_{2s} A_2 \cos(\beta_{2s})}
\] (42)

With \( W_{2s} \) known, conservation of rothalpy\(^{41} \) may be applied in a similar fashion to the primary zone in order to determine the static enthalpy of the secondary zone:

\[
h_{2s} = (h_2 + \frac{W_{1s}^2}{2} - \frac{U_{1s}^2}{2}) - \frac{W_{2s}^2}{2} + \frac{U_{2s}^2}{2}
\] (43)

With the secondary zone static pressure known from assumption 2 above (equal static pressures in both zones), all the thermodynamic properties may be determined.

The secondary flow angle may then be determined from the impeller exit blade angle and the secondary deviation angle (\( \delta_{2s} \)):

\[
\beta_{2s} = \beta_{2b} + \delta_{2s}
\] (44)

With \( W_{2s} \) and \( \beta_{2s} \) known, the velocity triangle for the secondary zone is fully defined. The primary and secondary zones are assumed to mix instantly and uniformly at the impeller exit. The mass and momentum conservation equations that apply to this situation are as follows:

\[
\rho_{2m} \rho_{2m} A = \rho_{2p} C_{M2p} (1 - \epsilon) A + \rho_{2s} C_{M2s} \epsilon A
\] (45)

\[
(P_{2p} - P_{2m}) A = \rho_{2m} C_{2m}^2 A - \{\rho_{2p} C_{M2p}^2 (1 - \epsilon) A + \rho_{2s} C_{M2s} \epsilon A\}
\] (46)

\[
C_{12m} = \chi C_{12s} + (1 - \chi) C_{12p}
\] (47)

The subscript \( m \) signifies mixed out conditions. The specific total enthalpy after mixing, \( h_{02m} \), after accounting for power losses from front and rear leakage (\( P_{\text{fleak}} \) and \( P_{\text{rleak}} \), respectively) disk friction (\( P_{\text{df}} \)), and recirculation(\( P_{\text{recirc}} \)) is:

(32)
\[ h_{o2m} = h_{o2a} + \frac{P_{\text{leak}} + P_{\text{ric}} + P_{\text{df}} + P_{\text{recirc}}}{m} \]  

(48)

With the fluid’s equation of state fixed (this case uses NIST\textsuperscript{43} data for Oxygen), equations (45) through (48) may be solved iteratively to determine the conditions after mixing.

3.3 Turbine Design

The Concepts NERC software Rital\textsuperscript{44} was used to design the turbine. This software uses a meanline code to predict turbine performance. Initial inputs to the program are shown below:

Table 9: Initial turbine design inputs

<p>| | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Inlet total pressure, psi (MPa)</td>
<td>3663 (25.26)</td>
</tr>
<tr>
<td>Outlet total pressure, psi (MPa)</td>
<td>2035 (14.03)</td>
</tr>
<tr>
<td>Inlet total temperature, R (K)</td>
<td>520 (288.9)</td>
</tr>
<tr>
<td>Shaft speed, rpm</td>
<td>32000</td>
</tr>
<tr>
<td>Mass flow, lbm/s (kg/s)</td>
<td>95 (43.09)</td>
</tr>
<tr>
<td>Optimum incidence, degrees</td>
<td>-35</td>
</tr>
<tr>
<td>Power required, hp (kW)</td>
<td>2215 (1651.7)</td>
</tr>
</tbody>
</table>

The optimum incidence angle was chosen based on the range suggested by Moustapha, et al.\textsuperscript{45} and the guidance given by Rohlik\textsuperscript{35} based on the need to prevent flow separation in the blade passage and past design experience and experimental results. Other inputs were derived from the power balance and Pumpal design.

3.3.1 Preliminary Sizing

In order to determine initial parameters for the turbine, Rital was run in preliminary design mode, which requires the user to specify three of the following conditions: inlet total pressure, exit static pressure, mass flow rate, and power. Since the
power requirement, inlet total pressure, and mass flow were determined in the power
balance and fluid-end design, these properties were chosen.

The preliminary sizing algorithm\textsuperscript{46} uses a specified optimum flow coefficient \((\phi, \text{ defined in equation (49) below})\) and loading coefficient \((\psi, \text{ defined in equation (50) below})\):

\[ \phi = \frac{C_{M6}}{U_4} \] \hspace{2cm} (49)

\[ \psi = \frac{\Delta h_0}{U_4^2} \] \hspace{2cm} (50)

where \(C_{M6}\) is the rotor exit meridional velocity, \(U_4\) is the rotor tip speed, and \(\Delta h_0\) is the actual specific enthalpy change. The value of \(\phi\) was chosen to be 0.25 for maximum efficiency as suggested by the program and echoed by Mathis\textsuperscript{47} based on past design experience. The loading coefficient was chosen to be 0.9, as suggested by the program based on past results\textsuperscript{46}. After the rotor inlet radius is found, RITAL proceeds to calculate the rest of the nozzle and rotor geometry as follows.

The velocity triangle at the rotor outlet is found by assuming a rotor meridional velocity ratio, \(\xi\), of unity and zero exit swirl; along with a specified incidence, this sets the rotor inlet angle. Continuity considerations then determine the blade inlet width.

The selected \(\phi\) may be used along with the assumption of zero exit swirl to determine the rotor exit area and thus the exit tip radius; the ratio of rotor exit hub radius to rotor inlet radius is set to 0.3. The exit blade angle is calculated with an assumed deviation angle, \(\delta_e\), of 5 degrees. The axial length (AxLen) is found from the relations below:
Intermediate values are found by linear interpolation. The blade thickness is set as two percent of the tip radius, while inlet and outlet clearances are set at one percent of the inlet blade height.

The nozzle exit to rotor inlet radius is fixed at 1.05; the velocity triangle is determined from conservation of mass and angular momentum from rotor inlet. The blade angle is then found assuming a two degree deviation angle. The nozzle inlet ratio is then set as 1.25 times the nozzle exit ratio. The nozzle exit blade angle is either set to zero or calculated assuming a straight blade, depending on the deviation model selected; in this case a straight blade was assumed. Results of this step are listed in Table 11 in Chapter 4.

3.3.2 Final Design

After completion of preliminary sizing, RITAL was run in a design mode that required the user to input the exit total pressure (known in this case from the initial power balance) and returned the nozzle exit blade angle. This mode was used to create the final design and to set such parameters as the number of nozzle and rotor blades, axial and radial clearances, and rotor exit hub-to-tip ratio.

The number of nozzle blades selected was based on a relation given by Mathis:

$$Z = \frac{(b/s)2\pi r_m t_e / \cos(\alpha_e) \delta_b}{\delta_b}$$  \hspace{1cm} (53)
where \((b/s)\) is the blockage ratio, \(r_m\) is the mean radius, \(t_e\) is the trailing edge thickness, and \(\alpha_e\) is the flow angle.

To determine the number of rotor blades, a relation presented by Rohlik\(^{35}\) to determine the minimum number of blades necessary to prevent flow separation was used:

\[
    n = 0.03(\alpha_i - 57)^2 + 12
\]

where \(n\) is the minimum number of rotor blades and \(\alpha_i\) is the nozzle exit flow angle in degrees as determined in the previous step.

The axial clearance was chosen to be one percent of the inlet blade height (due to manufacturability concerns) and the radial clearance was chosen to be one half of one percent of the exit blade height to maximize total efficiency in light of the results presented by Futral and Holeski\(^{48}\) who found that the deleterious effect of increasing radial clearance on total efficiency was ten times greater than an equal percentage increase in axial clearance. In accordance with the guidance in Mathis\(^{47}\) the rotor exit hub-to-tip ratio was chosen to be about 0.33 to enable the use of a smaller and less expensive rotor.

Nozzle losses were modeled by a user-specified loss coefficient that is used to calculate the difference between actual and ideal static enthalpy at the trailing edge of the nozzle. Based on guidance presented in the program and by Dixon\(^{41}\) for well designed nozzle rows in normal operation, this was chosen as 0.04.

The deviation in the nozzle, \(\delta\), was modeled using a modification to the Howell correlation proposed by Jansen\(^{49}\)
\[
\delta = \alpha_3 - \alpha_{b3} = a_3(\alpha_{b3} - \alpha_{b1}) \frac{\pi(r_i + r_s)}{Z_N \cdot C} \tag{55}
\]

where \(a_3\) is a constant, chosen as 0.13, \(\alpha_3\) is the nozzle exit flow angle, \(\alpha_{b3}\) is the nozzle exit blade angle, \(\alpha_{b1}\) is the nozzle inlet blade angle, \(r_i\) and \(r_s\) are the nozzle inlet and outlet radii, respectively, \(Z_N\) is the number of nozzle blades, and \(C\) is the blade cord.

There are four types of rotor losses modeled by the program: clearance, incidence, trailing edge, and passage losses. These are detailed below.

Passage losses in the rotor are modeled using a NASA loss model that calculates the passage loss as a fraction of the mean passage kinetic energy:

\[
L_p = \frac{1}{2} K_p (W_4^2 \cos^2 i + W_5^2) \tag{56}
\]

where \(i\) is the angle between the incoming flow and that at the best efficiency point, \(L_p\) is the passage loss, \(W_4\) is the relative velocity at the rotor entrance, \(W_5\) is the relative velocity at the rotor exit and \(K_p\) is an empirical coefficient whose value is set at 0.3.

Incidence losses (\(L_i\)) are modeled as the loss of tangential kinetic energy as the flow turns from the inlet flow angle to the angle at the best efficiency point:

\[
L_i = \frac{1}{2} W_4^2 \sin^2 i \tag{57}
\]

Clearance losses (\(L_c\)) are assumed to be a function of the clearance/blade height ratio:

\[
L_c = K_c \left( \frac{\varepsilon_r}{b_3} \right) \tag{58}
\]

Here \(\varepsilon_r\) is the exit clearance and \(b_3\) is the outlet blade height.
4 Results

This chapter presents and discusses the results of the DEAN Oxygen pump design study. Concepts NERC’s Pumpal$^{38}$ and Rital$^{44}$ programs were used to model the pump and turbine, respectively. This pump was designed to enable the DEAN to achieve IHPRPT Phase III performance and logistics goals and was required to deliver 106 lb/s (48.08 kg/s) LOX at a pressure of 4,500 psi (31.03 MPa) based on the power balance. Inputs to Pumpal and Rital are listed in Appendix A.

4.1 Pump Results

The final pump design and performance parameters are listed in Table 10; angles listed are measured using the meridional convention. This pump will deliver 106 lbm/s (48.08 kg/s) LOX at a total pressure of slightly over 4600 psi (31.7 MPa) while demanding a power input of 2215 hp (1651 kW). Figure 10 is an illustration of the final impeller.

<table>
<thead>
<tr>
<th>Table 10: Pump design and performance parameters</th>
</tr>
</thead>
<tbody>
<tr>
<td>Total Inlet Pressure, psi (MPa)</td>
</tr>
<tr>
<td>Total Inlet Temperature, R (K)</td>
</tr>
<tr>
<td>Mass Flow, lbm/s (kg/s)</td>
</tr>
<tr>
<td>Volumetric Flow rate, ft$^3$/s (m$^3$/s)</td>
</tr>
<tr>
<td>Rotational Speed, RPM</td>
</tr>
<tr>
<td>Inlet Blade Number</td>
</tr>
<tr>
<td>Outlet Blade Number</td>
</tr>
<tr>
<td>Inlet Blade Angle, mean, degrees</td>
</tr>
<tr>
<td>Outlet Blade Angle, degrees</td>
</tr>
<tr>
<td>Total Exit pressure, psi (MPa)</td>
</tr>
<tr>
<td>Total Head Rise, ft (m)</td>
</tr>
<tr>
<td>$\eta_{t-r}$, %</td>
</tr>
<tr>
<td>Net Positive Suction Head, ft (m)</td>
</tr>
<tr>
<td>Non-dimensional Specific Speed</td>
</tr>
</tbody>
</table>
The final design speed was chosen as a compromise between the desire to have a smaller pump (which would argue for a faster rotational speed) and the necessity to avoid excessive friction heating in the pump or turbine that could lead to catastrophic pump failure (which would dictate a lower speed). As pointed out by Campbell and Farquhar\textsuperscript{19} other limits on shaft speed which should be considered include allowable stresses, gear and seal velocities, and optimum specific speed. The speed chosen (32,000 rpm) is in the range of current state of the art LOX pumps and should be attainable.\textsuperscript{6,13,15}

Figure 11 is the pump head/flow curve. Based on the guidance in NASA SP-8107\textsuperscript{11} that a pump-engine system becomes unstable when the slope of the head/flow lines are positive, this pump will be capable of throttling down 32 per cent from its maximum flow at design speed. Its total throttling range (down to half the design speed)
will be 66%. The true lower boundary will depend on pressure losses in the cooling jacket which will decrease as the volumetric flow and thus flow velocity decrease. Figure 13 shows the pump’s head/flow behavior and the surge line, which is found by connecting points of zero slope on each of the constant speed lines. The stable operating range is to the right of this line. Given that the pump exit total pressure must be greater than 2,600 psi (17.9 MPa) due to combustion chamber pressure requirements (assuming a
constant pressure loss in the cooling jacket of 20 per cent at all flow conditions), the
lowest speed line in Figure 13 likely represents a pressure rise that is of no use to the
engine. The lowest useful flow likely obtainable is then 59 lbm/s (26.8kg/s), or 52% of
the maximum flow at design speed.

Figure 14 shows the pump’s Net Positive Suction Head (NPSH) requirements as a
function of flow rate. As expected, these requirements increase as the flow increases. The
NPSH available may be calculated by the relation:

\[ NPSH = H_{static} + \frac{C_m^2}{2g} - H_{vap} \]  

(59)

where \( H_{static} \) is the static head, \( C_m \) is the impeller inlet absolute velocity, and \( H_{vap} \) is the
head due to vapor pressure. Calculating this quantity using the method suggested by
Perry, Green, and Maloney gives an available NPSH of 134 ft (40.8 m) at the design
point, against a requirement of 67 ft (20.4 m) as shown by the circled point in Figure 13.
Figure 12: Pump power curve
Figure 13: Pump map with surge line
The final turbine design and performance parameters are listed in Table 11. This turbine will supply approximately 10 per cent more power than the pump currently requires; the rotor is illustrated in Figure 15. The specific speed at the design point is very close to the 0.43 suggested by Kofsky and Nusbaum\textsuperscript{51} for optimum static efficiency and within the range suggested by them for maximum total efficiency.

Figure 14: NPSH curve

4.2 Turbine Results

The final turbine design and performance parameters are listed in Table 11. This turbine will supply approximately 10 per cent more power than the pump currently requires; the rotor is illustrated in Figure 15. The specific speed at the design point is very close to the 0.43 suggested by Kofsky and Nusbaum\textsuperscript{51} for optimum static efficiency and within the range suggested by them for maximum total efficiency.
The turbine’s efficiency/velocity ratio curve is shown in Figure 16. The overall trend mirrors that presented by Kofskey and Holeski\textsuperscript{52} for a slightly (~7%) larger turbine and is similar to that seen by Kofskey and Wasserbauer\textsuperscript{53} for a turbine approximately half as large. The peak total efficiency occurs at a slightly higher value of velocity ratio than that corresponding to the design point, although the difference is slight (roughly one-half of one percent).

Figure 17 shows the corrected mass flow (defined as $\frac{\dot{m}\sqrt{T_e}}{P_0}$) as a function of expansion ratio. The curves seen are typical of subsonic turbines, with mass flow increasing as pressure ratio increases for all speeds; the turbine does not experience choked flow. This indicates that the turbine is not a limiting factor for throttleability.

Figure 18 shows the variation of total efficiency with specific speed; the optimum specific speed for this turbine is 0.465, near that of Kofskey and Nusbaum.\textsuperscript{51}

<table>
<thead>
<tr>
<th>Table 11: Turbine design and performance parameters</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Total-to-total Pressure ratio</strong></td>
</tr>
<tr>
<td><strong>Total-to-static Pressure ratio</strong></td>
</tr>
<tr>
<td><strong>Inlet Total Temperature, R (K)</strong></td>
</tr>
<tr>
<td><strong>Inlet Total Pressure, psi (MPa)</strong></td>
</tr>
<tr>
<td><strong>Mass Flow rate, lbm/s (Kg/s)</strong></td>
</tr>
<tr>
<td><strong>Rotational Speed, RPM</strong></td>
</tr>
<tr>
<td><strong>Nozzle Blades</strong></td>
</tr>
<tr>
<td><strong>Rotor Blades</strong></td>
</tr>
<tr>
<td><strong>Rotor Hub-to-tip Ratio</strong></td>
</tr>
<tr>
<td><strong>Rotor Exit Blade Angle, degrees</strong></td>
</tr>
<tr>
<td><strong>Velocity Ratio, U/C0</strong></td>
</tr>
<tr>
<td>$\eta_{t-to}$, %</td>
</tr>
<tr>
<td>$\eta_{t-st}$, %</td>
</tr>
<tr>
<td><strong>Non-dimensional Specific Speed</strong></td>
</tr>
<tr>
<td><strong>Power, hp (kW)</strong></td>
</tr>
</tbody>
</table>
Figure 15: Turbine rotor
Figure 16: Variation of total efficiency with velocity ratio
Figure 17: Variation of corrected mass flow with expansion ratio
4.3 Sensitivity Analysis

In order to determine the most promising areas for future improvement, a sensitivity analysis was done for both the pump and turbine using power as the quantity to be optimized (minimum power requirement for the pump and maximum power output for the turbine); the results of this process are shown in Table 12.
Table 12: Sensitivity Analysis

<table>
<thead>
<tr>
<th>TURBINE</th>
<th>Mass flow,lbm/s (Kg/s)</th>
<th>Inlet Temperature, R (K)</th>
<th>Inlet Pressure, psi (Mpa)</th>
<th>Nozzle blade #</th>
<th>Rotor Blade #</th>
<th>Rotor blade angle,Degrees</th>
<th>Power, HP (kW)</th>
<th>(deltaHP)/(deltaQ/Q)</th>
</tr>
</thead>
<tbody>
<tr>
<td>95 (43.1)</td>
<td>600 (333)</td>
<td>3663 (25.26)</td>
<td>15</td>
<td>22</td>
<td>-60</td>
<td>2441 (1820)</td>
<td>NA</td>
<td></td>
</tr>
<tr>
<td>90 (40.8)</td>
<td>600 (333)</td>
<td>3664 (25.26)</td>
<td>15</td>
<td>22</td>
<td>-60</td>
<td>2313 (1725)</td>
<td>-2432.0</td>
<td></td>
</tr>
<tr>
<td>95 (43.1)</td>
<td>568 (315.6)</td>
<td>3665 (25.26)</td>
<td>15</td>
<td>22</td>
<td>-60</td>
<td>2268 (1691)</td>
<td>-3287.0</td>
<td></td>
</tr>
<tr>
<td>95 (43.1)</td>
<td>600 (333)</td>
<td>3470 (23.92)</td>
<td>15</td>
<td>22</td>
<td>-60</td>
<td>2246 (1675)</td>
<td>-3705.0</td>
<td></td>
</tr>
<tr>
<td>95 (43.1)</td>
<td>600 (333)</td>
<td>3663 (25.26)</td>
<td>14</td>
<td>22</td>
<td>-60</td>
<td>2437 (1817)</td>
<td>-60.0</td>
<td></td>
</tr>
<tr>
<td>95 (43.1)</td>
<td>600 (333)</td>
<td>3663 (25.26)</td>
<td>15</td>
<td>23</td>
<td>-60</td>
<td>2434 (1815)</td>
<td>-154.0</td>
<td></td>
</tr>
<tr>
<td>95 (43.1)</td>
<td>600 (333)</td>
<td>3663 (25.26)</td>
<td>15</td>
<td>22</td>
<td>-56.84</td>
<td>2431 (1813)</td>
<td>-190.0</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>PUMP</th>
<th>Main Blades</th>
<th>Total Blades</th>
<th>Blade Angle</th>
<th>Blade Thickness</th>
<th>RPM</th>
<th>Volute exit diameter ratio</th>
<th>Power, HP (kW)</th>
<th>(deltaHP)/(deltaQ/Q)</th>
</tr>
</thead>
<tbody>
<tr>
<td>7</td>
<td>14</td>
<td>-59.98</td>
<td>0.1</td>
<td>32000</td>
<td>2</td>
<td></td>
<td>2215 (1652)</td>
<td>NA</td>
</tr>
<tr>
<td>6</td>
<td>12</td>
<td>-59.98</td>
<td>0.1</td>
<td>32000</td>
<td>2</td>
<td></td>
<td>2225.451 (1660)</td>
<td>73.2</td>
</tr>
<tr>
<td>7</td>
<td>7</td>
<td>-59.98</td>
<td>0.1</td>
<td>32000</td>
<td>2</td>
<td></td>
<td>2249.402 (1677)</td>
<td>68.8</td>
</tr>
<tr>
<td>7</td>
<td>14</td>
<td>-56.82</td>
<td>0.1</td>
<td>32000</td>
<td>2</td>
<td></td>
<td>2254 (1681)</td>
<td>741.0</td>
</tr>
<tr>
<td>7</td>
<td>14</td>
<td>-59.98</td>
<td>0.095</td>
<td>32000</td>
<td>2</td>
<td></td>
<td>2219 (1655)</td>
<td>-494.0</td>
</tr>
<tr>
<td>7</td>
<td>14</td>
<td>-59.98</td>
<td>0.1</td>
<td>30316</td>
<td>2</td>
<td></td>
<td>2189 (1632)</td>
<td>-692.6</td>
</tr>
</tbody>
</table>

For the turbine, the three factors with the most impact on power delivered are inlet mass flow, inlet temperature and inlet pressure. Changing these parameters by roughly five percent lead to a power loss of 5.2, 7.1, and 8.0 percent, respectively.
All three of these quantities depend heavily on attributes of the rest of the engine (e.g., chamber combustion temperature, chamber length, materials of construction) and especially in the case of inlet pressure, on assumed performance characteristics (in this case, the pressure drop to be expected in the cooling jacket).

None of the factors evaluated on the pump side had as much impact on power requirement as the top three turbine factors. Pump power requirements were most affected by blade angle, blade thickness, and rotational speed. Among these parameters, rotational speed had the greatest impact. This parameter, in turn, is dependant on the turbine: in the absence of a gear box, both must rotate at the same speed.

Slowing the speed of the pump will necessitate a lower specific speed for the turbine and thus represents potential impact on turbine efficiency. While the speed in the Table 13 corresponds to a turbine specific speed of 0.415, still within the range suggested by Kofskey and Nusbaum\textsuperscript{51} for maximum total efficiency, this parameter must be varied with care to avoid a deleterious impact on the turbine. Additionally, as pointed out in NASA SP-8107\textsuperscript{11}, throttling range usually increases with increasing specific speed for sweptback impellers with constant discharge blade angles due to the decrease in head coefficient with increasing specific speed. Therefore, a reduced pump speed is expected to result in a reduced throttling range.

### 4.4 Shaft and Bearings

The shaft diameter was determined based on stress criteria rather than stiffness (critical speed) criteria as is usual\textsuperscript{54} since the rotodynamic analysis necessary to determine the latter quantity is outside the scope of this effort. From a stress perspective,
minimum required shaft diameter may be found by considering the power supplied by the
turbine using the relations\(^55\):

\[
\tau = \frac{P}{2\pi f}
\]

\[
J = \frac{\tau}{c \sigma_{allowable}}
\]

\[
\sigma_{allowable} = \frac{\sigma_y}{\delta}
\]

J is the polar moment of inertia, f is frequency (in Hz), c is the shaft radius, P is the
turbine’s power output, \(\sigma_y\) is the yield stress (found to be 168 ksi for Inconel 718\(^56\)),
\(\sigma_{allowable}\) is the allowable stress, \(\delta\) is a safety factor (chosen to be 1.2 in accordance with
the safety factor chosen for the RL-10\(^54\)) and \(\tau\) is the shaft torque. The shaft must thus
be at least 0.26 in (6.604mm) in diameter; this would correspond to a DN number of
about 211,000. Based on the relatively low DN number and the need to meet IHPRPT’s
reliability and maintainability goals, a ceramic hybrid ball/hydrostatic bearing is the best
choice for this application; these have been tested up to a DN number of 3 million\(^57\). The
primary motivation for selecting these bearings is to take advantage of the long service
life of hydrostatic bearings\(^26\) while using ball bearings to accommodate the transient
loads occurring at start-up and shut down. Ceramic balls are preferred due to their
increased resistance to liquid oxygen relative to steel.

The maximum shaft length, which is calculated based on the maximum allowable
deflection, is calculated from the relation given by Karassik, et al.\(^58\):

\[
f = \frac{wI^3}{CEI}
\]
where $f$ is the shaft deflection (a maximum allowable value of 0.006 in (0.152 mm) was chosen), $w$ is the weight of the rotating elements, $C$ is a coefficient which depends on load distribution and shaft support method (set to one for purposes of this calculation), $E$ is the modulus of elasticity, and $I$ is the moment of inertia. For an Inconel 718 shaft, the maximum length is 3.4 in. The expected axial loads and fatigue limits calculated by the Concepts NERC software AxCENT\textsuperscript{59} for Inconel-718 are shown in Table 14 and suggested bearing locations are shown in Figure 18. A representation of the final integrated rotor is found in Figure 19.

Table 13: Axial loads and fatigue limits

<table>
<thead>
<tr>
<th>Net Force on Pump Impeller, lbf (N)</th>
<th>195.8 (871)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Net Force on Turbine Rotor, lbf (N)</td>
<td>-237.9 (1058)</td>
</tr>
<tr>
<td>Turbine Bore Stress level, ksi (MPa)</td>
<td>40.15 (276.8)</td>
</tr>
<tr>
<td>Pump Bore Stress level, ksi (MPa)</td>
<td>36.11 (249.0)</td>
</tr>
<tr>
<td>Turbine High Cycle Fatigue Margin at Design Speed, ksi (MPa)</td>
<td>57.88 (399.0)</td>
</tr>
<tr>
<td>Pump High Cycle Fatigue Margin at Design Speed, ksi (MPa)</td>
<td>69.82 (481.4)</td>
</tr>
<tr>
<td>Low Cycle Fatigue Limit at Design Speed</td>
<td>&gt; $10^6$ cycles</td>
</tr>
</tbody>
</table>

Figure 19: Bearing arrangement
Figure 20: Final integrated rotor
5 Conclusions and Recommendations

This research effort was undertaken to examine the design of an oxygen pump to support a dual-expander engine concept (the DEAN) intended to meet the Phase III goals of the IHPRPT program. The main thrust of this program is to ensure reliable access to space and make space launch more efficient from both a monetary and time perspective. This effort used software that employs industry standard techniques and practices that satisfy governing equations and physics to model and predict pump and turbine performance. 38,44,59

5.1 Conclusions

A LOX pump powered by warm gaseous oxygen is a plausible candidate for use in a dual expander cycle upper stage engine that will meet the performance, reliability, maintainability, and service life goals of IHPRPT Phase III.

Inconel 718 is the recommended material of construction for both the pump and the turbine due to its record of satisfactory service in oxygen and favorable mechanical properties, including its good ductility at cryogenic temperatures and high yield strength. Monel K-500, while exhibiting good oxygen resistance, does not possess the strength of Inconel 718. The expected turbine inlet temperature (600 R) is 55 percent of the ignition temperature of Inconel 600 demonstrated in Schoenman’s friction rubbing test. 24 Additionally, Schoenman found that Monel, 400, 316 Stainless Steel, and Nickel 200 became more difficult to ignite and burn at oxygen pressures above 1000 psi (6.89 MPa) 23; if this trend holds for Inconel then the difference in oxygen resistance may be insignificant at the pressures expected in the turbine. While Inconel 600 and Inconel
718 would be expected to behave similarly (based on their similar composition), a further test would be prudent.

The factors most affecting the turbine’s power output are inlet temperature, inlet total pressure, and mass flow rate. These quantities are highly dependant on engine characteristics outside the pump designer’s purview. Therefore, this system will be heavily influenced by engine design choices affecting chamber cooling.

The pump’s power requirements are most affected by blade angle, blade thickness, and rotational speed, with the last having the most impact and being directly dependant on the turbine. While the pump appears to have ample NPSH, the addition of a small boost pump such as that used by Buckmann, et al.\textsuperscript{10} or an axial inducer ahead of the impeller (such as those investigated by Kamijo et al.\textsuperscript{60}, Shimagaki, et al.\textsuperscript{61}, and Bramanti, Cervone, and d’Agostino\textsuperscript{62}) is advisable.

The pump is capable of throttling down to 52 per cent of its maximum flow at design speed. While it may successfully operate at lower flow rates, it is likely the head rise at these lower flow rates will be insufficient to meet the engine’s demands.

This study examined the design of an oxygen pump intended for use with a dual expander engine concept. This pump must be capable of supporting Phase III IHPRPT goals of maintainability, reliability, and supportability in addition to providing the flow and head rise demanded by the DEAN engine concept. The pump presented will provide ample flow at an appropriate pressure at the design point and will be capable of a wide throttling range. The turbine presented supplies adequate power over a wide range of desired flow rates. Its output is highly dependant on other engine characteristics, particularly the combustion chamber. The hydrostatic liftoff bearing will maximize the

56
likelihood of achieving the reliability, maintainability, and service life goals of the IHPRPT program.

5.2 Recommendations for Future Research

First, as this study focused on the hydrodynamic design of the pump and turbine, a rotodynamic analysis of the turbopump is in order.

Also, this study used a constant turbine nozzle loss coefficient based on a relation given by Dixon\(^41\) for well-designed nozzle rows in normal operation and software package guidance\(^44\); a nozzle designed for this application with calculated losses would give more reliable results.

The turbine uses all full blades with no splitters. While Rohlik\(^63\) suggests only a modest improvement is possible by replacing half the blades with splitters, it should be investigated.

Furthermore, while the turbine is operating in a favorable specific speed for attainment of high efficiency, the same may not be true of the pump. A trade study may find another rotational speed that achieves higher pump efficiency and perhaps a deeper throttling range while having a minimal effect on the turbine\(^11\).

Finally, a water/air flow test on a model of the pump and turbine would help to define performance and validate the design methods and loss models used. Conversely, it may show the need to use alternative loss models.
Appendix A

RITAL Inputs

Inlet Conditions

Total Temperature    600R
Total Pressure     3663psi
Mass Flow     95.0 lbm/s
Rotational Speed    32000 rpm

Nozzle Geometry

Inlet tip radius     3.40836 in
Inlet hub radius    3.40836 in
Inlet blade height    0.243 in
Exit tip radius     2.9 in
Exit hub radius    3.40836 in
Exit blade height    0.243044 in
Number of blades    15
Blade TE normal thickness  .035446 in
Vane Cord Length    0.5
Throat area multiplier    1.0
Nozzle Properties

Inlet blockage 0.02
Loss coefficient 0.0395
Trailing edge loss multiplier 0.2
Fraction of loss upstream of throat 0.3
Throat aerodynamic blockage 0.05

Nozzle Options

Loss model User Specified Loss Coefficient
Deviation model Modified Howell Correlation
Constants \( a_3 = 0.13 \)

Interspace

Swirl coefficient 1.0
Inlet blockage 0.01
Loss coefficient 0.001

Rotor Geometry

Inlet: Exit
Tip radius 2.8 in 2.3 in
Hub radius 2.8 in 0.75 in
Blade height 0.35 in
Blade angle 0.0 degrees -60 degrees
Blade TE normal thickness 0.03 in
Rotor throat area multiplier  1.0
Number of blades  22
Suction Surface blade thickness at throat  0.05 in
Axial clearance  0.0035 in
Radial clearance  0.007724 in
Back face clearance  0.0035 in

Rotor Properties
Optimum incidence  -35.0 degrees
Inlet blockage  0.1
Rotor throat aerodynamic blockage  0.05
Rotor exit deviation  3.0 degrees
Trailing edge loss multiplier  1.0
Fraction of loss upstream of throat  0.6
Rotor loss model  NASA passage loss

Rotor Loss Coefficient Multipliers
Incidence  1.0
Passage  0.1
Axial clearance  0.4
Radial clearance  0.75
Exit Conditions

Blockage 0.0
Exit total pressure 2035

PUMPAL Inputs

Upstream Conditions

Stagnation temperature 150 R
Stagnation pressure 45 psi
Rotational Speed 32000 rpm

Impeller Inlet-Geometry

Dimensions Variable
Hub radius 0.760267
Setback angle 36.9 degrees
Number of main blades 7
Leading edge thickness .0625
Incidence (Tip, hub, and RMS) 2 degrees

Impeller Inlet-Properties

Blockage 0.083337
Velocity Ratio 1.05
LC1 0.01
Flow angle correction 0.0
**Impeller Inlet-Options**

Inlet incidence (hub, mean, and tip)  
Inducer optimization  
LC1  
Swirl Option

**Impeller Exit-Geometry**

Rotor Design Option  
PHI2  
BEATA2B, Mean  
Number of exit blades  
Blade thickness  
Bexp ratio

**Impeller Exit-Properties**

Msec/M  
DELTAs  
DELp option  
LAM2  
DF multiplier  
Design Target  
Pressure Rise Multiplier (safety factor)  
ETAa:  
ETAb
### Impeller Exit-Options

<table>
<thead>
<tr>
<th>Option</th>
<th>Setting</th>
</tr>
</thead>
<tbody>
<tr>
<td>Impeller tip model</td>
<td>Two-zone: Frozen</td>
</tr>
<tr>
<td>Slip model</td>
<td>Preferred deviation function</td>
</tr>
<tr>
<td>Slip definition</td>
<td>American</td>
</tr>
<tr>
<td>Disk friction</td>
<td>Rear disk friction only</td>
</tr>
<tr>
<td>Recirculation power</td>
<td>Variable Power</td>
</tr>
<tr>
<td>Impeller Diffusion</td>
<td>Specific Speed Function</td>
</tr>
<tr>
<td>Two-zone calculation</td>
<td>Based on tip to tip</td>
</tr>
<tr>
<td>Exit width design model</td>
<td>User Specified Lam2</td>
</tr>
</tbody>
</table>

### Volute-Geometry

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Setting</th>
</tr>
</thead>
<tbody>
<tr>
<td>Dimensions</td>
<td>Variable</td>
</tr>
<tr>
<td>Type</td>
<td>Symmetric (22.5 deg)</td>
</tr>
<tr>
<td>Nominal Area at 0 degrees</td>
<td>Fixed</td>
</tr>
<tr>
<td>Radius (VR7/R5)</td>
<td>1.0</td>
</tr>
<tr>
<td>Station 8 exit diameter ratio</td>
<td>2.0</td>
</tr>
</tbody>
</table>

### Volute-Properties

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Setting</th>
</tr>
</thead>
<tbody>
<tr>
<td>LC57Mult</td>
<td>1.0</td>
</tr>
<tr>
<td>CP57</td>
<td>-1.370E-4</td>
</tr>
<tr>
<td>CP78Mult</td>
<td>1.0</td>
</tr>
<tr>
<td>Volute exit cone model</td>
<td>Blockage correction</td>
</tr>
<tr>
<td>Impeller exit area multiplier</td>
<td>1.1</td>
</tr>
</tbody>
</table>
Bibliography


3 Stucke, Brian A. and Anderl, Timothy R., “Doubling our Reach to Space,” The AMPTIAC Quarterly, Volume 8, Number 1, 2004, pp.35-38.


11 National Aeronautics and Space Administration, Turbopump Systems for Liquid Rocket Engines, NASA SP-8107, August 1974


20 Fukushima, Y and Imoto, T, Lessons Learned in the Development of the LE-5 and LE-7 AIAA-94-3375.


37 National Aeronautics and Space Administration, Numerical Propulsion Simulation System, v1.6.4, 30 May 2006


59 Concepts NERC, AxCent v. 7.9.16.0, July 2006.


Vita


Capt Strain’s first assignment was to Kirtland AFB, NM where he was a Laser System Engineer in the Airborne Laser System Program Office. He entered the Graduate School of Engineering and Management, Air Force Institute of Technology, WPAFB, Ohio in March 2006. After graduation, he will be assigned to the National Air and Space Intelligence Center, WPAFB, OH.
Design Of An Oxygen Turbopump For A Dual Expander Cycle Rocket Engine

The design of a pump intended for use with a dual expander cycle (LOX/H₂) engine is presented. This arrangement offers a number of advantages over hydrogen expander cycles; among these are the elimination of gearboxes and inter-propellant purges and seals, an extended throttling range, and higher engine operating pressures and performance. The target engine has been designed to meet the needs of Phase III of the Integrated High Payoff Rocket Propulsion Technology (IHPRPT) program; thus, this pump must meet the program’s reliability, maintainability, and service life goals. In addition, this pump will be driven by warm gaseous oxygen. In order to meet the needs of this engine, the pump will need to be capable of delivering 106 lbm/s (48.1 kg/s) at 4500 psi (31 MPa); this will necessitate a turbine capable of supplying at least 2215 hp (1652 kW). The pump and turbine were designed with the aid of an industry standard design program; the design methodology and justification for design choices are presented. Appropriate materials of construction and bearings for this pump are discussed.

Dual expander cycle engine, LOX/H₂, upper stage, turbopump, liquid oxygen, oxygen driven turbine, throttletability, NPSS, IHPRPT, hybrid bearings

<table>
<thead>
<tr>
<th>16. SECURITY CLASSIFICATION OF:</th>
<th>17. LIMITATION OF ABSTRACT</th>
<th>18. NUMBER OF PAGES</th>
</tr>
</thead>
<tbody>
<tr>
<td>a. REPORT</td>
<td>U</td>
<td>84</td>
</tr>
<tr>
<td>b. ABSTRACT</td>
<td>U</td>
<td></td>
</tr>
<tr>
<td>c. THIS PAGE</td>
<td>U</td>
<td></td>
</tr>
</tbody>
</table>

19a. NAME OF RESPONSIBLE PERSON
Richard D. Branam, Maj, USAF

19b. TELEPHONE NUMBER (include area code)
(937) 255-3636, ext 7485
(rbranam@afit.edu)